

# Introduction to Imaging in CASA



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**NRAO**

Atacama Large Millimeter/submillimeter Array

Expanded Very Large Array

Robert C. Byrd Green Bank Telescope

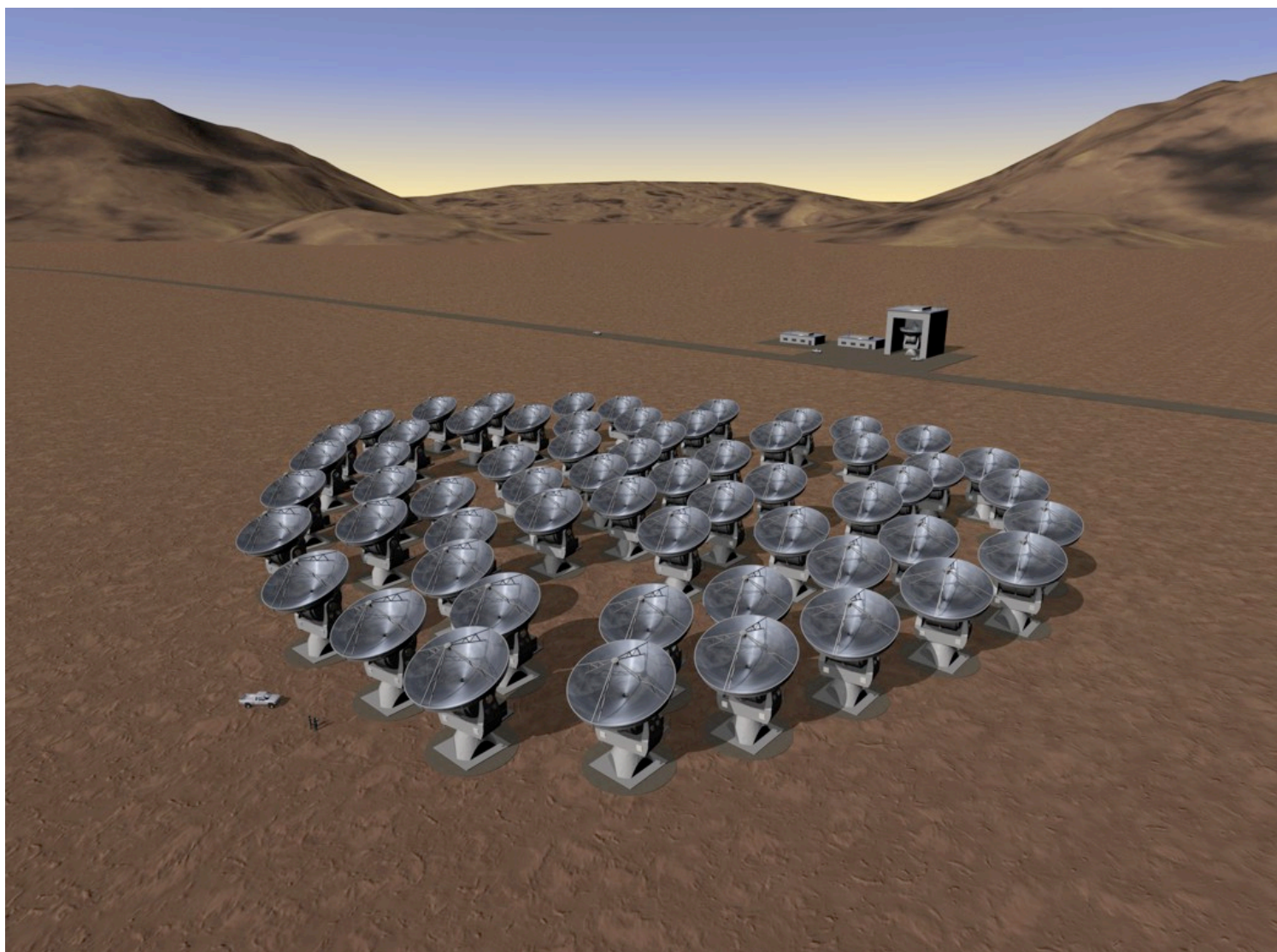
Very Long Baseline Array



# Overview

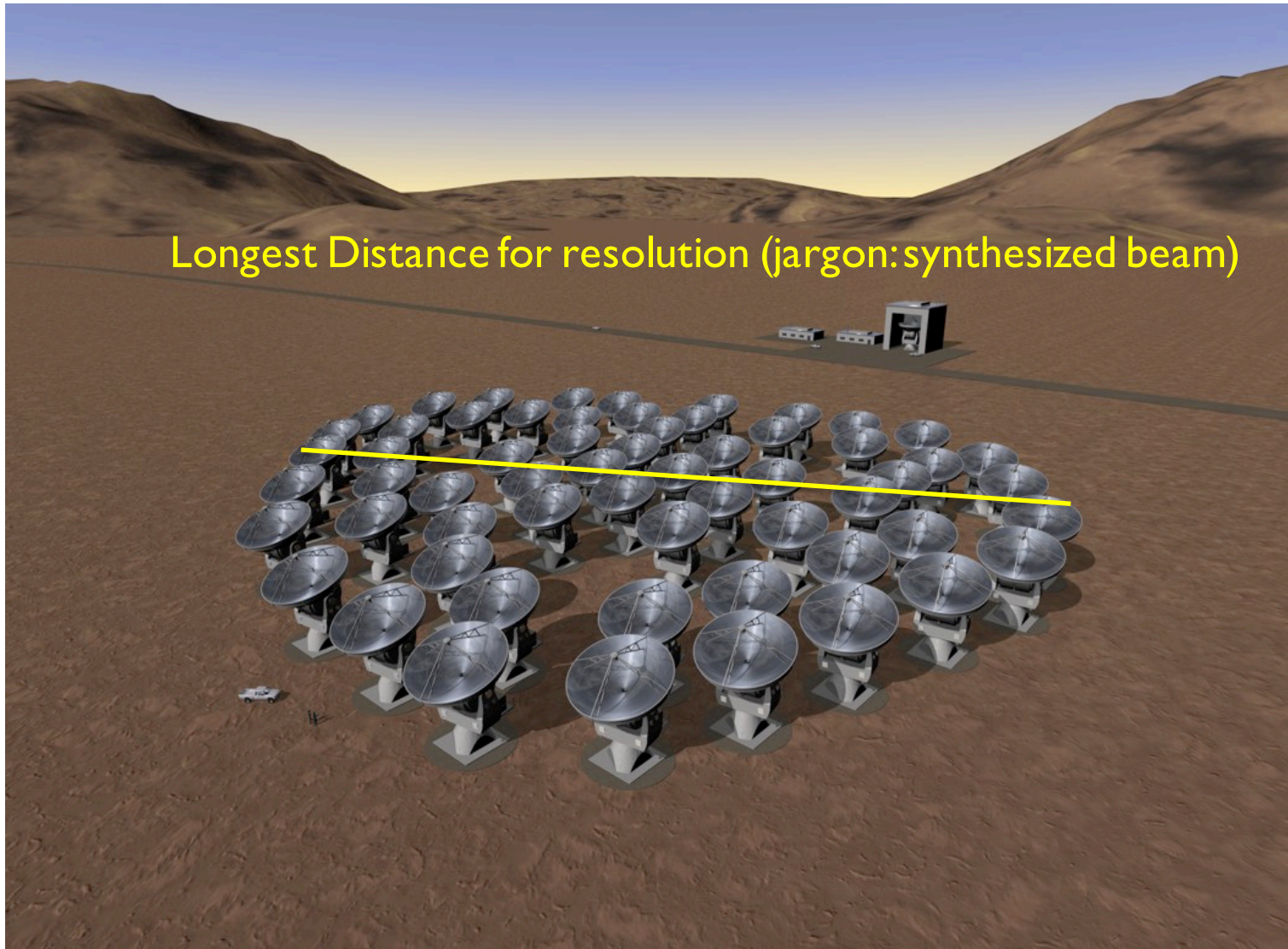
- Goals of this talk:
  - Gain some intuition for interferometric imaging
  - Introduce deconvolution in CASA (CLEAN)
  - Introduce various imaging methods available in CASA
- More formal description of imaging available in NRAO Synthesis Imaging Workshop lectures, especially David Wilner and Greg Taylor's talks from the 2014 workshop (available as powerpoint and videos).
- Also, sign up for the Synthesis Imaging Summer School this summer! More fun than a boatful of sopapillas.







Longest Distance for resolution (jargon: synthesized beam)

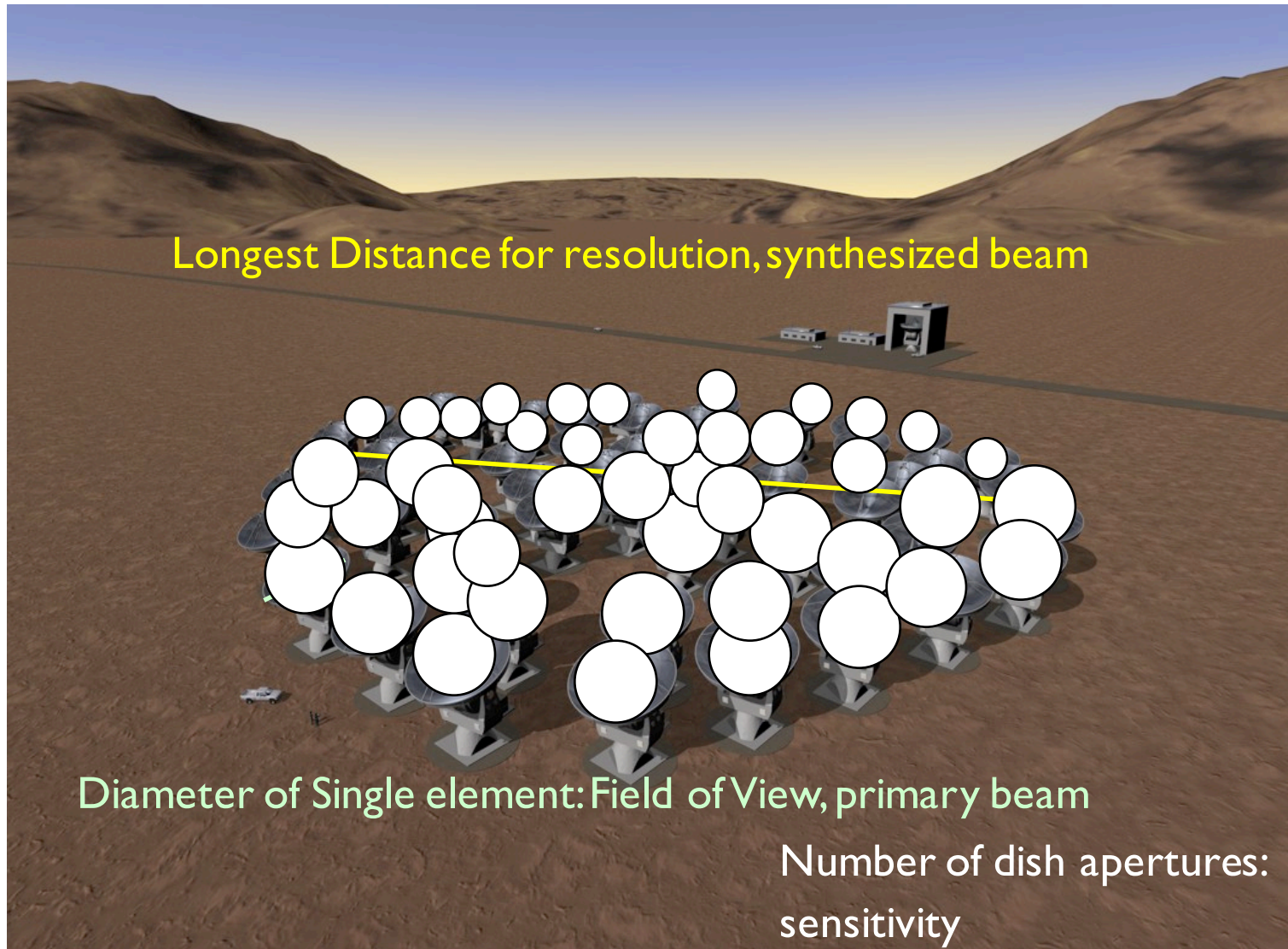






Longest Distance for resolution (jargon:synthesized beam)

Diameter of Single element: Field of View (jargon:primary beam)



# From Sky Brightness to Visibility

1. An interferometer measures the interference pattern observed by pairs of apertures
2. The interference pattern is directly related to the source brightness. In particular, for small fields of view the complex visibility,  $V(u,v)$ , is the 2D Fourier transform of the brightness on the sky,  $T(x,y)$

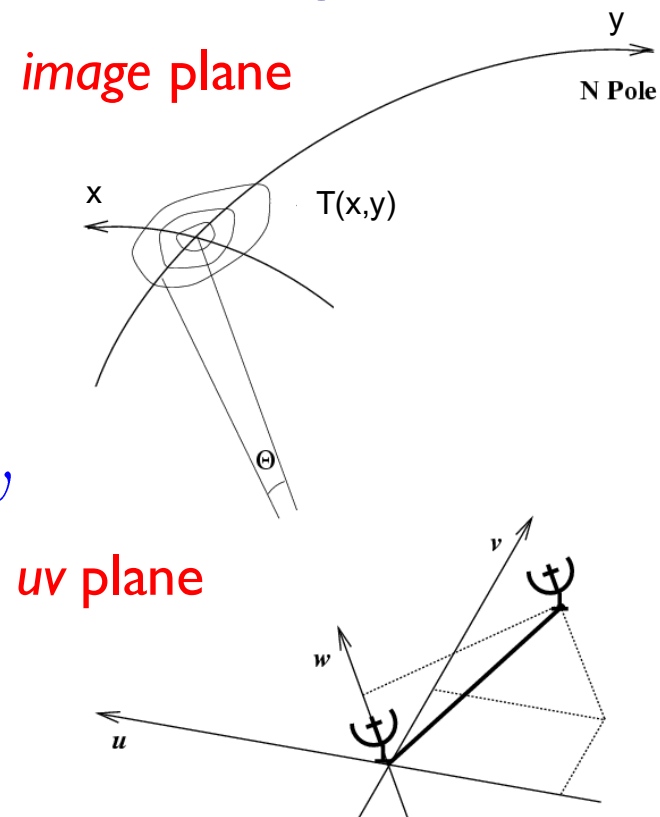
(van Cittert-Zernike theorem)

Fourier space/domain

$$V(u, v) = \iint T(x, y) e^{2\pi i(ux+vy)} dx dy$$

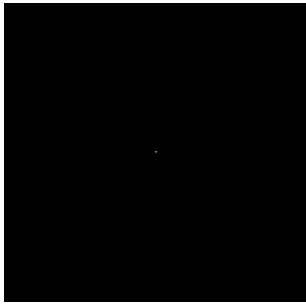
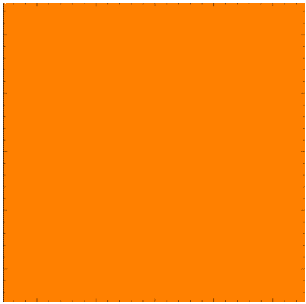
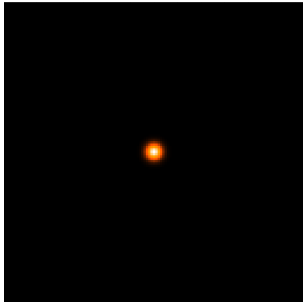


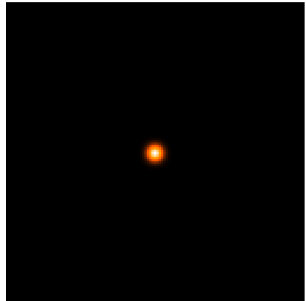
$$T(x, y) = \iint V(u, v) e^{-2\pi i(ux+vy)} du dv$$

Image space/domain





# Some 2D Fourier Transform Pairs

$T(x,y)$			$\text{Amp}\{V(u,v)\}$
$\delta$ Function		$\longleftrightarrow$	
Gaussian		$\longleftrightarrow$	
Gaussian		$\longleftrightarrow$	

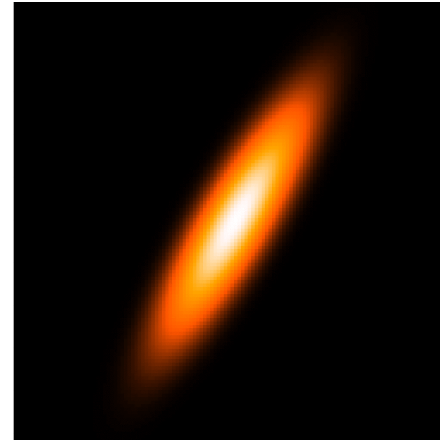
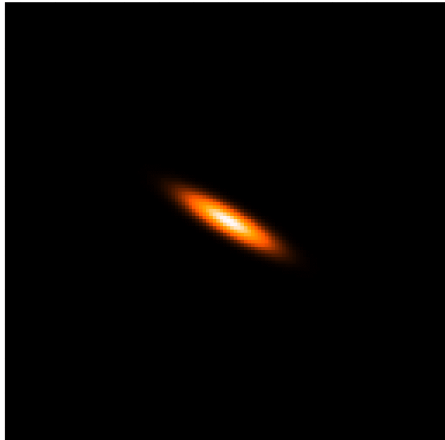


narrow features transform to wide features (and vice-versa)

# More 2D Fourier Transform Pairs

$T(x,y)$

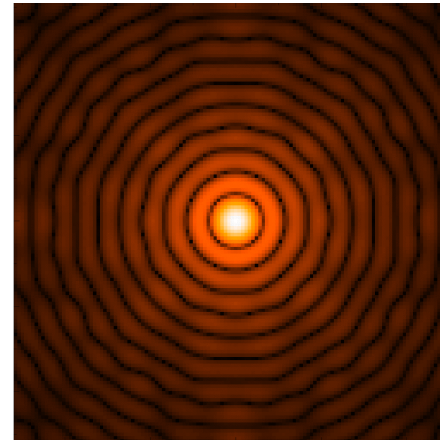
elliptical  
Gaussian



$\text{Amp}\{V(u,v)\}$

elliptical  
Gaussian

Disk

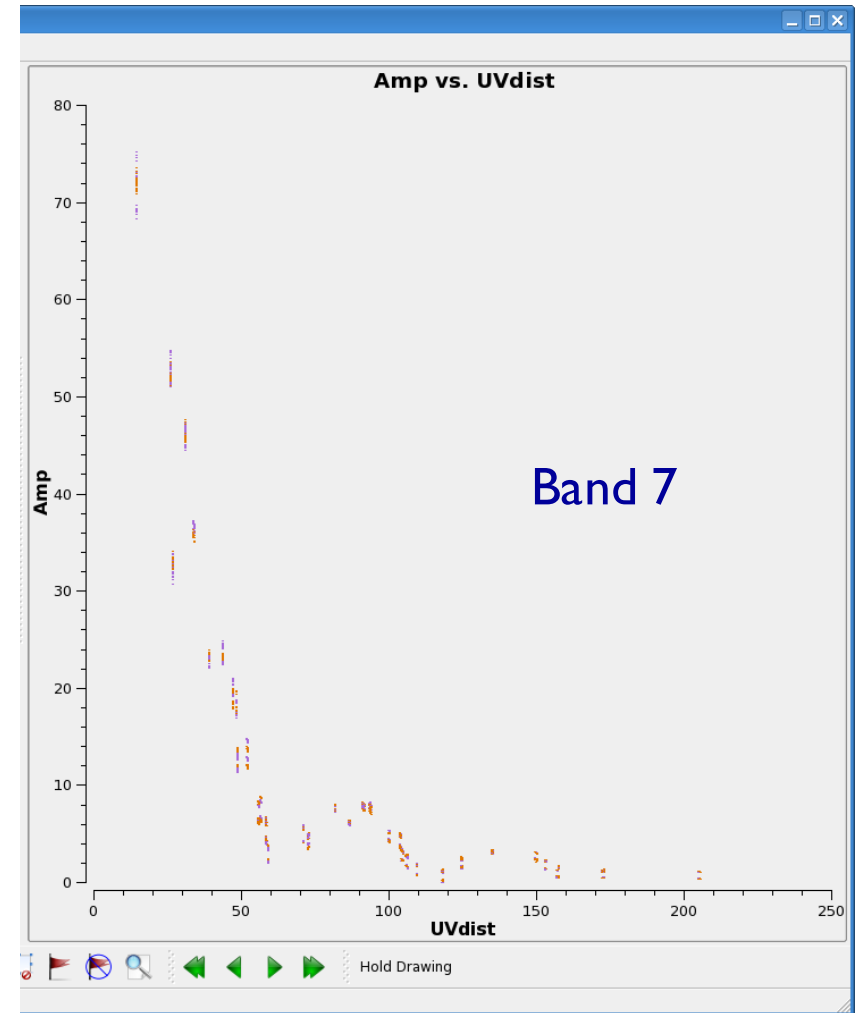
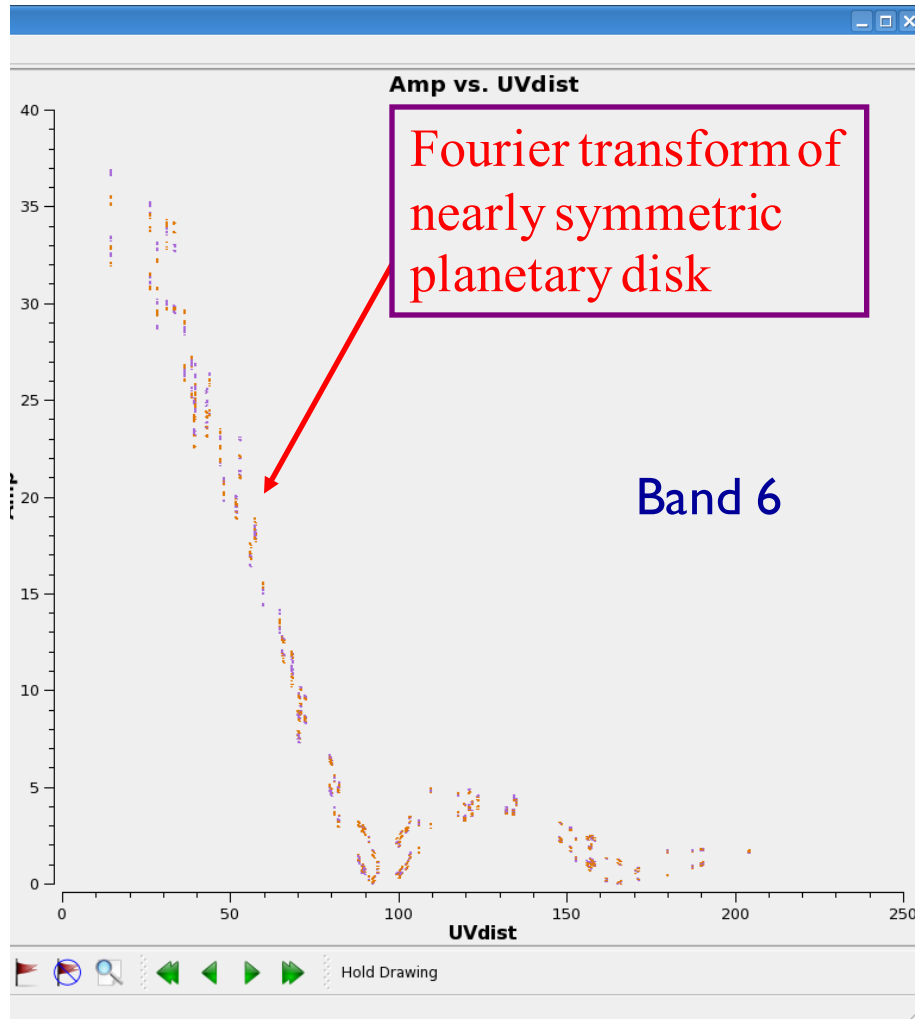


Bessel



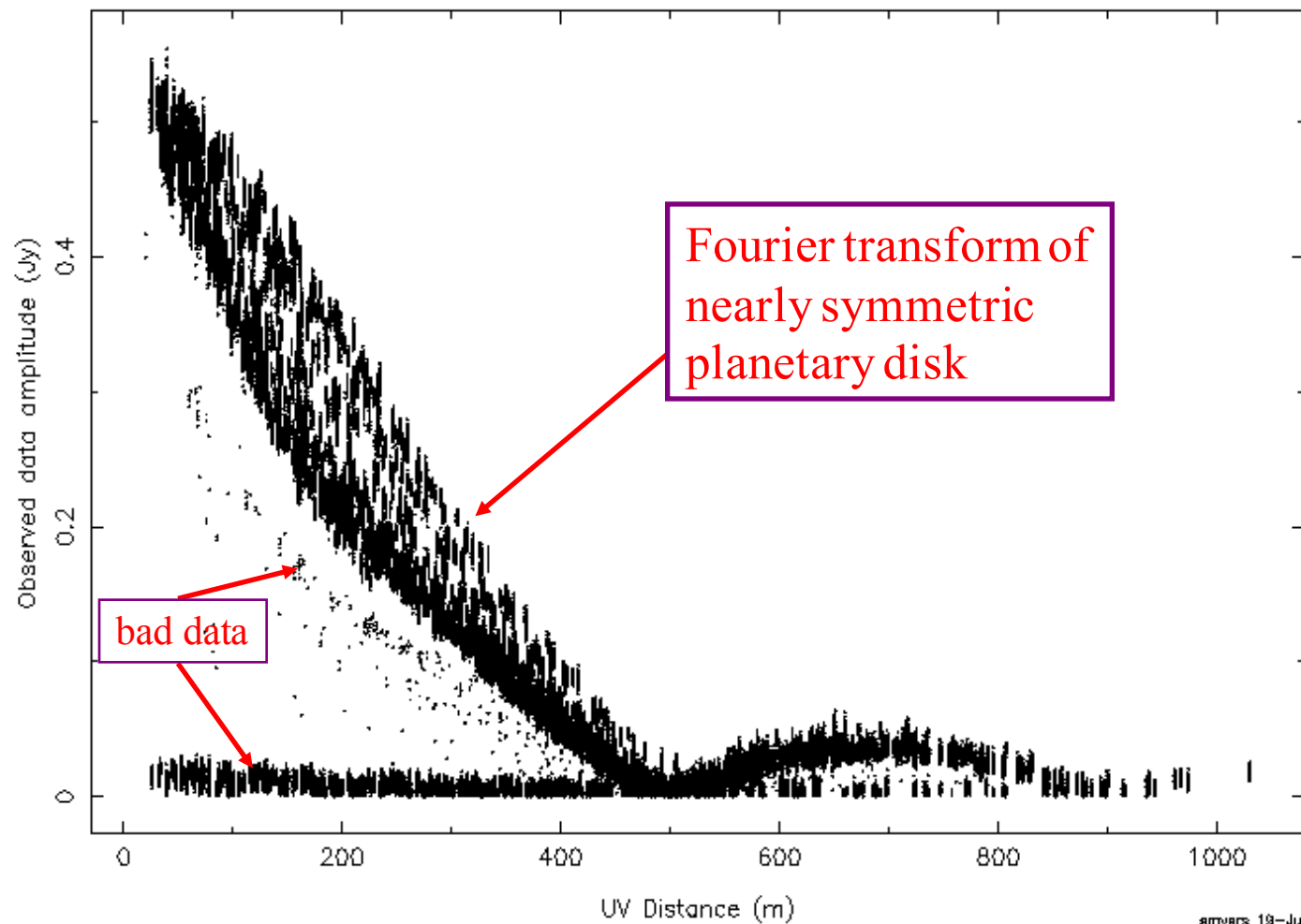
sharp edges result in many high spatial frequencies  
(sinc function, “ringing”, Gibbs phenomenon)

# ALMA observes planetary disk



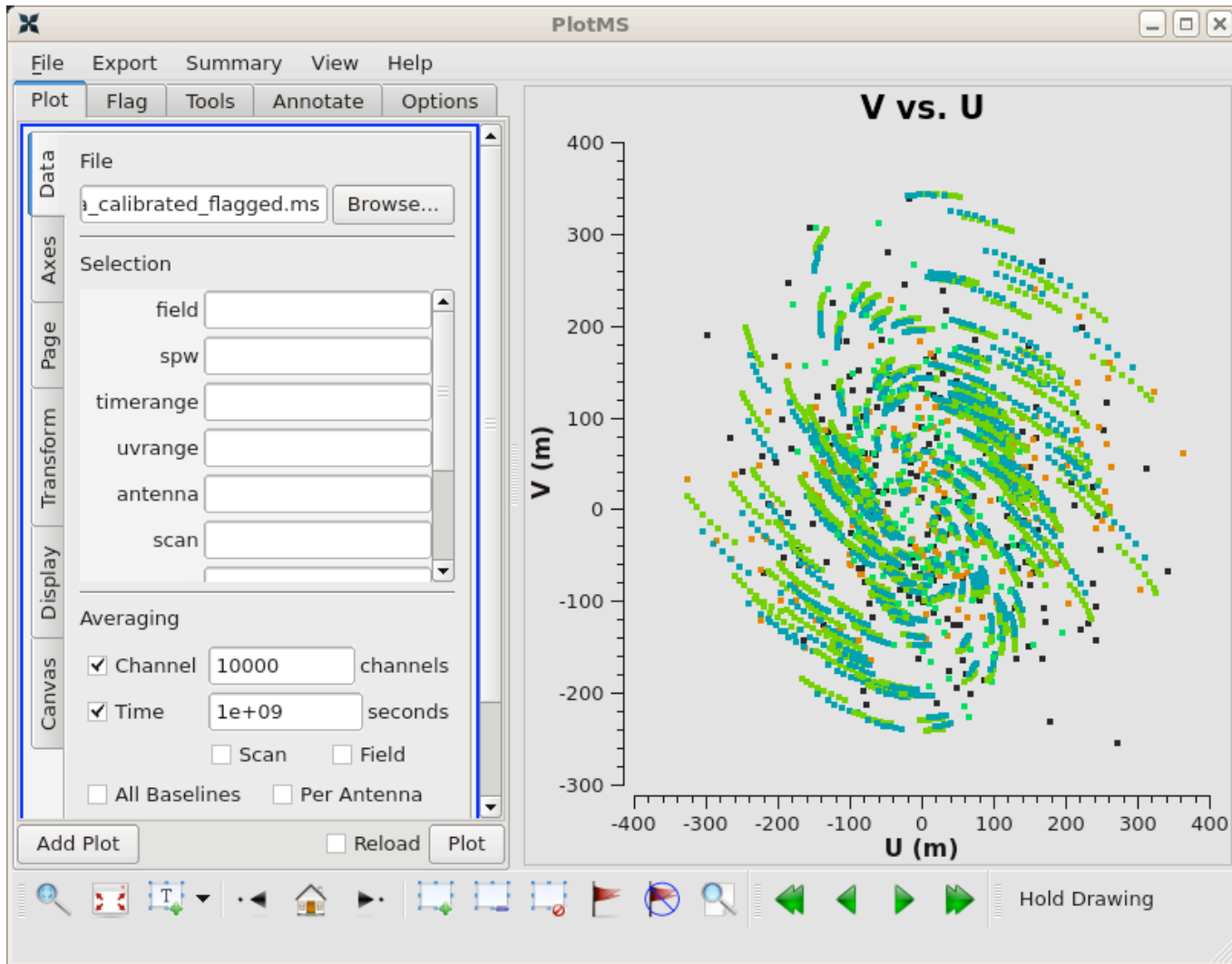


# VLA observes Jupiter (6cm)



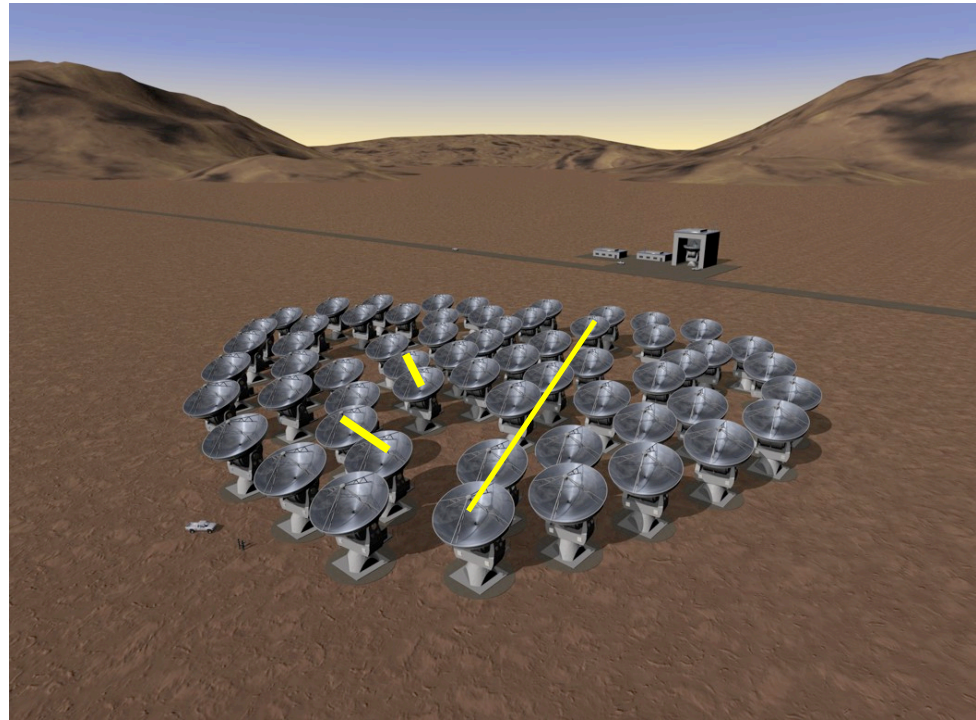
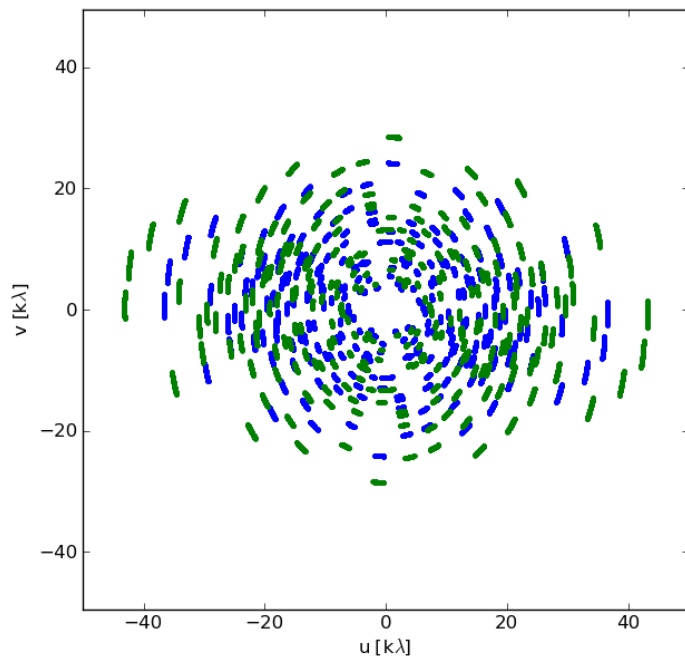
S.T. Myers

# Plotms: Versatile examination of UV data



# Sampling Function

Interferometers cannot see the entire Fourier/uv domain. But each antenna pair samples one spot: → **imperfect image**



Small uv-distance: short baselines (measure extended emission)

Long uv-distance: long baselines (measure small scale emission)

Orientation of baseline also determines orientation in the uv-plane

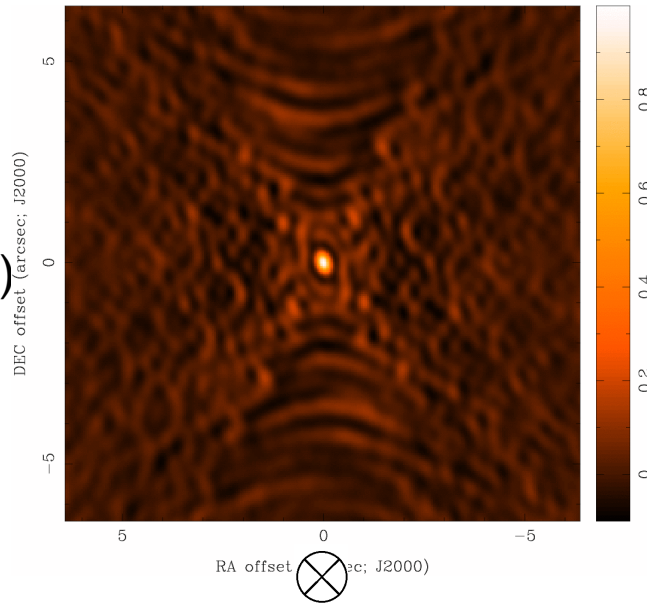
Each visibility has a phase and an amplitude



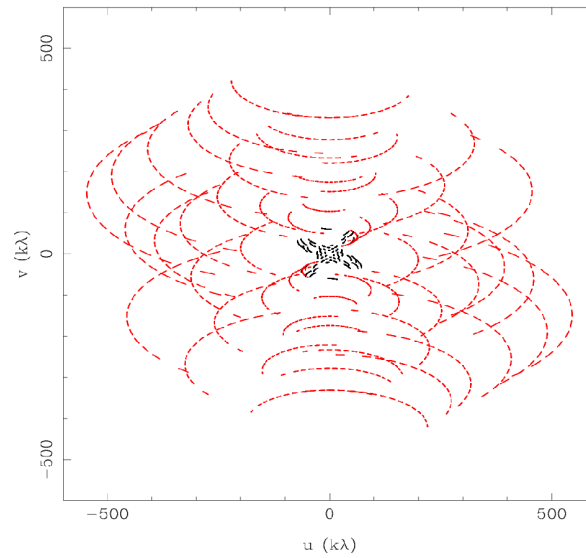


# Dirty Beam and Dirty Image

$b(x,y)$   
(dirty beam)

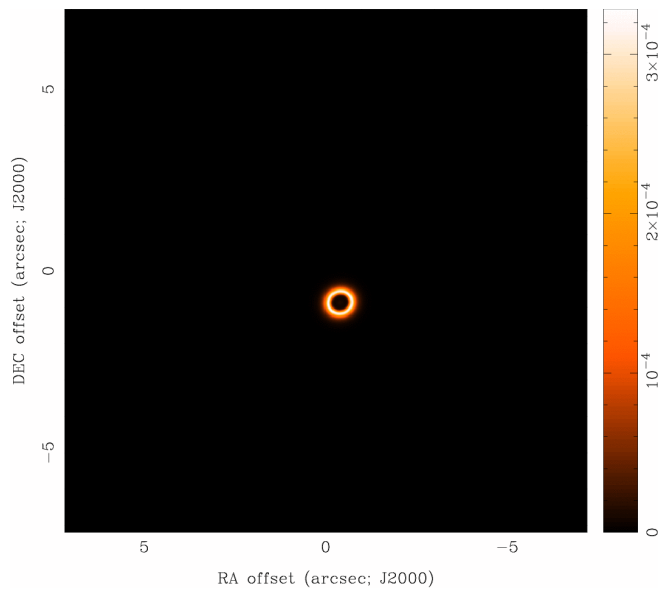


$\Downarrow$

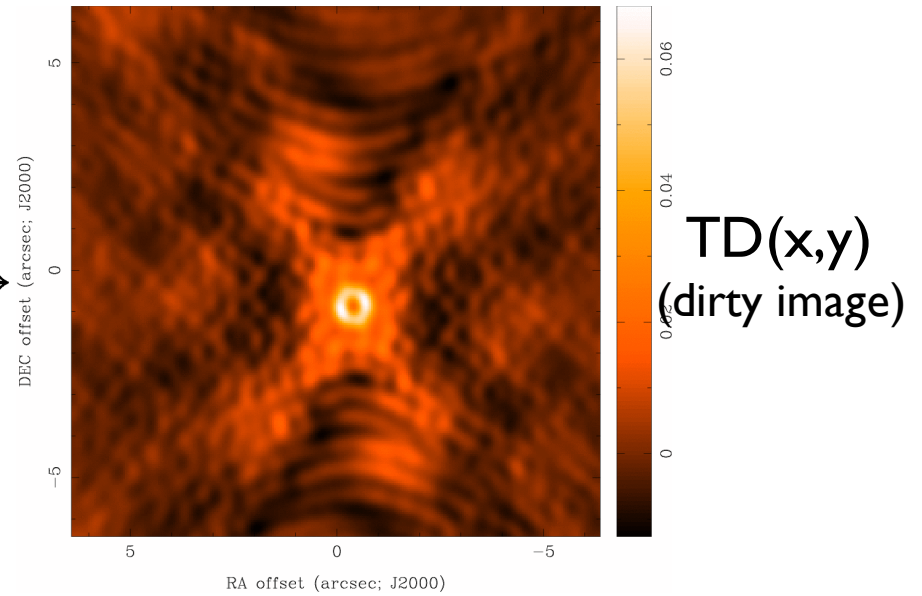


$B(u,v)$

$T(x,y)$



$\rightarrow$

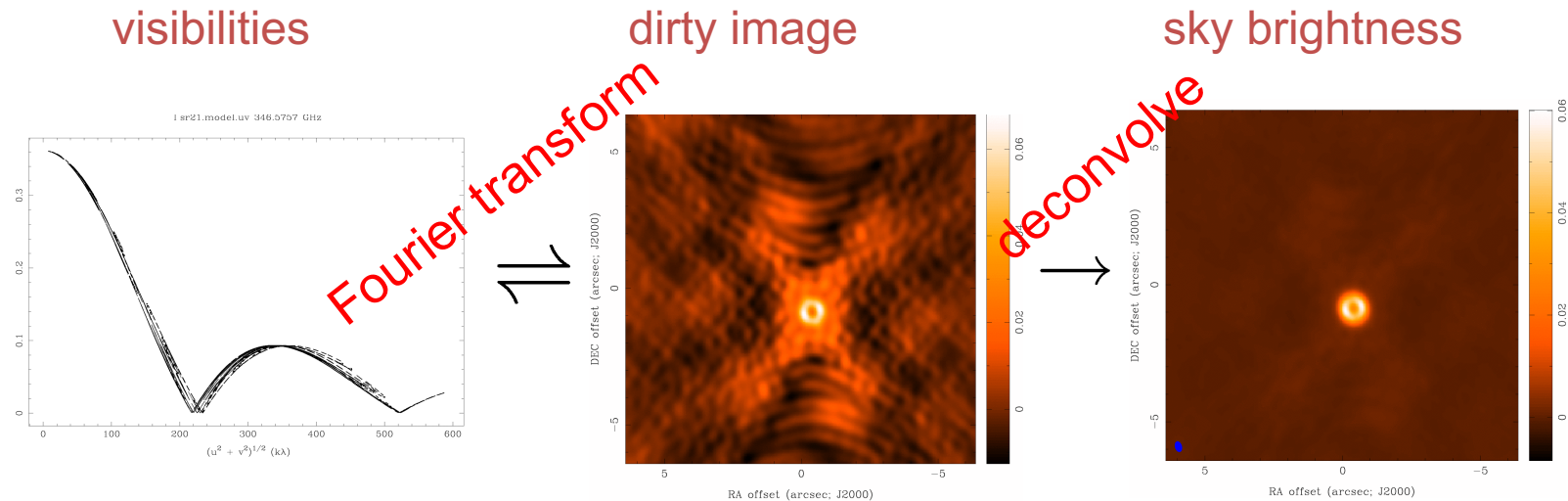


$TD(x,y)$   
(dirty image)

# How to analyze (imperfect) interferometer data

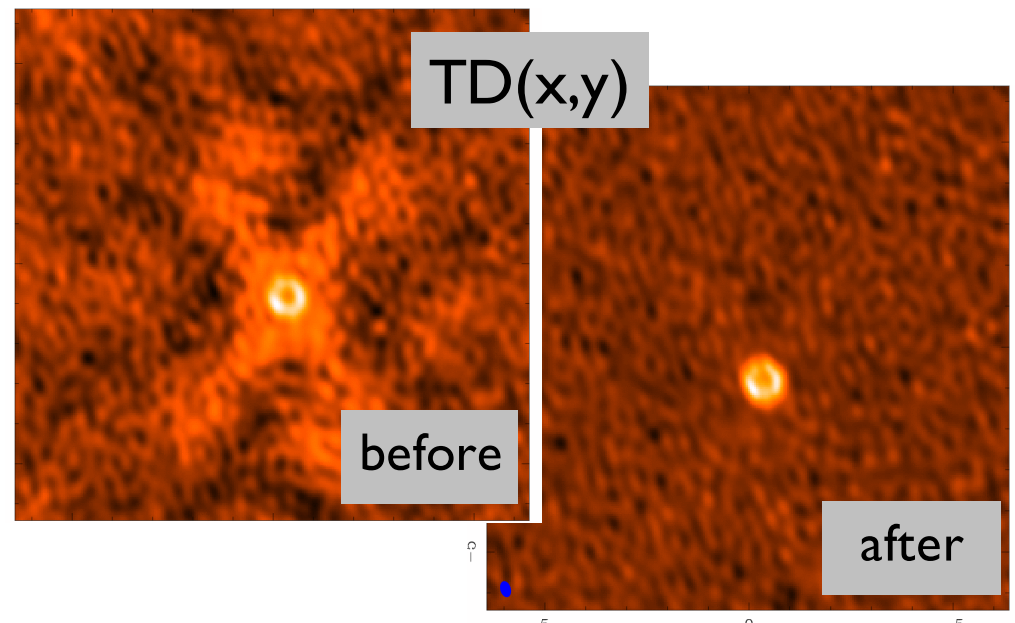
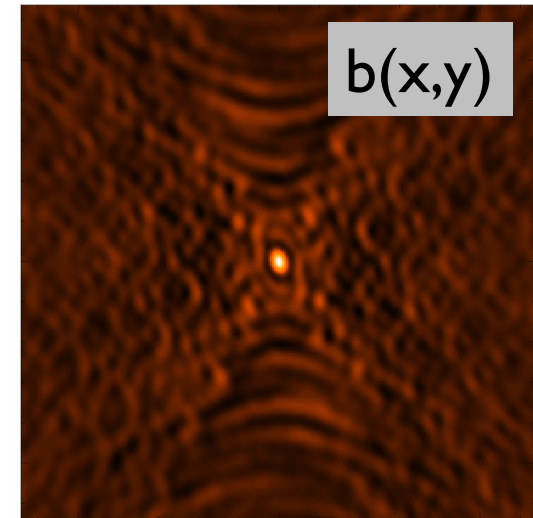
## Image plane analysis

- dirty image  $TD(x,y)$  = Fourier transform  $\{V(u,v)\}$
- deconvolve  $b(x,y)$  from  $TD(x,y)$  to determine (model of)  $T(x,y)$



# Basic CLEAN Algorithm

- A. Initialize a *residual* map to the dirty map
  1. Start loop
  2. Identify strongest feature in *residual* map as a point source
  3. Add this point source to the clean component list
  4. Convolve the point source with  $b(x,y)$  and subtract a fraction  $g$  (the loop gain) of that from *residual* map
  5. If stopping criteria not reached, do next iteration
- B. Convolve *Clean component* (cc) list by an estimate of the main lobe of the dirty beam (the “Clean beam”) and add *residual* map to make the final “restored” image





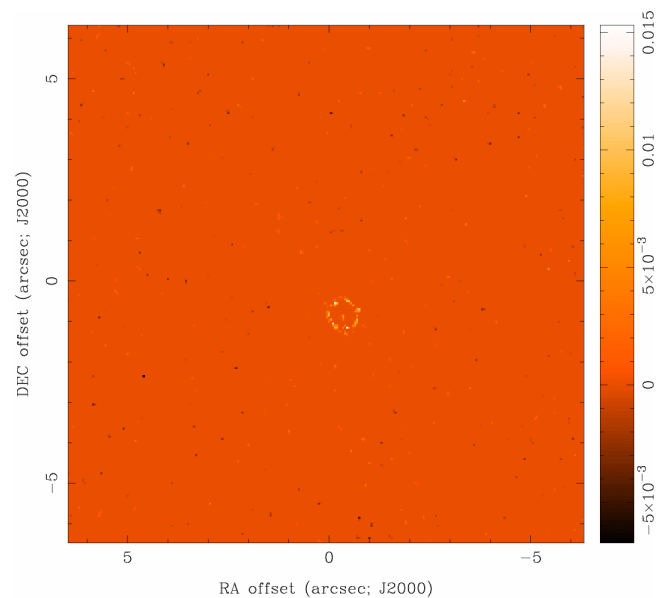
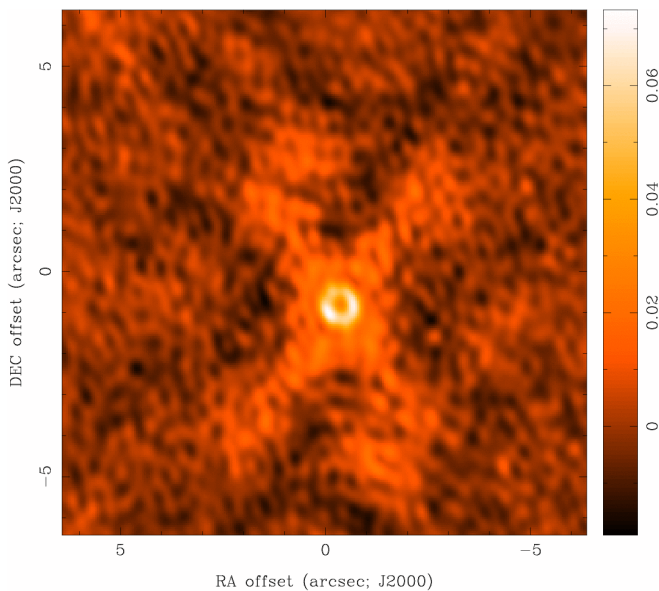
# Basic CLEAN Algorithm (cont.)

- Stopping criteria [recommend interactively cleaning to start]
  - *residual* map max < multiple of rms (when noise limited)
  - *residual* map max < fraction of dirty map max (dynamic range limited)
  - max number of clean components reached (no justification)
- Loop gain [default usually okay]
  - good results for  $g \sim 0.1$  to  $0.3$
  - lower values can work better for smoother emission,  $g \sim 0.05$ , but other methods (multi-scale clean) may be more effective.
- Easy to include *a priori* information about where to search for clean components (“clean boxes”) [strongly recommended]
  - very useful but need to exercise caution to only box real emission.



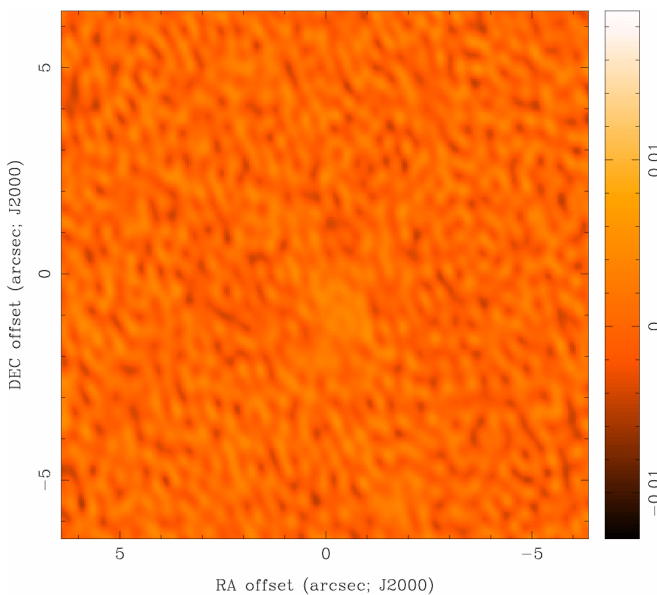
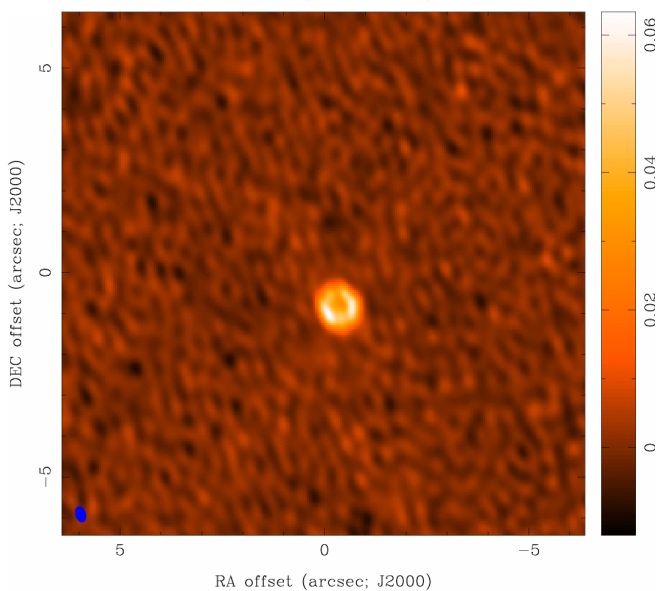
# CLEAN

TD(x,y)



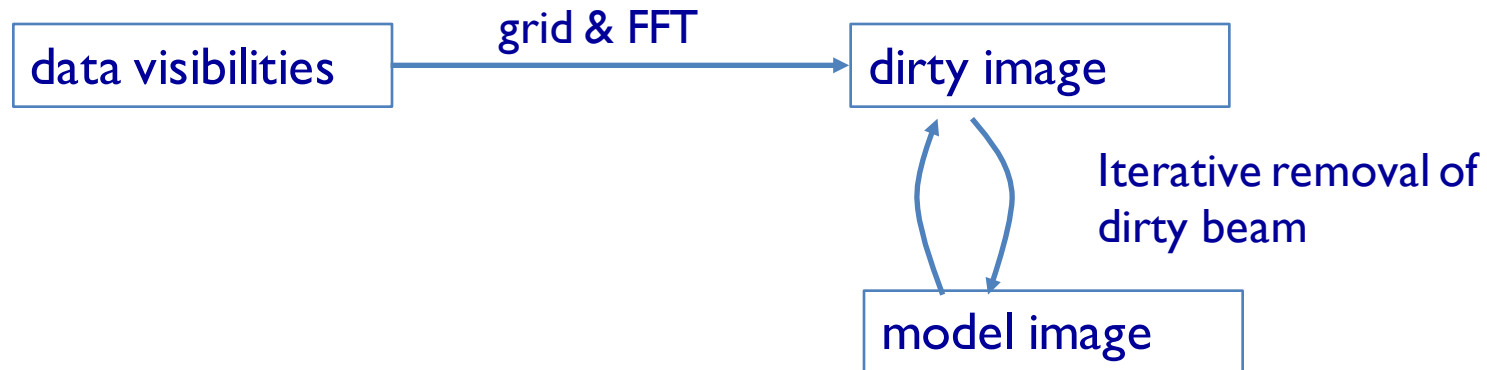
CLEAN  
model

restored  
image



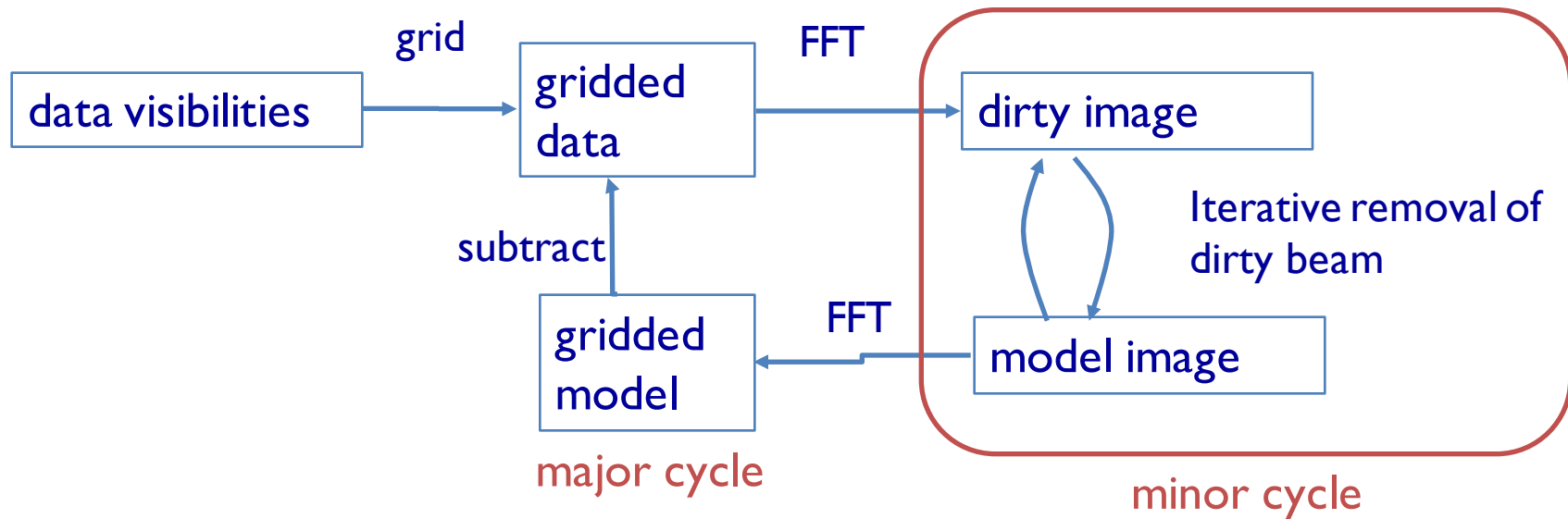
residual  
map

# Deconvolution algorithms : Hogbom



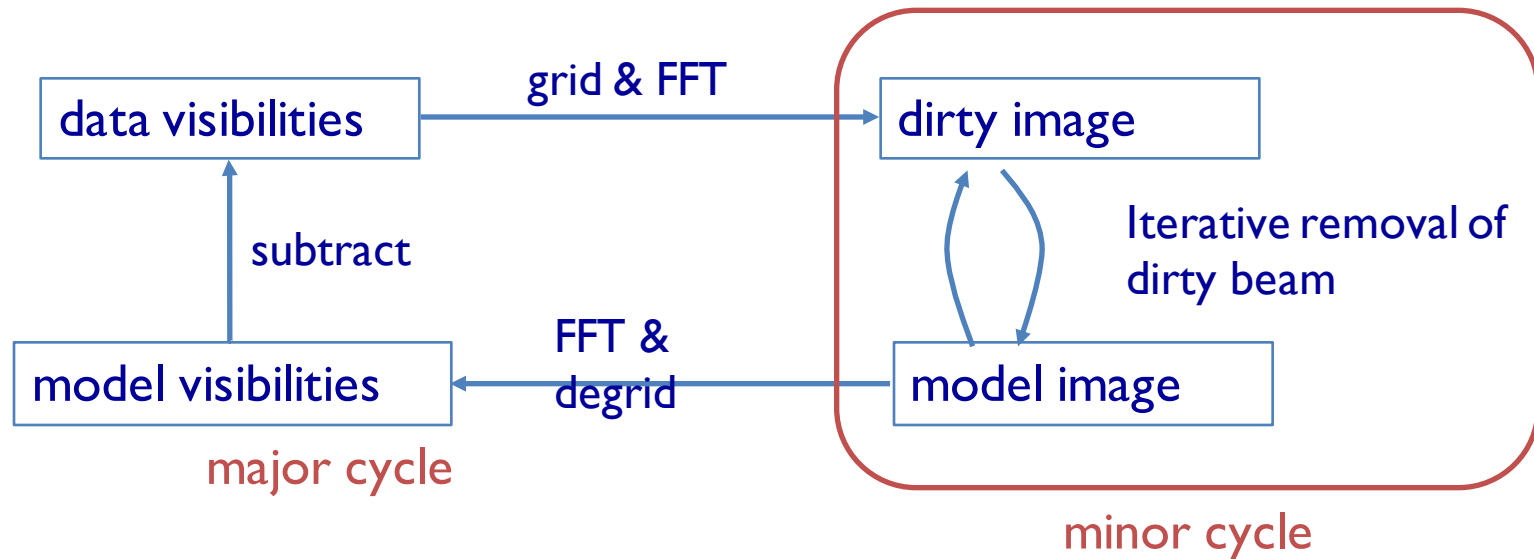
- Subtracts full PSF in image domain
- Typically not a preferred algorithm
- Errors can build for complex images
- Slow, but may be a good option for poor uv coverage (i.e., PSF for large sidelobes)

# Deconvolution algorithms : Clark



- Subtracts truncated PSF in image domain
- Periodically subtracts from gridded data in uv domain

# Deconvolution algorithms: Cotton-Schwab



Cotton-Schwab (csclean):

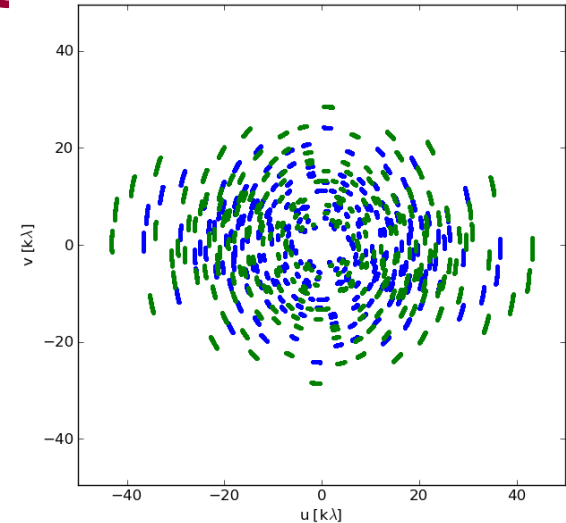
- subtracts truncated PSF in image domain
- major cycle subtracts from full visibilities
- significant I/O per major cycle





# Dirty Beam Shape and Weighting

- Each visibility point is given a weight in the imaging step
- First piece: weight given by  $T_{\text{sys}}$ , integration time, etc.
- **Natural**
  - Each sample is given the same weight
  - There are many samples at short baselines, so natural weighting will give the largest beam and the best surface brightness sensitivity (and sometimes pronounced wings in the dirty beam)



- **Uniform**
  - Each visibility is given a weight inversely proportional to the sample density
  - Weighs down short baselines, long baselines are more pronounced.
  - Best resolution; poorer noise characteristics
  - May also be affected by errors in long baselines.
- **Briggs (Robust)**
  - A graduated scheme using the parameter *robust*; compromise of noise and resolution
  - In CASA, set *robust* from -2 ( ~ uniform) to +2 ( ~ natural)
  - *robust* = 0 often a good choice
- **Taper:** additional weight function to be applied (typically a Gaussian to suppress the weights of the outer visibilities – be careful, however, not to substantially reduce the collecting area)

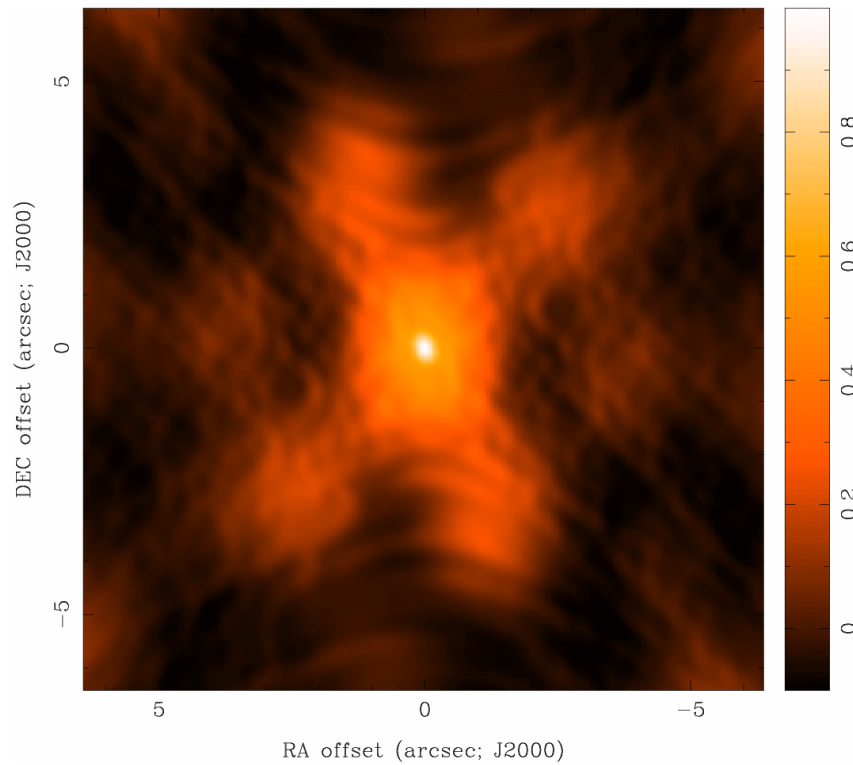
# Adjust the weighting to match your science goal

- Detection experiment/weak extended source:  
**natural** (maybe even with a taper)
- Finer detail of strong sources: **robust** or even **uniform**

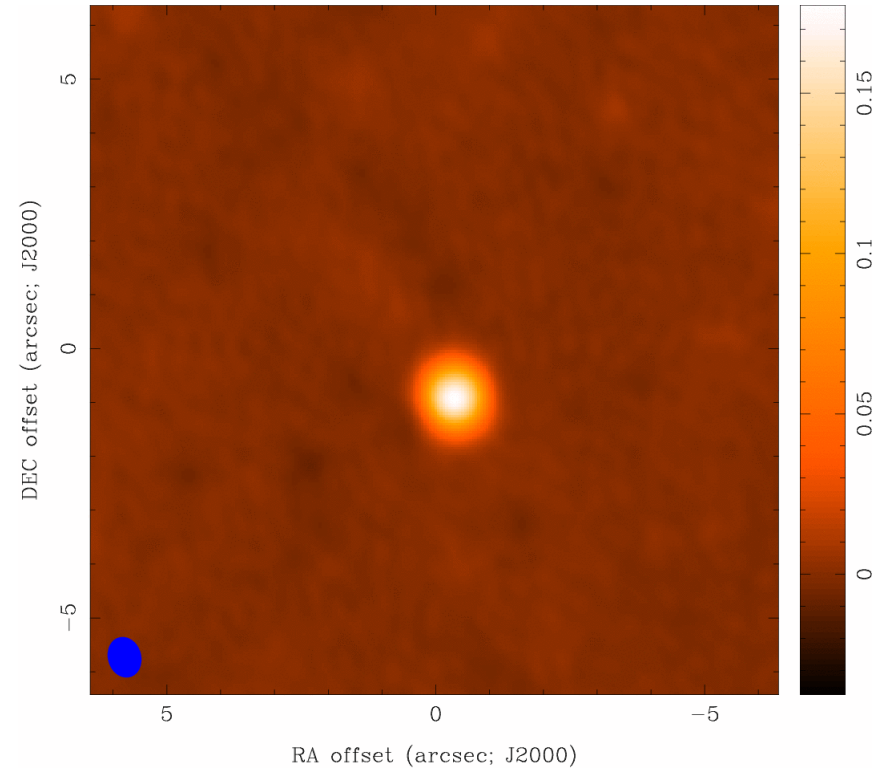


# Imaging Results

## Natural Weight Beam

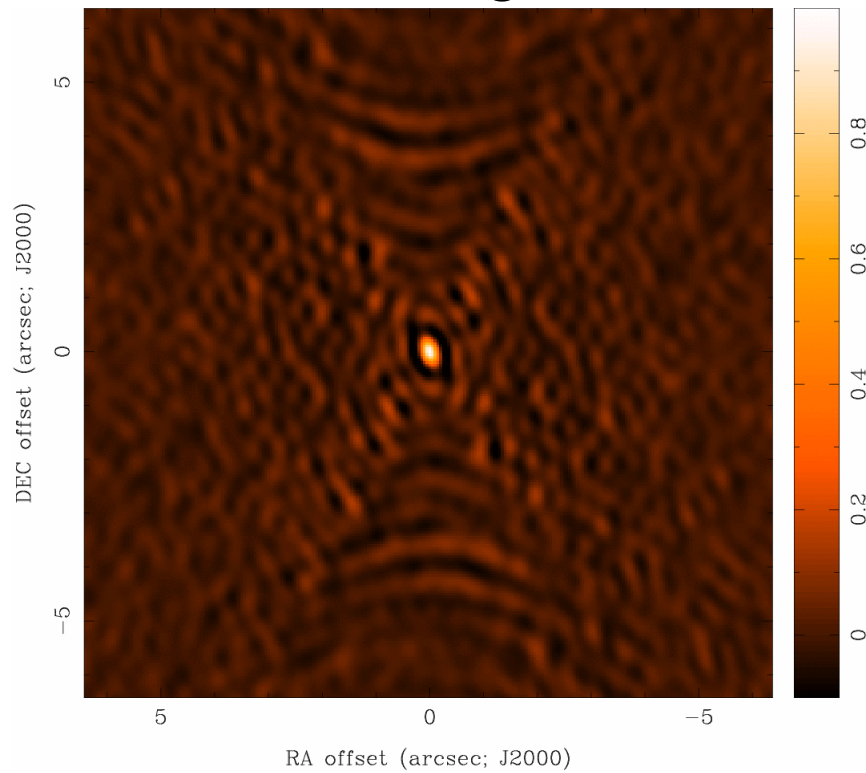


## CLEAN image

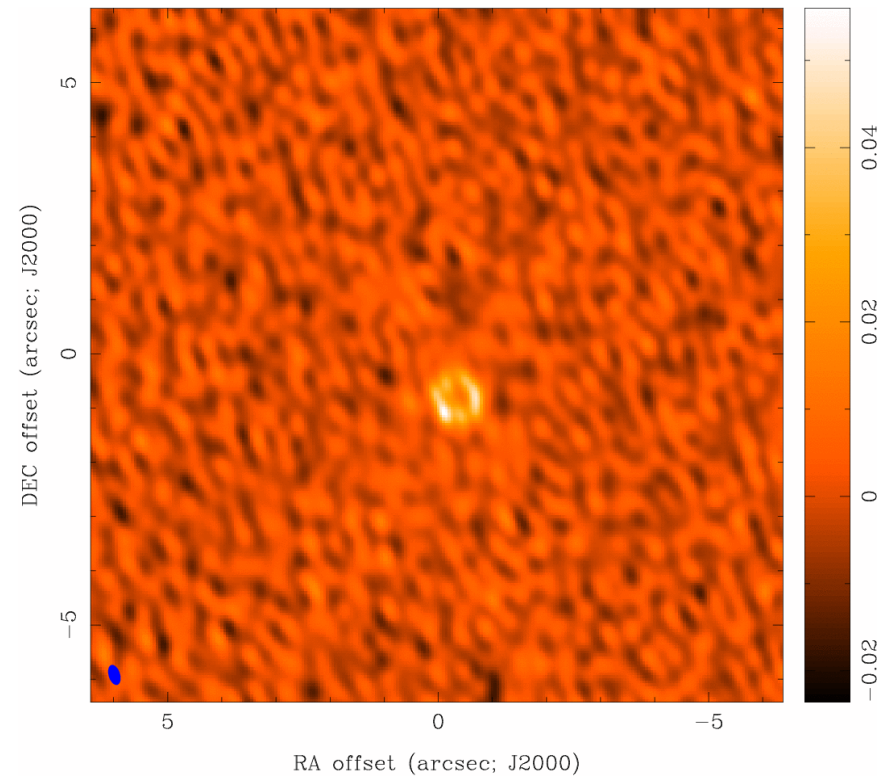


# Imaging Results

## Uniform Weight Beam



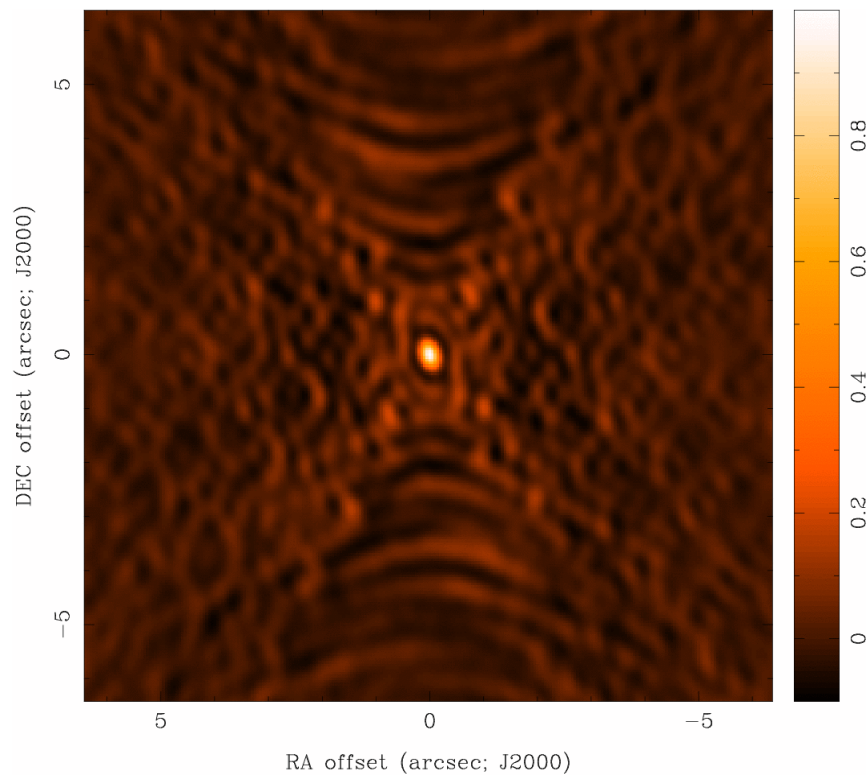
## CLEAN image



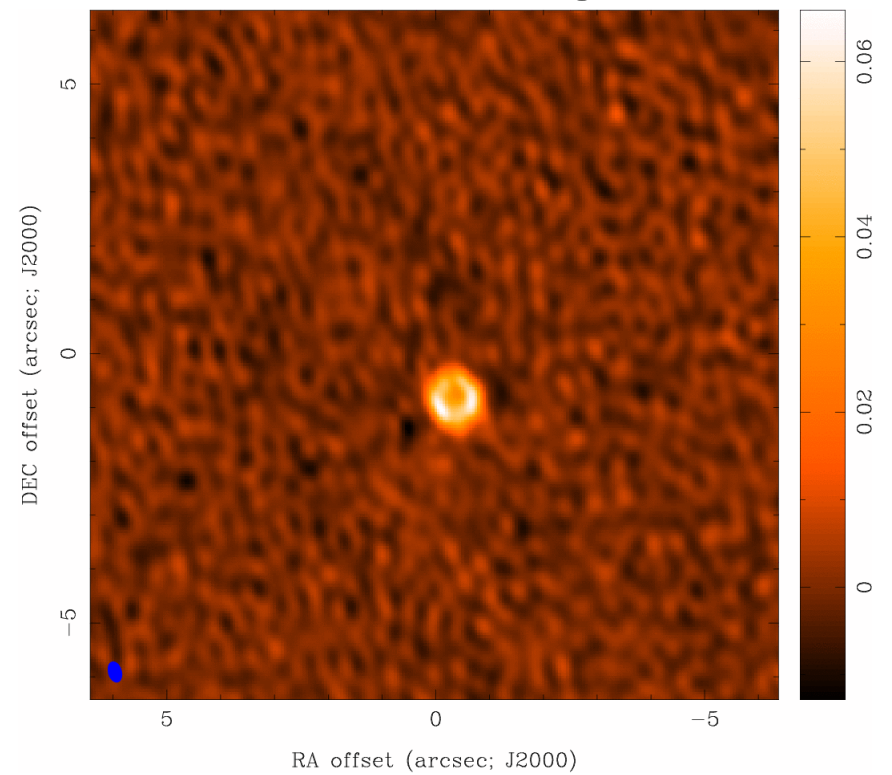


# Imaging Results

Robust=0 Beam



CLEAN image



# CLEAN in CASA

CLEAN is the current imaging task in CASA. It:

- takes the calibrated visibilities
- grids them on the UV-plane
- performs the FFT to a dirty image
- deconvolves the image
- restores the image from clean table and residual

## **Modes/Capabilities:**

- continuum: incl. multi-frequency synthesis (radial extend of each visibility due to bandwidth), and Taylor term expansion (to derive spectral index and curvature
- spectral line: data cubes (many planes) grids in velocity space, takes account of Doppler shift of line
- mosaicking: combine multiple pointings to single image
- w-projection/faceting for images beyond the half-power point [not as big a concern for ALMA]
- outlier fields to deconvolve strong sources in primary beam sidelobes [not as big a concern for ALMA]
- multiscale cleaning [very handy]
- primary beam correction
- Not all modes are available at the same time. A updated version of clean (tclean) is in development.



# CLEAN in CASA:

Don't panic at the large number of parameters!

You can start simple and get more complex!

I've highlighted things I usually change first.



```
CASA <3>: inp clean
-----> inp(clean)
# clean :: Invert and deconvolve images with selected algorithm
vis = '' # Name of input visibility file
imagename = '' # Pre-name of output images
outlierfile = '' # Text file with image names, sizes, centers for
# outliers
field = '' # Field Name or id
spw = '' # Spectral windows e.g. '0~3', '' is all
selectdata = True # Other data selection parameters
    timerange = '' # Range of time to select from data
    uvrange = '' # Select data within uvrange
    antenna = '' # Select data based on antenna/baseline
    scan = '' # Scan number range
    observation = '' # Observation ID range
    intent = '' # Scan Intent(s)

mode = 'mfs' # Spectral gridding type (mfs, channel, velocity,
# frequency)
gridmode = '' # Gridding kernel for FFT-based transforms,
# default='' None
niter = 500 # Maximum number of iterations
gain = 0.1 # Loop gain for cleaning
threshold = '0.0mJy' # Flux level to stop cleaning, must include
# units: '1.0mJy'
psfmode = 'clark' # Method of PSF calculation to use during minor
# cycles
imagermode = 'csclean' # Options: 'csclean' or 'mosaic', '', uses
# psfmode
    cyclefactor = 1.5 # Controls how often major cycles are done. (e.g.
# 5 for frequently)
    cyclespeedup = -1 # Cycle threshold doubles in this number of
# iterations

multiscale = [] # Deconvolution scales (pixels); [] = standard
# clean
interactive = False # Use interactive clean (with GUI viewer)
mask = [] # Cleanbox(es), mask image(s), region(s), or a
# level
imsize = [256, 256] # x and y image size in pixels. Single value:
# same for both
cell = ['1.0arcsec'] # x and y cell size(s). Default unit arcsec.
phasecenter = '' # Image center: direction or field index
restfreq = '' # Rest frequency to assign to image (see help)
stokes = 'I' # Stokes params to image (eg I,IV,IQ,IQV)
weighting = 'natural' # Weighting of uv (natural, uniform, briggs, ...)
uvtaper = False # Apply additional uv tapering of visibilities
modelimage = '' # Name of model image(s) to initialize cleaning
restoringbeam = [''] # Output Gaussian restoring beam for CLEAN image
pbcor = False # Output primary beam-corrected image
minpb = 0.2 # Minimum PB level to use
usescratch = False # True if to save model visibilities in
# MODEL_DATA column
allowchunk = False # Divide large image cubes into channel chunks
# for deconvolution
```

# Basic Image Parameters:

## Pixel Size and Image Size

- **Pixel size**

- should satisfy  $\Delta x < 1/2 u_{\max}$ ,  $\Delta y < 1/2 v_{\max}$  (Nyquist)
- in practice, 3 to 7 pixels across the main lobe of the beam
- can be determined by using plotms to look at amp vs. uvwave:
  - Beam size (") =  $206265.0 / (\text{longest baseline in wavelengths})$ .

- **Image size**

- Consider FWHM of primary beam. The ALMA 12m primary beam in arcsec scales as  $6300 / \nu[\text{GHz}]$  and the ALMA 7m primary beam in arcsec scales as  $10608 / \nu[\text{GHz}]$ , where  $\nu[\text{GHz}]$  is the sky frequency.
- Use mosaicking to image multiple pointings. Make sure to make these images much bigger than the area mapped to avoid aliasing!
- Not restricted to powers of 2; CASA performs best at given image sizes, rule of thumb:  $2^n * 10$
- If there are bright sources in the sidelobes, they will throw sidelobes onto the image, so image large to be able to clean them out, or use outlierfile to specify the positions of outlier fields





# Output of CLEAN

Minimally:

- |                                  |  |
|----------------------------------|--|
| • <code>my_image.flux</code>     | Relative sky sensitivity                   |
| • <code>my_image.image</code>    | Cleaned and restored image (Jy/clean beam) |
| • <code>my_image.mask</code>     | Clean “boxes”                              |
| • <code>my_image.model</code>    | Clean components (Jy/pixel)                |
| • <code>my_image.psf</code>      | Dirty beam                                 |
| • <code>my_image.residual</code> | Residual (Jy/dirty beam)                   |

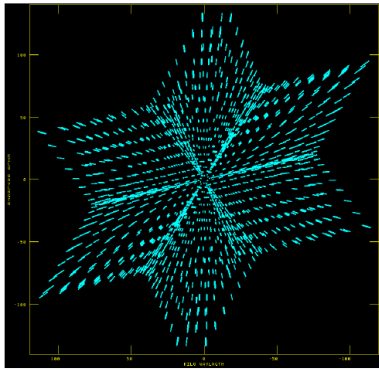
If CLEAN is started again with same image name, it will try to continue deconvolution from where it left off. Make sure this is what you want. If not, give a new name or remove existing files with `rmtables('my_image.*')`. It's generally a bad idea to delete some of the files output by clean.



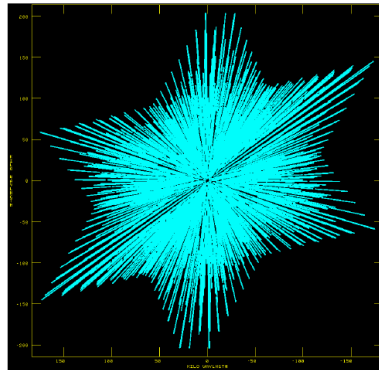
Try **NOT** to do CTRL+C as it could corrupt your MS!

# Continuum Imaging

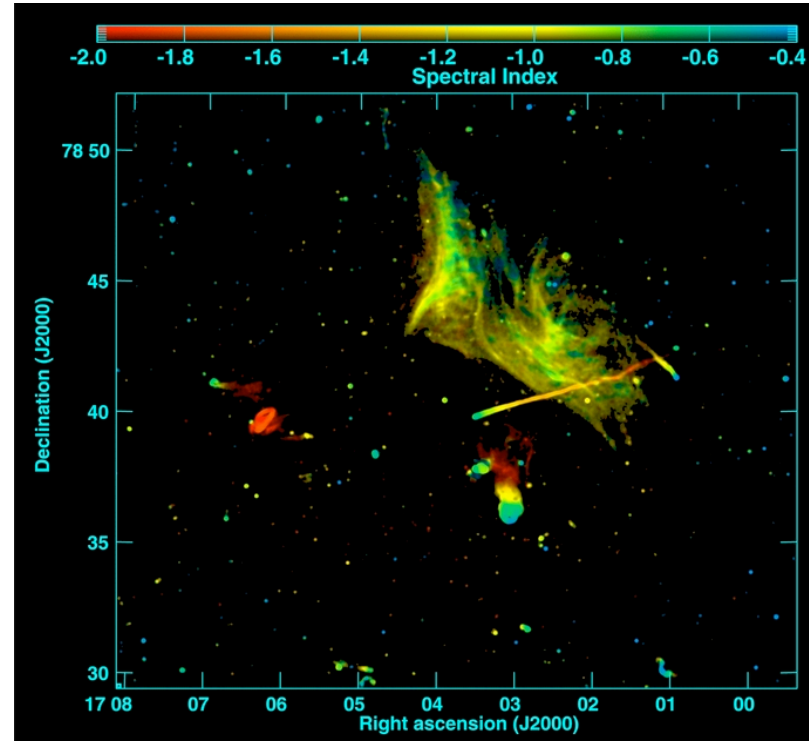
- Multi-scale Multi-Frequency Taylor Term expansion



Narrow BW



wide BW  
(better uv-coverage)



- Plus spectral index:

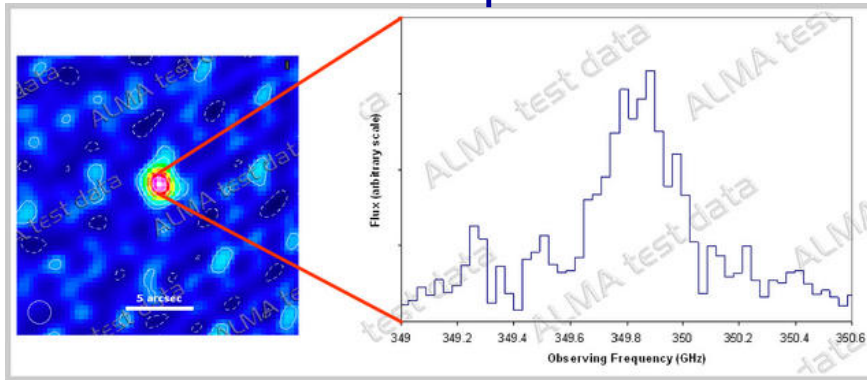
- MFS (mode mfs)
  - nterm=2 compute spectral index, 3 for curvature etc.
  - needed for bandwidths ~5% or more (S/N dependent)
  - tt0 average intensity, tt1  $\alpha \cdot tt0$ , alpha images output
  - takes at least nterms longer (image size dependent)
  - For most ALMA imaging, nterms=1 recommended (exception: band 3 continuum).

Abell 2256; Owen et al. (2014)

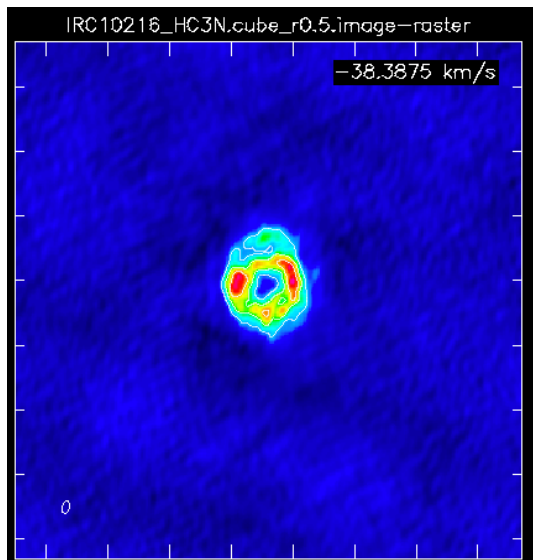


# Imaging spectral lines

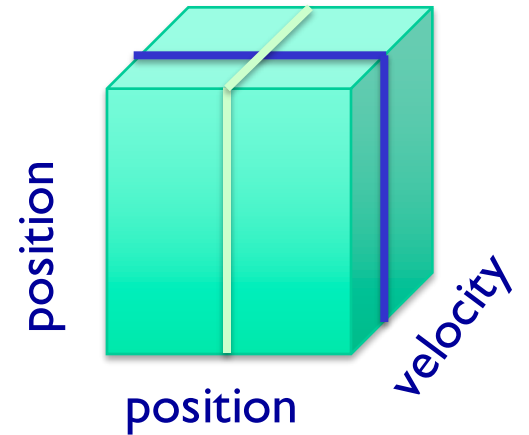
- Spectrum



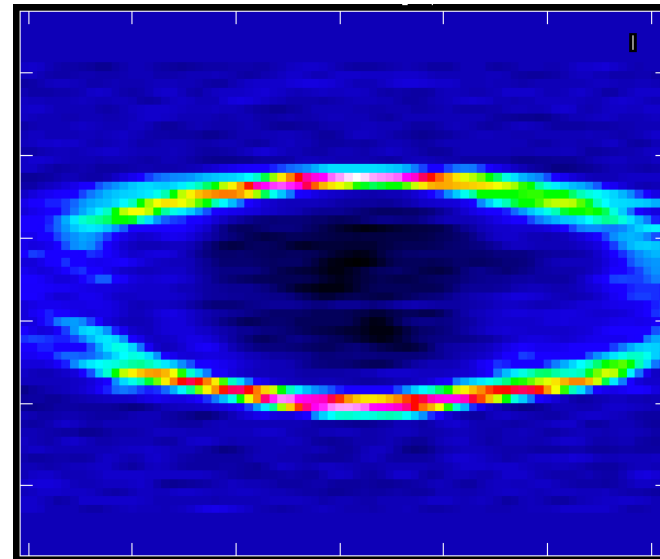
- Channel map



Fixed velocity,  
polarization, etc.



- Position-velocity map



One fixed position,  
polarization, etc.

# Imaging spectral lines: continuum subtraction

- Generally would like to subtract continuum emission
  - can use heavily averaged amp vs. frequency plot in plotms to determine
- Use `uvcontsub` to do the subtraction in uv plane.
- Channel selection is done in whatever frame your ms is in (generally topo for ALMA data, but may be lsrk)
- Be careful when specifying channel ranges for multiple
- Rest of defaults usually okay..

```
CASA <11>: inp
-----> inp()
# uvcontsub :: Continuum fitting and subtraction in the uv plane
vis          = 'ngc3256_co.ms'    # Name of input MS.  Output goes to vis + ".contsub"
field        = ''                 # Select field(s) using id(s) or name(s)
fitspw       = '0:20~53;71~120'  # Spectral window;channel selection for fitting the continuum
combine      = ''                 # Data axes to combine for the continuum estimation (none, or spw and/or scan)
solint       = 'int'              # Continuum fit timescale (int recommended!)
fitorder     = 0                  # Polynomial order for the fits
spw          = ''                 # Spectral window selection for output
want_cont    = False              # Create vis + ".cont" to hold the continuum estimate.
async       = False              # If true the taskname must be started using uvcontsub(...)
```



# Imaging spectral lines

```
mode = 'velocity' # Spectral gridding type (mfs, channel,
                  # velocity, frequency)
nchan = 100 # Number of channels (planes) in output
           # image; -1 = all
start = '300km/s' # Velocity of first channel: e.g
                  # '0.0km/s' (''=first channel in first
                  # SpW of MS)
width = '10km/s' # Channel width e.g '-1.0km/s'
                # (''=width of first channel in first
                # SpW of MS)
interpolation = 'linear' # Spectral interpolation (nearest,
                          # linear, cubic).
resmooth = False # Re-restore the cube image to a common
                 # beam when True
chaniter = False # Clean each channel to completion
                 # (True), or all channels each cycle
                 # (False)
outframe = 'LSRK' # Velocity reference frame of output
                  # image; '' =input
veltype = 'radio' # Velocity definition of output image

restfreq = '115.271201800GHz' # Rest frequency to assign to image (see help)
```

mode="velocity"

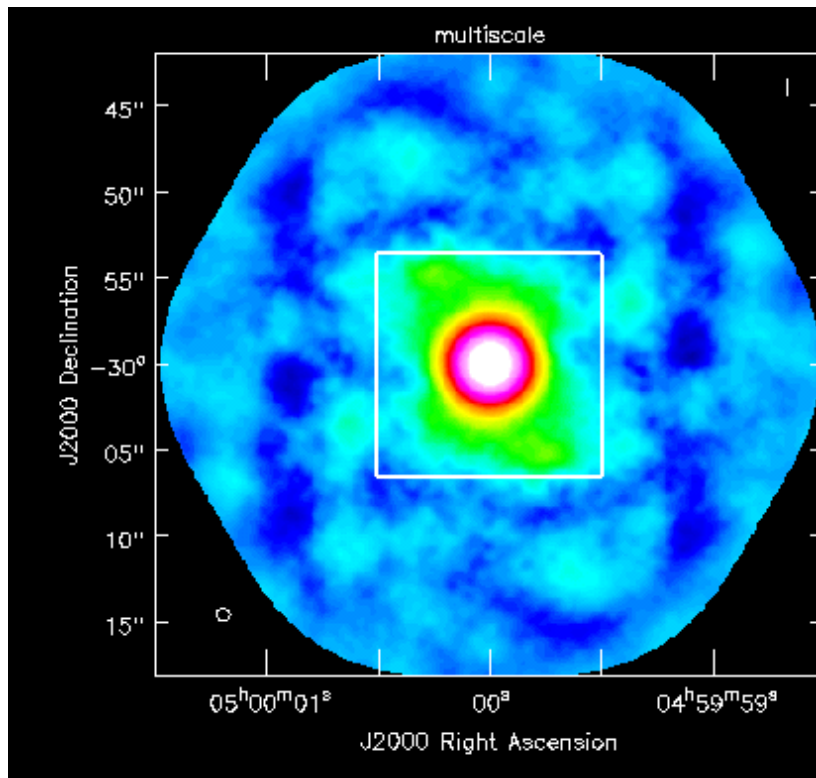
- Set the dimensions of the cube
- Set Rest frequency
- Set Velocity Frame (LSRK, BARY, ...)
- Set Doppler definition (optical/radio)



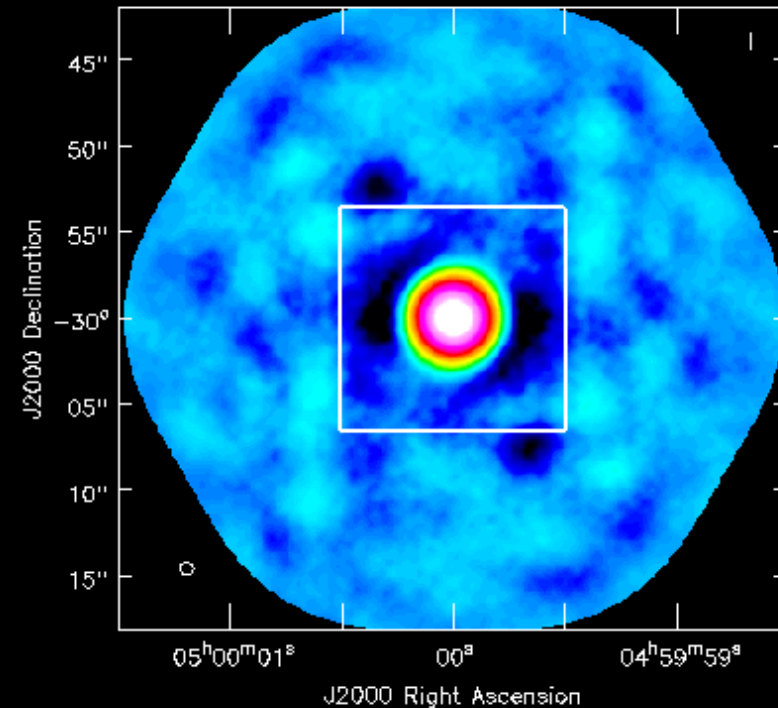
Clean will calculate the Doppler corrections for you! No need to realign beforehand (but **cvel** can do it for you if needed, e.g. when self-calibrating)

# Multi-scale CLEAN

multi-scale



“classic” scale



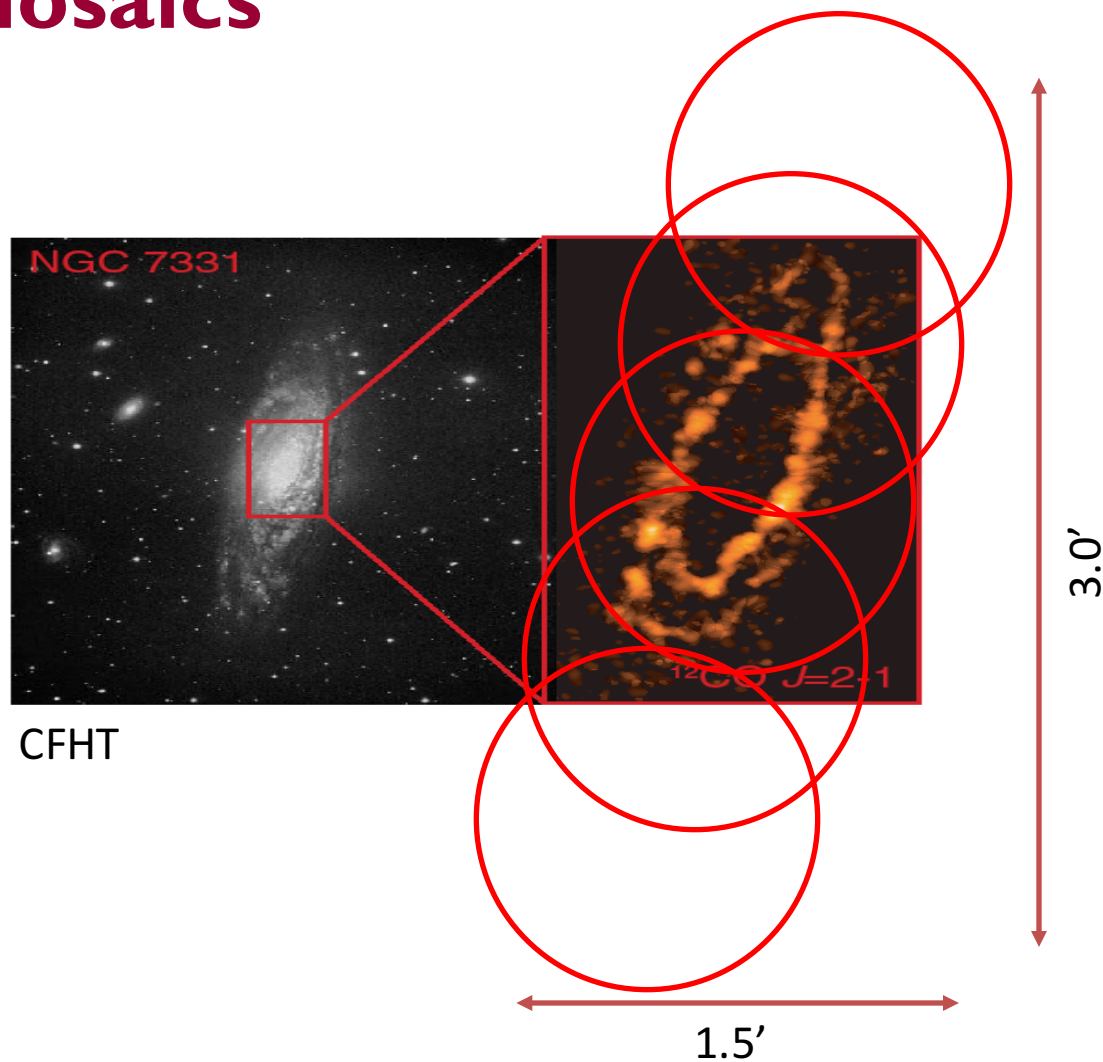
```
multiscale = [0, 5, 12, 24, 50] # Deconvolution scales (pixels); [] =  
# standard clean
```



Instead of delta functions, one can use extended clean components to better match emission scales (multiscales, typically paraboloids)

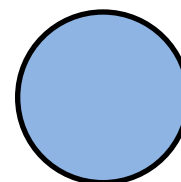
Pick delta function, half the largest emission and a few in between

# Mosaics

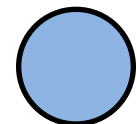


Example: SMA 1.3 mm  
observations: 5  
pointings

- Primary beam  $\sim 1'$
- Resolution  $\sim 3''$



ALMA 1.3mm PB



ALMA 0.85mm PB



Petitpas et al.

# Imaging mosaics

```
imagermode = 'mosaic' # Options: 'csclean' or 'mosaic', '', uses psfmode
mosweight = False # Individually weight the fields of the mosaic
ftmachine = 'ft' # Gridding method for the image
scaletype = 'SAULT' # Controls scaling of pixels in the image plane. default='SAULT'; example:
# scaletype='PBCOR' Options: 'PBCOR','SAULT'
cyclefactor = 1.5 # Controls how often major cycles are done. (e.g. 5 for frequently)
cyclespeedup = -1 # Cycle threshold doubles in this number of iterations
flatnoise = True # Controls whether searching for clean components is done in a constant noise
# residual image (True) or in an optimal signal-to-noise residual image
# (False)
```

ftmachine = “mosaic” : add in uv plane and invert together,  
Use *csclean* for deconvolution. Generally what you want  
unless very LARGE final image.

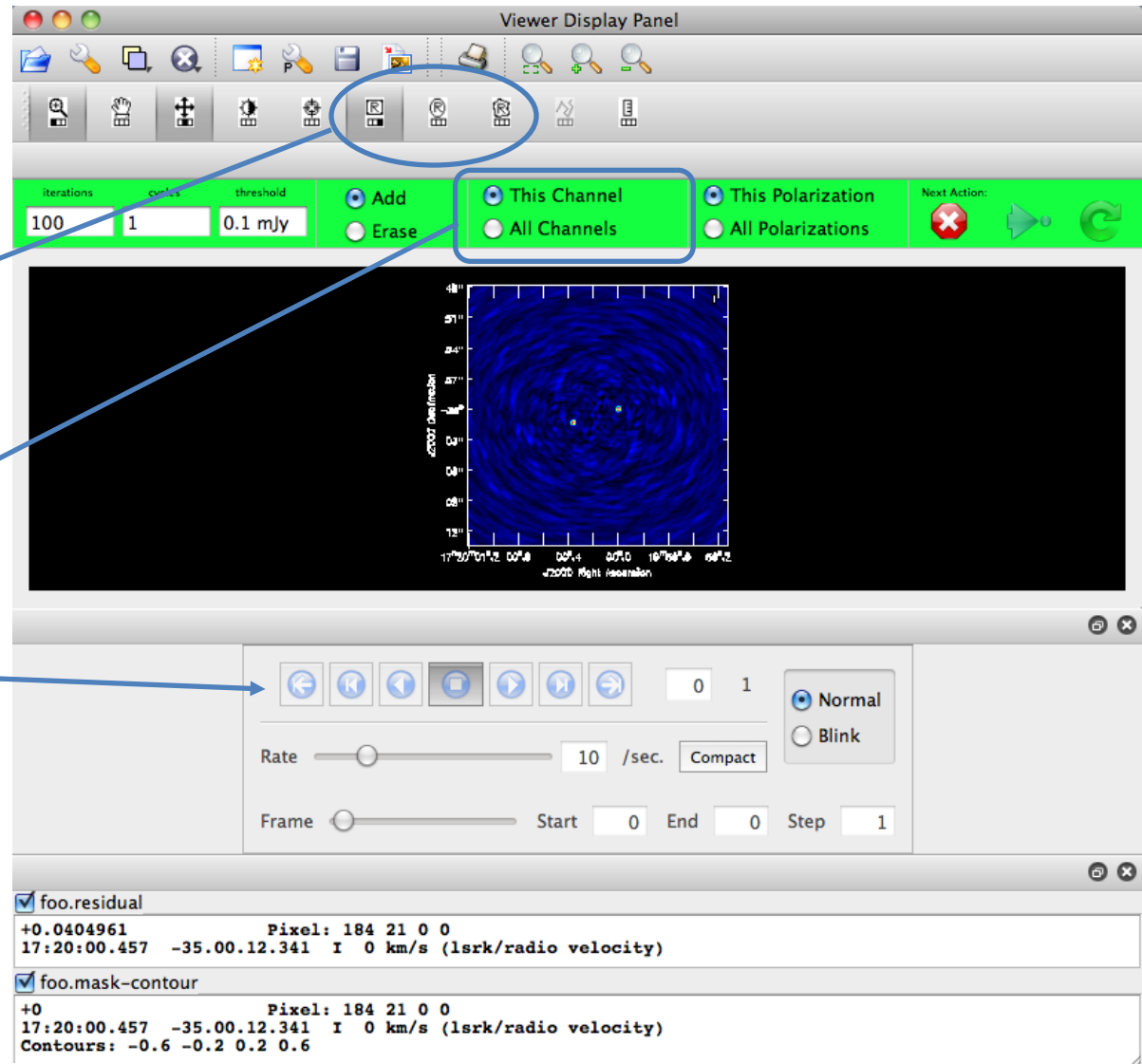
ftmachine = “ft” : shift and add in image plane

There’s a tool (“ia.linear\_mosaic”) to linear mosaic after  
cleaning each pointing and to stitch all pointings together  
entirely in the image domain



# Interactive CLEAN

- residual image in viewer
- define a mask with defining a mouse button on shape type
- define the same mask for all channels
- or iterate through the channels with the tape deck and define separate masks

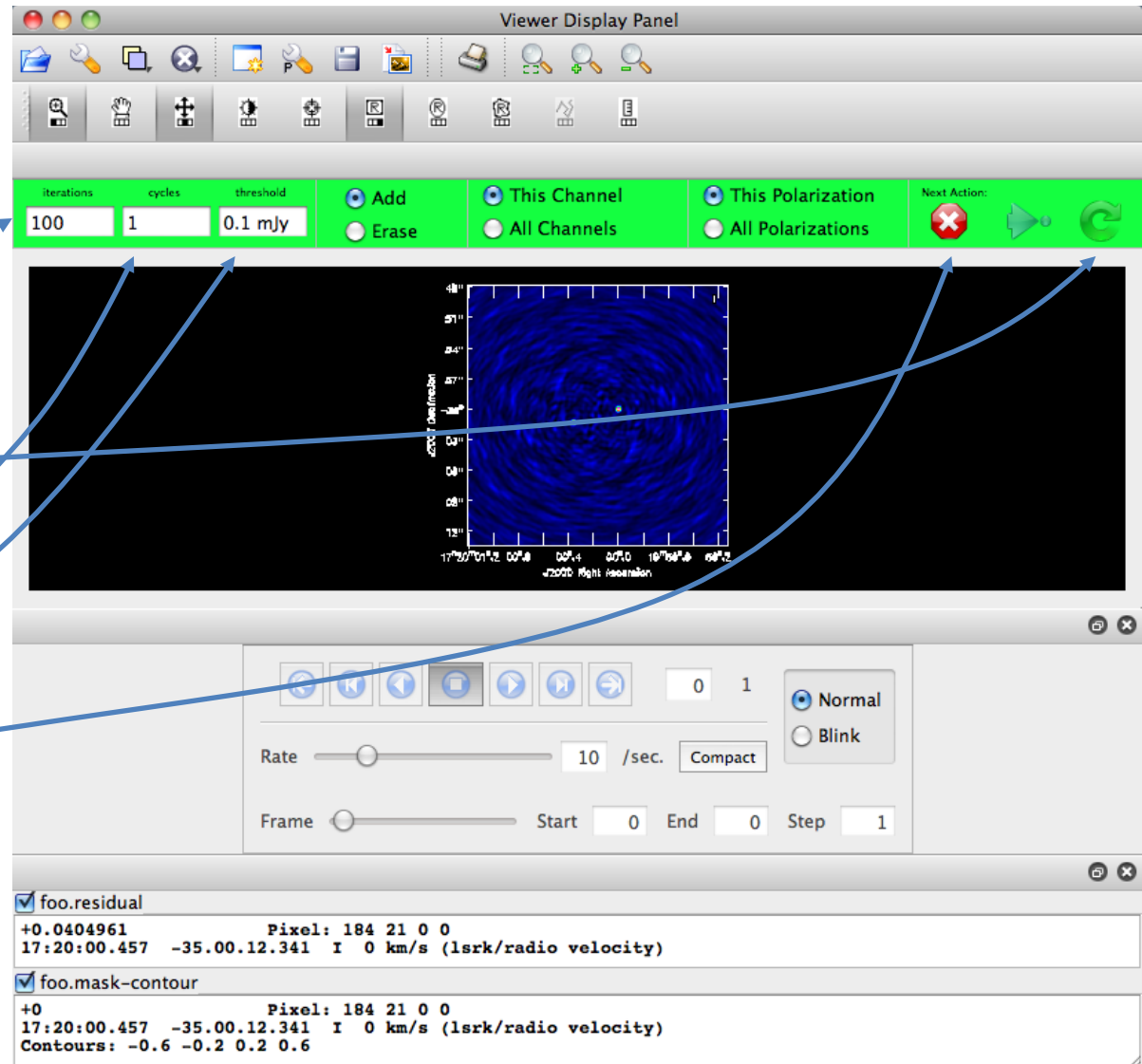


Talk to me during the hands-on portion to see how you can re-arrange this window!



# Interactive CLEAN

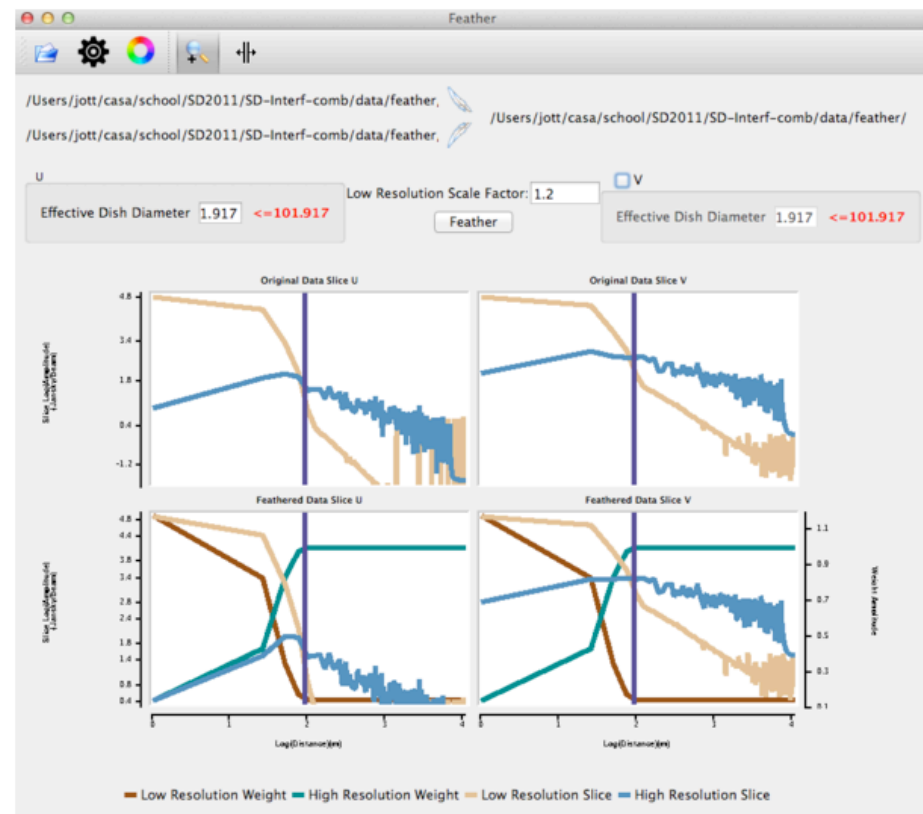
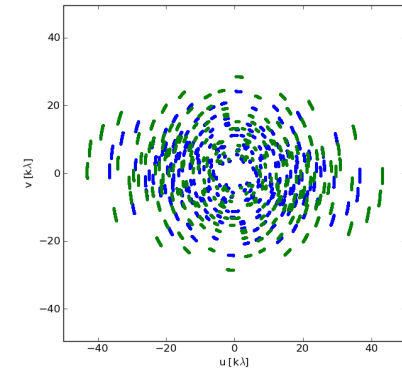
- perform N iterations
- and return – every time the residual is displayed is a major cycle
- continue until #cycles or threshold reached, or user stop



# Combining with single-dish or other interferometric maps

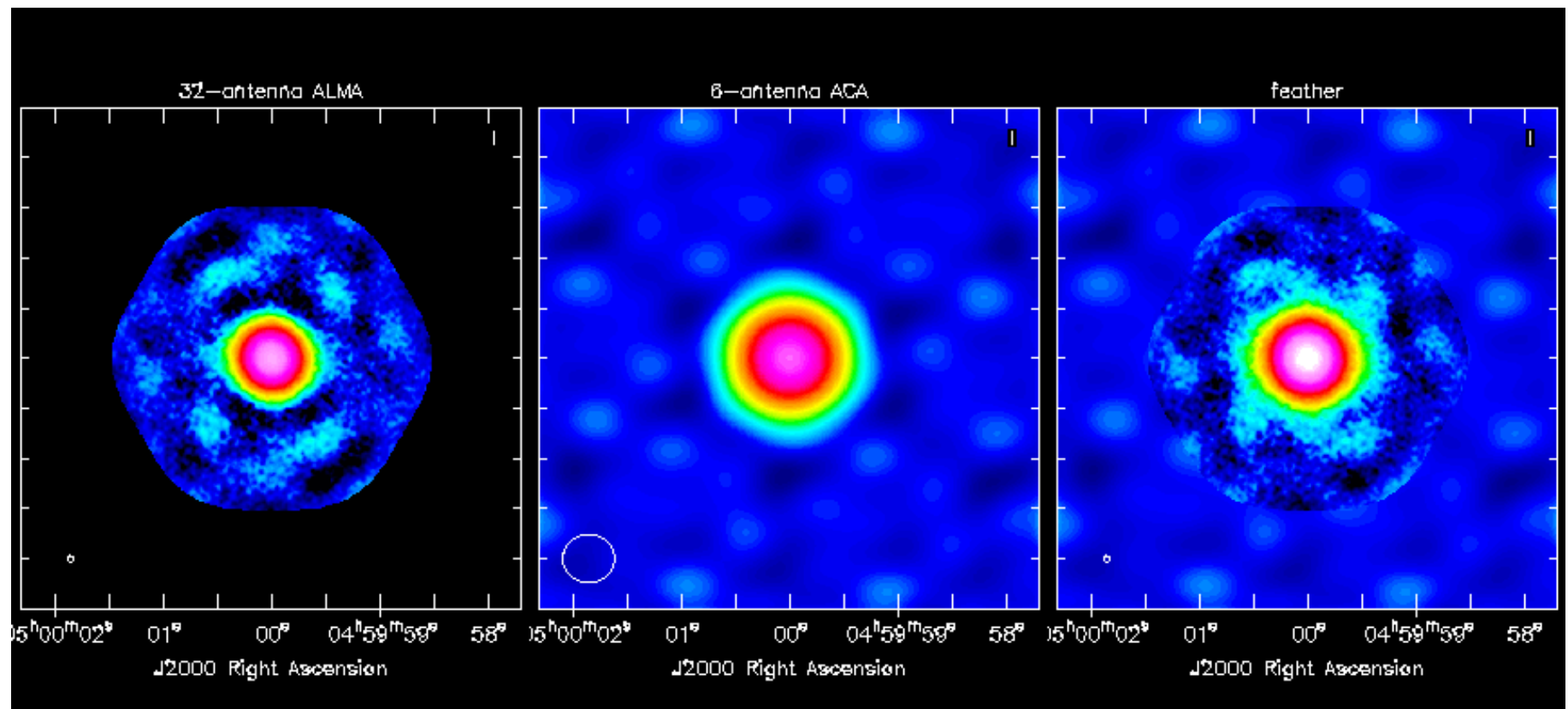
- If you have only images:
  - feather (or “casafeather”)
- If you have an image and an MS:
  - use CLEAN with the image as “modelimage” [not well tested]
  - and/or feather
- If you have multiple MS plus an image:
  - Same as above, input to clean will be all the MS

The best way to combine ALMA single dish and interferometer data is an active area of research. See the M100 imaging tutorial for the gory details.



# Combining with other data: feather

```
# feather :: Combine two images using their Fourier transforms
imagenname      = ''          # Name of output feathered image
highres         = ''          # Name of high resolution (interferometer) image
lowres          = ''          # Name of low resolution (single dish) image
async           = False       # If true the taskname must be started using feather(...)
```



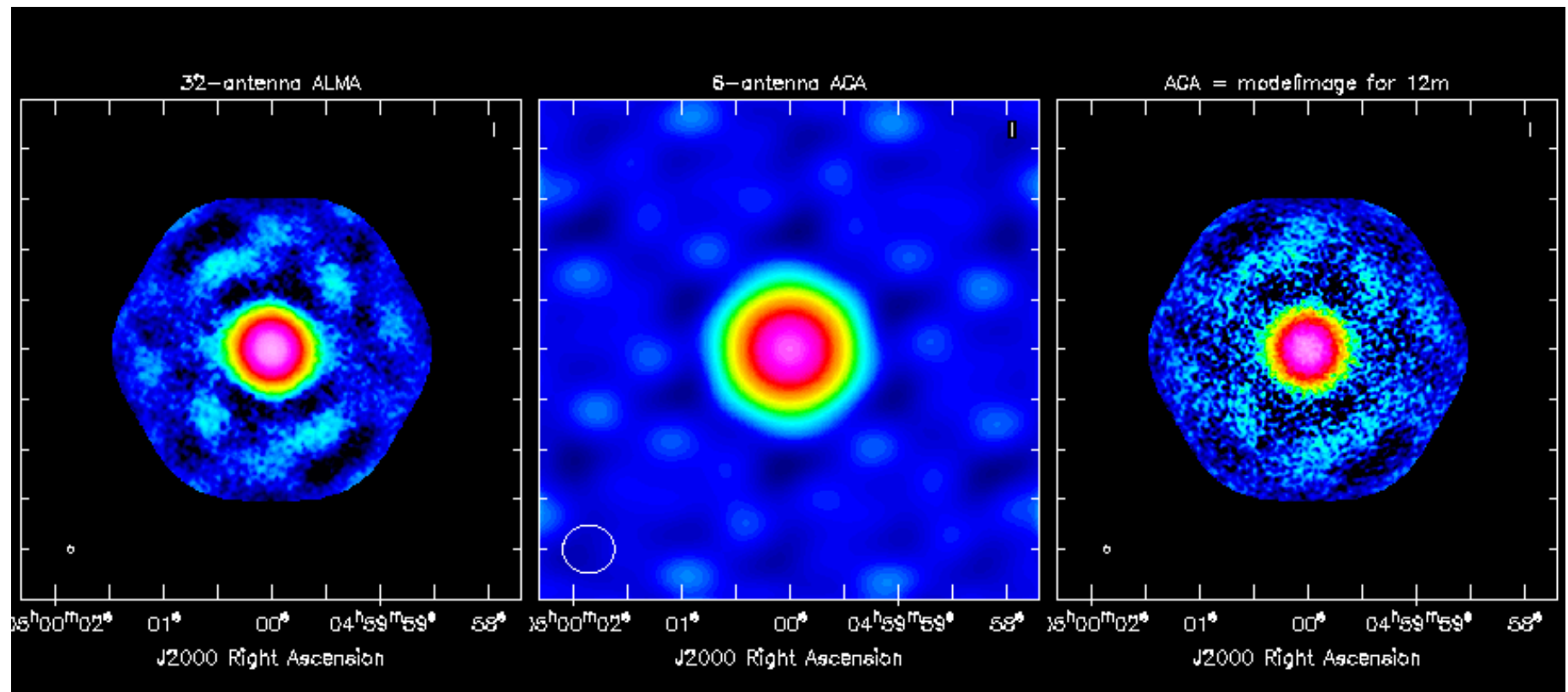
We also have a graphical tool: CASAfeather

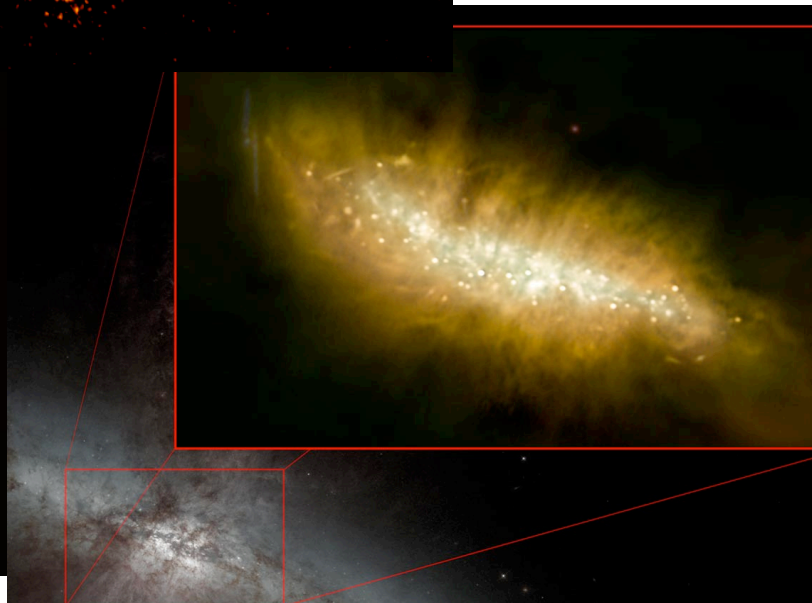
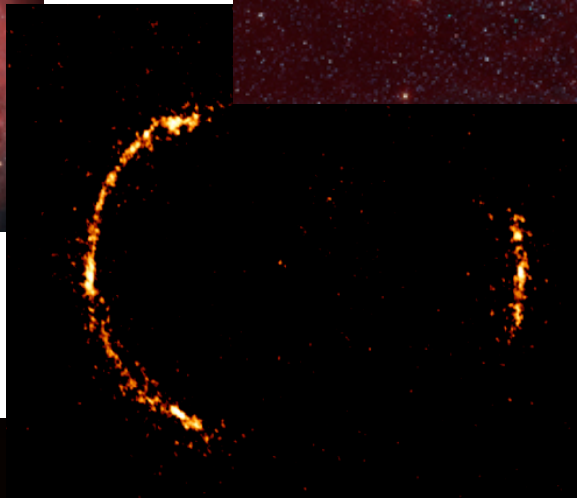
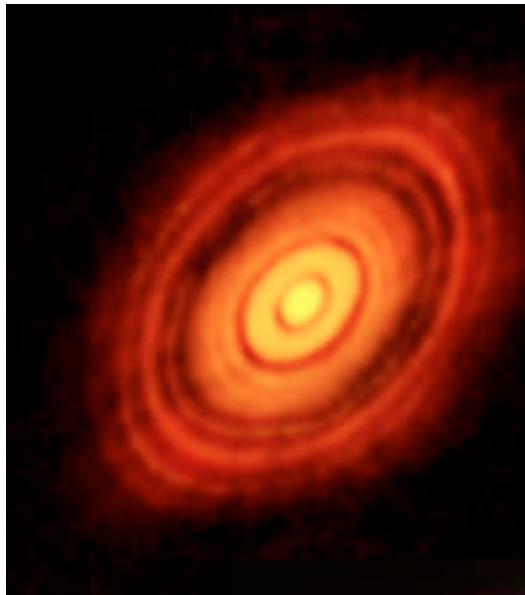
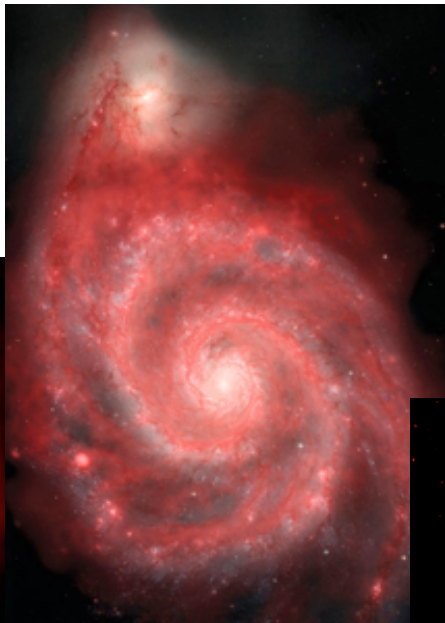
## Combining with other data: modelimage

```

----> inp(clean)
# clean :: Invert and deconvolve images with selected algorithm
# clean :: Invert and deconvolve images with selected algorithm
modelimage = '' # Name of model image(s) to initialize cleaning

```







# Looking ahead ...

## ALMAguides

---

### How to use these CASA Tutorials

#### Imaging Tutorials for CASA beginners

If you are new to CASA, start with the following tutorials. ALMA data are delivered with standard calibrations applied and they are ready for imaging. These guides cover the basic steps required for imaging and self-calibration.

- [A first look at imaging in CASA](#) This guide gives a first look at imaging and image analysis in CASA.
- [A first look at self-calibration in CASA](#) This guide demonstrates continuum self-cal.
- [A first look at spectral line imaging in CASA](#) This guide shows imaging of a spectral line.
- [A first look at image analysis in CASA](#) This guide demonstrates moment creation and basic image analysis.

#### Guides for reducing ALMA Science Verification data

The links below lead to overview pages for each science verification observation. The guides themselves are linked from the overview pages. These guides are a useful tools for those who would like to learn the process of calibration and imaging in detail.

*The following ALMA science verification guides have been validated for CASA version 4.3. They should also work for CASA version 4.4, and they will be validated for version 4.4 soon.*

- [TWHydraBand7](#): The protoplanetary disk source TW Hya at Band 7 (0.87 mm)
- [NGC3256Band3](#): The galaxy merger NGC 3256 at Band 3 (3 mm)
- [AntennaeBand7](#): Mosaic of the galaxy merger NGC 4038/4039 (Antennae) at Band 7 (0.87 mm)
- [IRAS16293Band9](#): Mosaic of the protostellar cluster IRAS16293-2422 at Band 9 (0.45 mm)
- [File:BR1202 SV Band7 Calibration notes.pdf](#): Supplemental notes on the calibration of Science Verification target BR1202-0725 in CASA 3.3
- [ALMA2014\\_LBC\\_SVDATA](#): Imaging scripts and details for the 2014 ALMA Long Baseline Campaign science verification data for Juno, Mira, HL Tau, and SDP.81.
- [M100\\_Band3](#): Demonstration of combining 12m-array, 7m-array, and Total Power data for M100 using CASA 4.3.1
- [3C286\\_Polarization](#): Demonstration of the reduction of ALMA continuum polarization toward the quasar 3C286

### A Guide to CASA Data Weights and How to Ensure They are Correct for Data Combination

#### A Guide to Processing ALMA Data for Cycle 0

This page takes you through the steps of processing Cycle 0 data from the ALMA data archive. The guide describes some helpful hints for downloading the data, and describes the process all the way through imaging and self-calibration, and image analysis.

You can also get a look at example data calibration scripts used for Cycle 0 data at the following links. These were written for CASA version 3.4.

- TDM (128 channels/spw) [File:TDM.example.ms.scriptForCalibration.py](#)
- FDM (3840 channels/spw) [File:FDM.example.ms.scriptForCalibration.py](#)
- If you need to update 3.4 scripts to 4.2, see more information [here](#)

#### A Tutorial for Simulating ALMA Data.

Start here to learn about simulations. The CASA 4.3 simulation examples in the above tutorial should also work for version 4.4, and they will be validated for version 4.4 soon. Jump directly to the simulations examples with the following links.

- [Simulation Examples in CASA 4.3](#)
- Examples for older versions of CASA: [4.2](#) [4.1](#) [4.0](#) [3.4](#) [3.3](#)

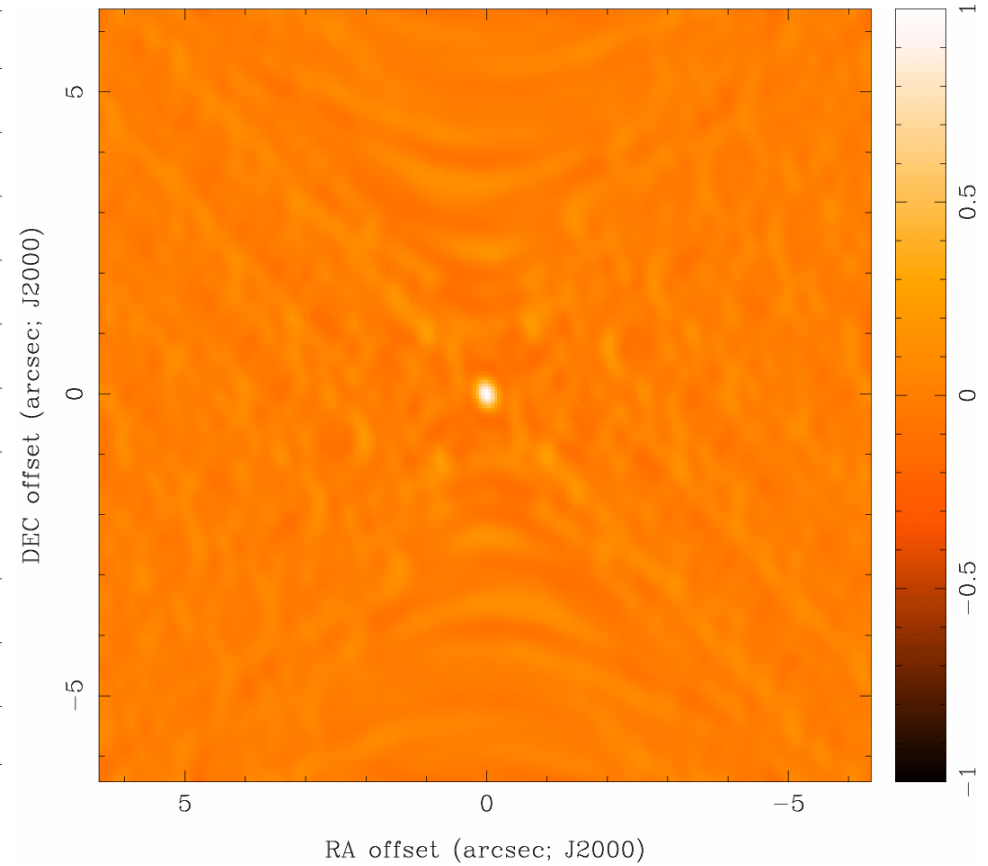
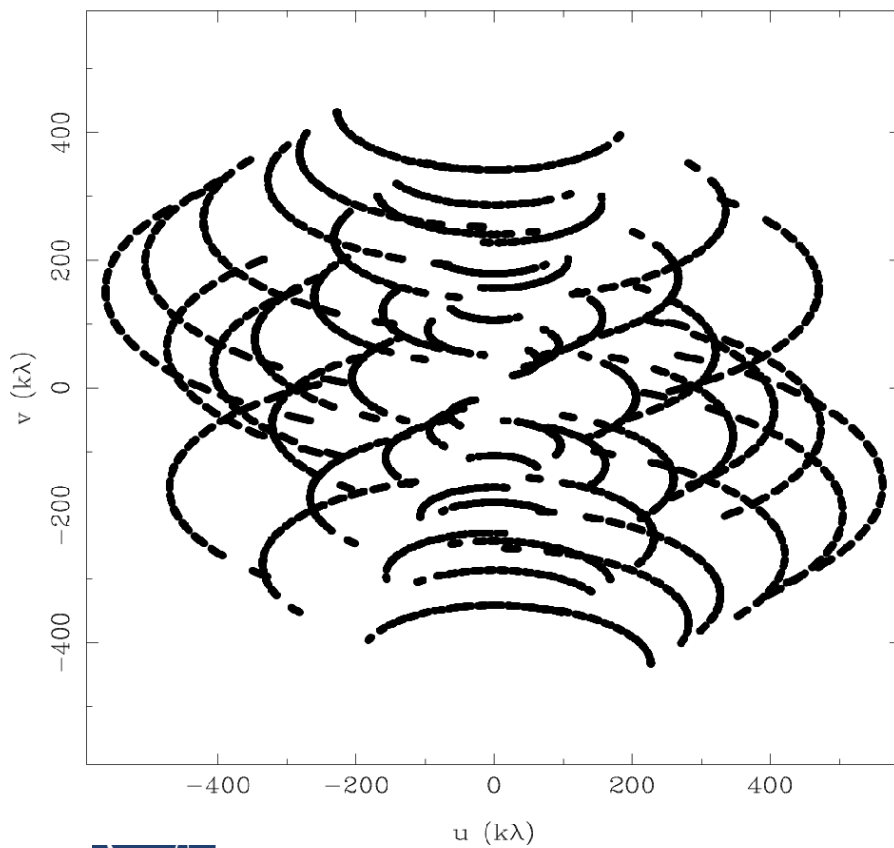




# Dirty Beam Shape and N Antennas

Earth Rotation!

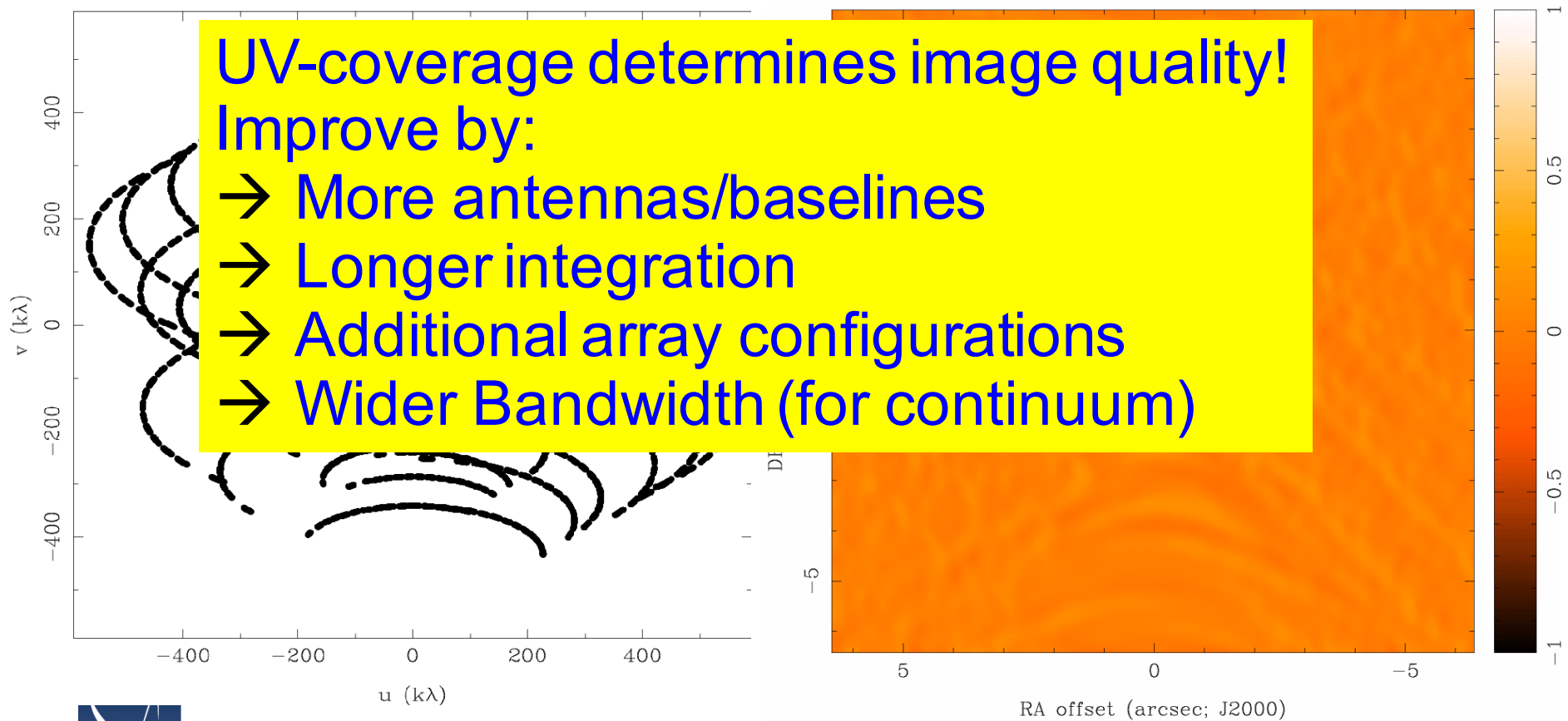
8 Antennas x 480 Samples



# Dirty Beam Shape and N Antennas

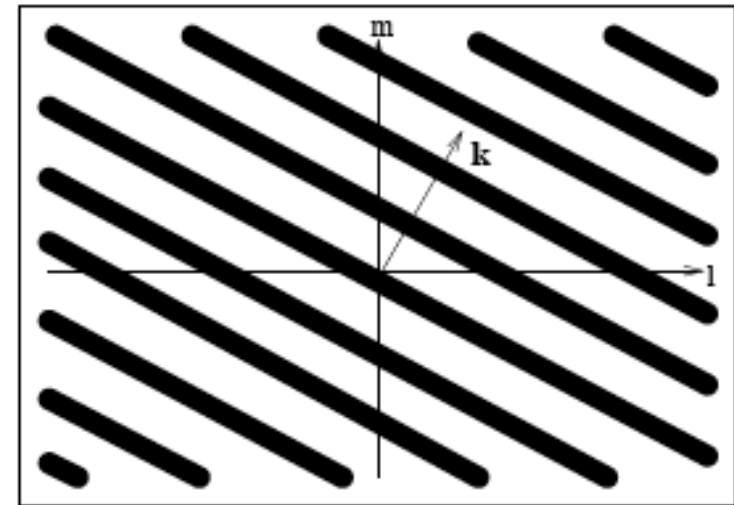
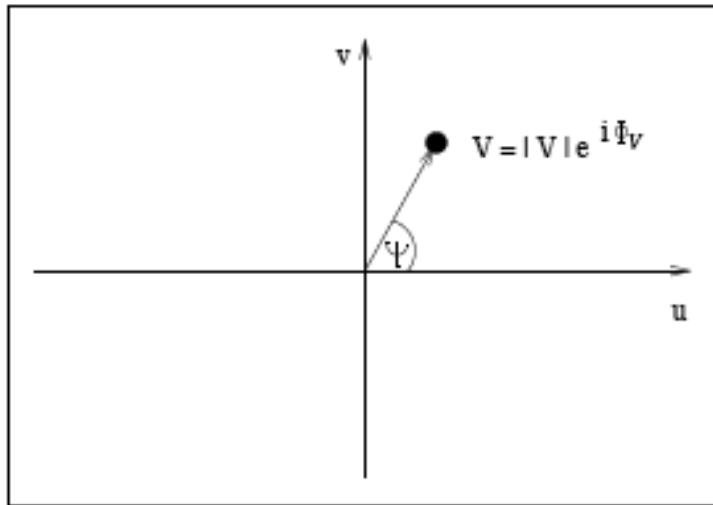
8 Antennas x 480 Samples

Earth Rotation!



# Spatial Frequency

uv-domain  $\longleftrightarrow$  FT  $\longrightarrow$  Image domain



(geometric baseline orientation) Angle  $\Psi$ :  
 (geometric baseline length) Vector length (uv-distance):  
 (measured) Amplitude  $V$ :  
 (measured) Phase  $\Phi$ :

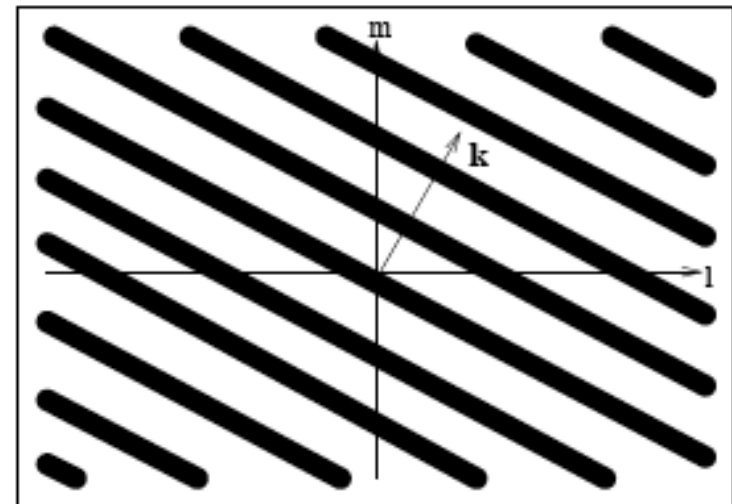
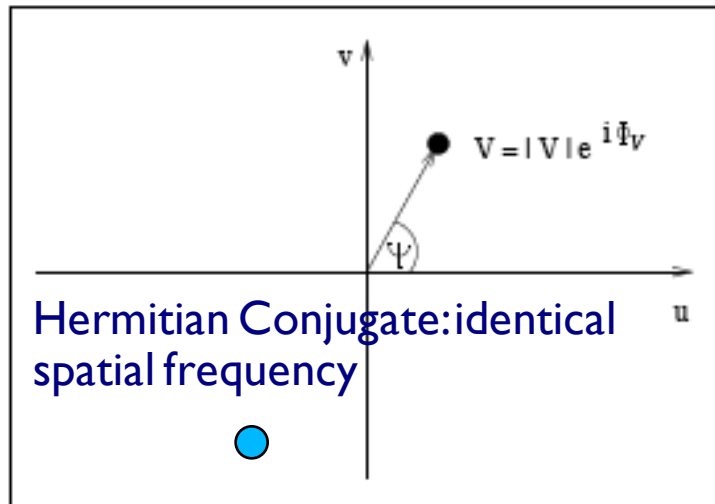
Direction of  $k$   
 Spatial Frequency  
 Amplitude  
 Pattern Offset from Origin



The image is the sum of a large number of spatial frequencies

# Spatial Frequency

uv-domain  $\longleftrightarrow$  FT  $\longleftrightarrow$  Image domain



(geometric baseline orientation) Angle  $\Psi$ :  
 (geometric baseline length) Vector length (uv-distance):  
 (measured) Amplitude  $V$ :  
 (measured) Phase  $\Phi$ :

Direction of  $k$   
 Spatial Frequency  
 Amplitude  
 Pattern Offset from Origin



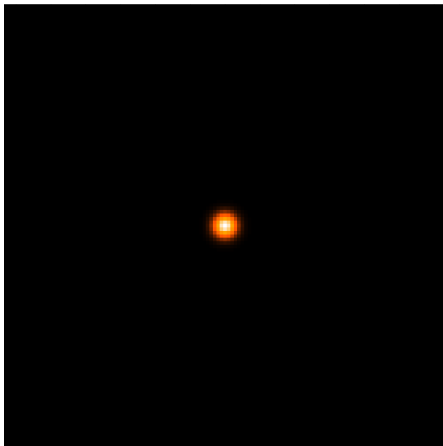
The image is the sum of a large number of spatial frequencies



# Amplitude and Phase

- complex numbers: (real, imaginary) or (amplitude, phase)
  - amplitude tells “how much” of a certain frequency component
  - phase tells “where” this component is located

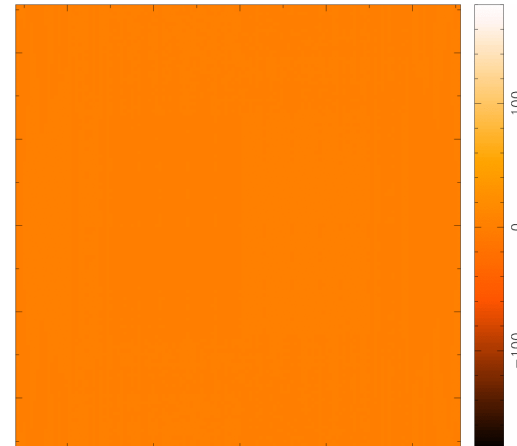
$T(x,y)$



$\text{Amp}\{V(u,v)\}$



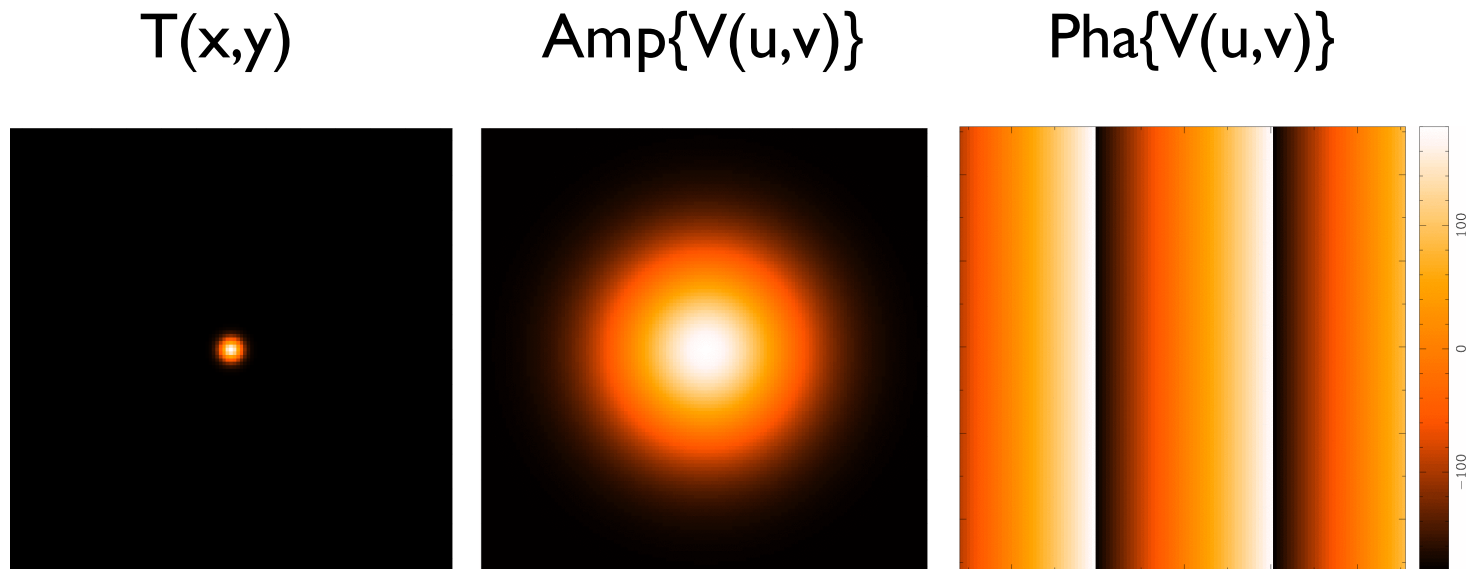
$\text{Pha}\{V(u,v)\}$



center

# Amplitude and Phase

- complex numbers: (real, imaginary) or (amplitude, phase)
  - amplitude tells “how much” of a certain frequency component
  - phase tells “where” this component is located

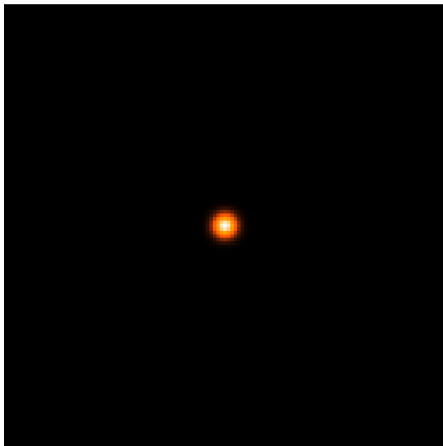


Shifted to side

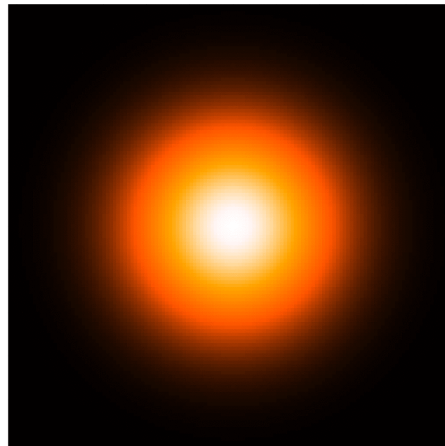
# Amplitude and Phase

- complex numbers: (real, imaginary) or (amplitude, phase)
  - amplitude tells “how much” of a certain frequency component
  - phase tells “where” this component is located

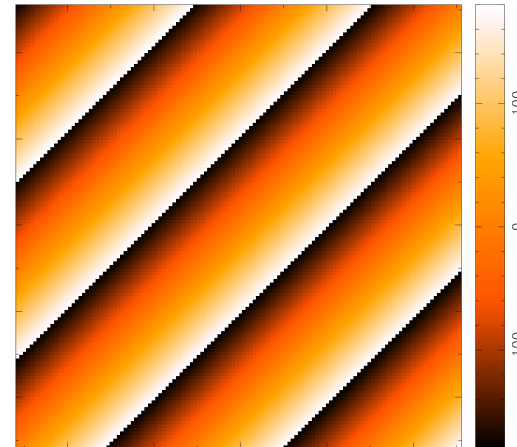
$T(x,y)$



$\text{Amp}\{V(u,v)\}$



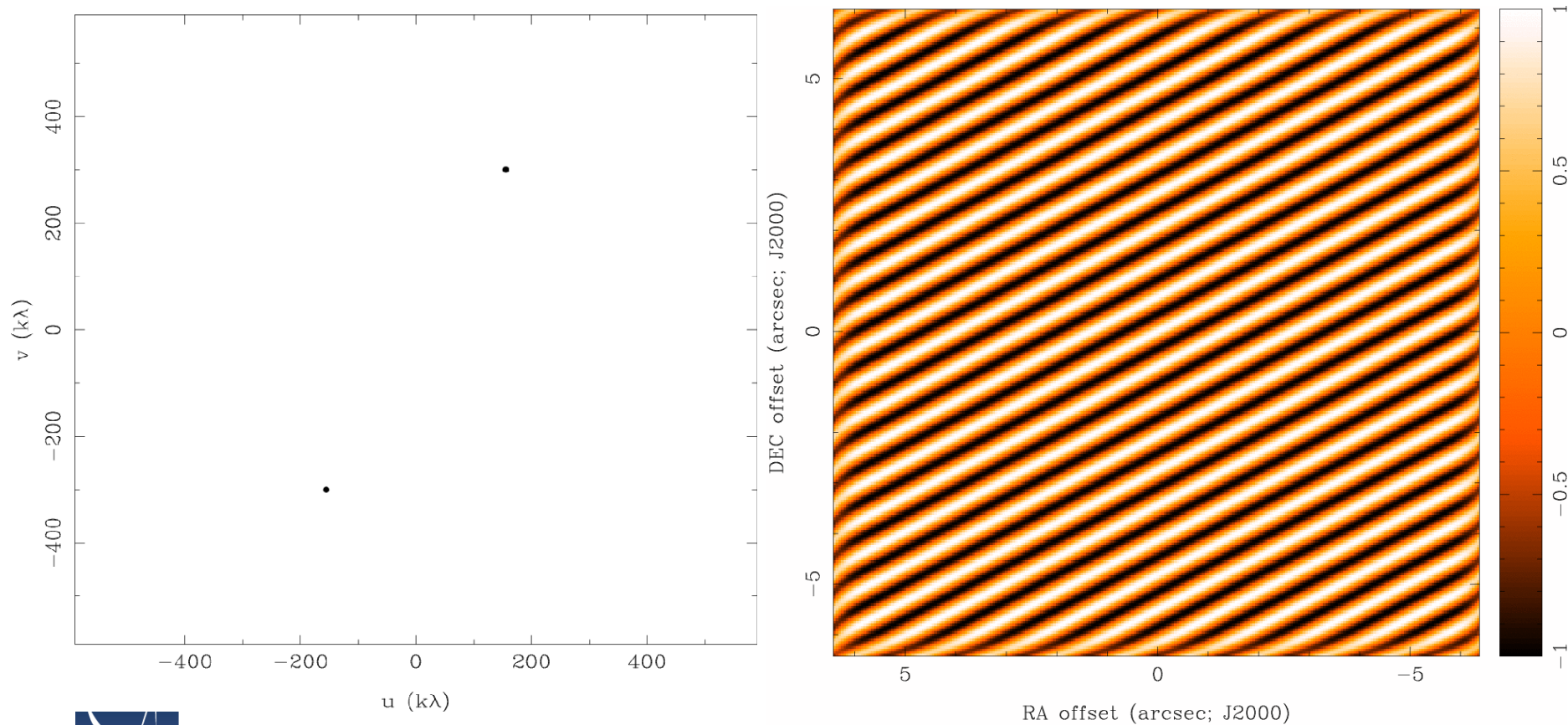
$\text{Pha}\{V(u,v)\}$



Shifted diagonally

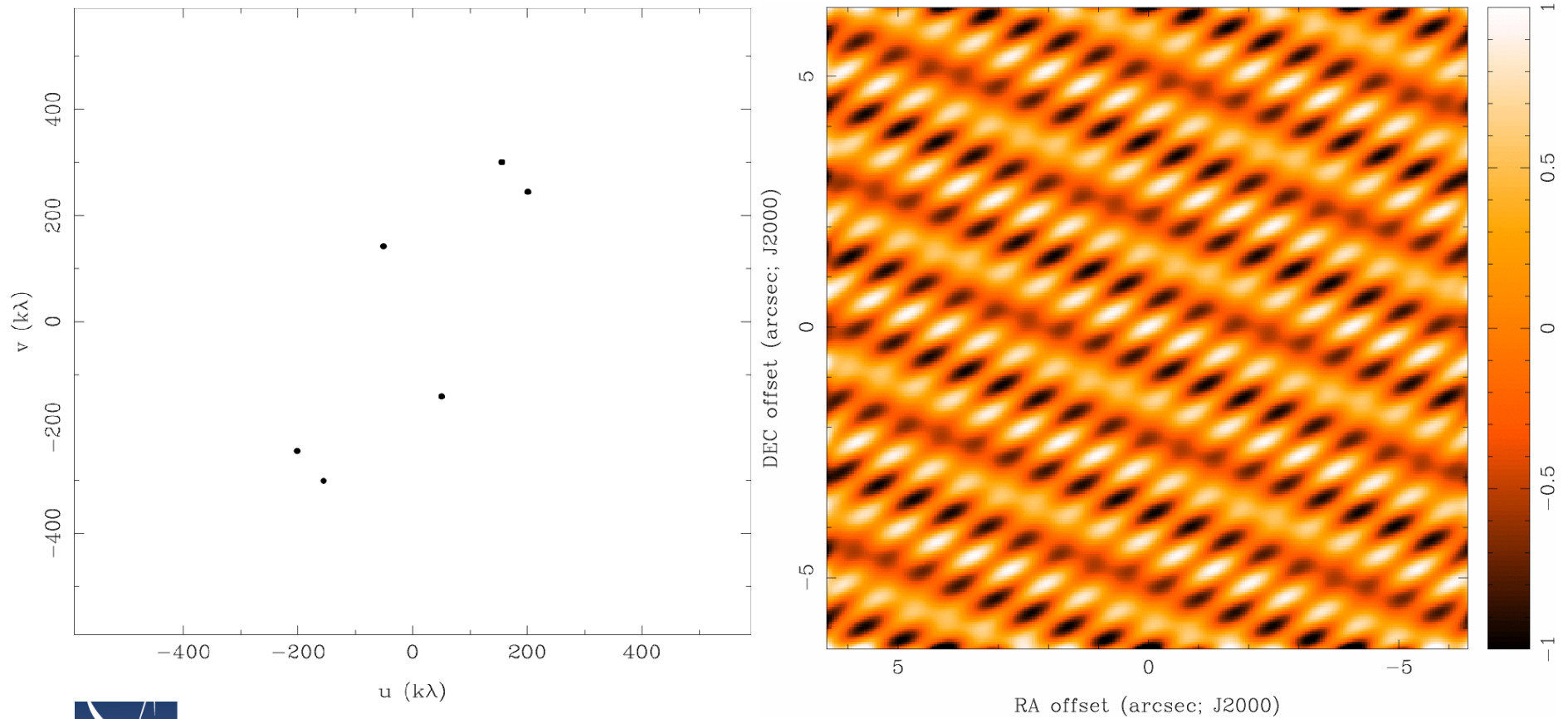
# Dirty Beam Shape and N Antennas

## 2 Antennas (1 baseline)



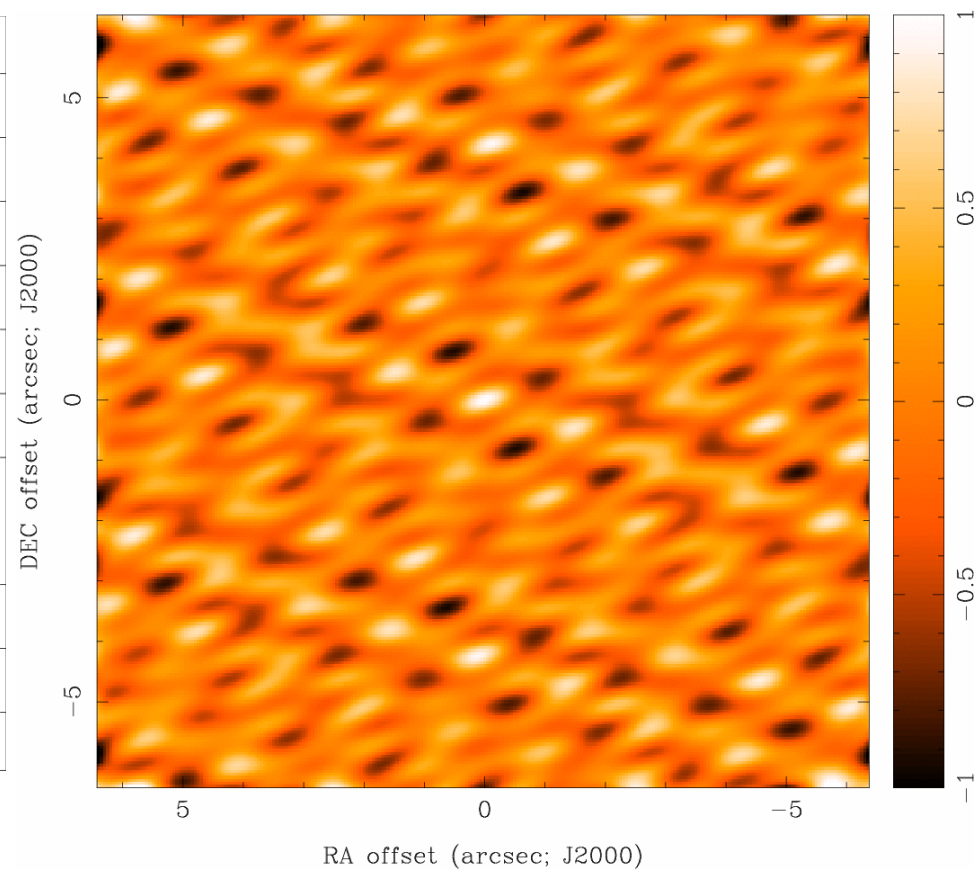
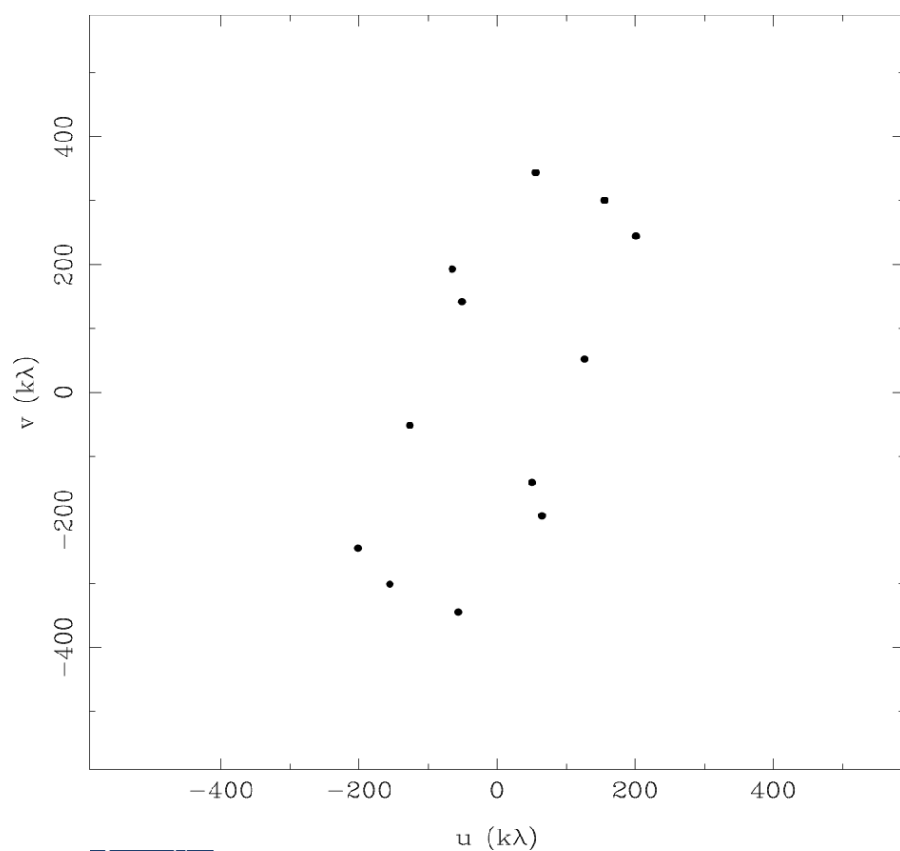
# Dirty Beam Shape and N Antennas

3 Antennas (3 baselines)



# Dirty Beam Shape and N Antennas

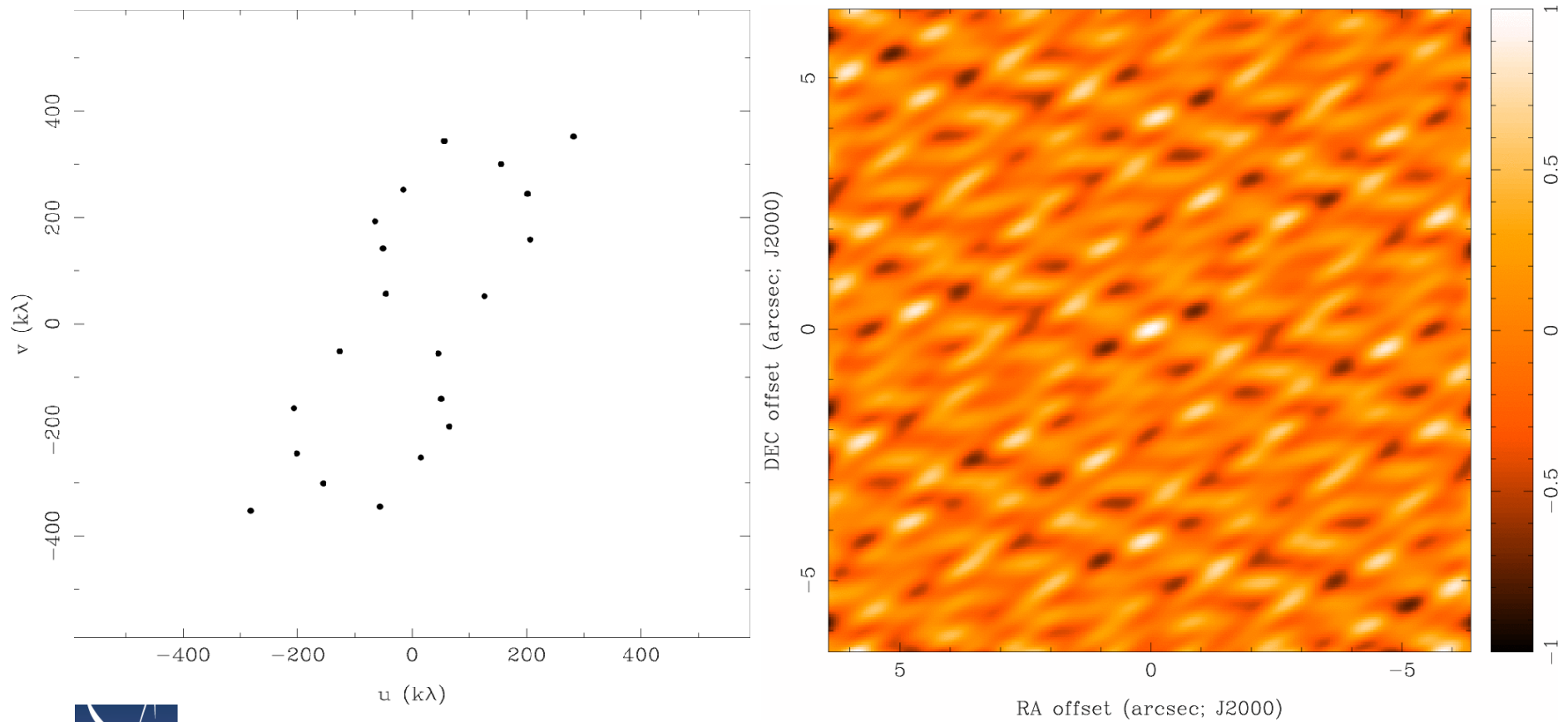
4 Antennas (6 baselines)





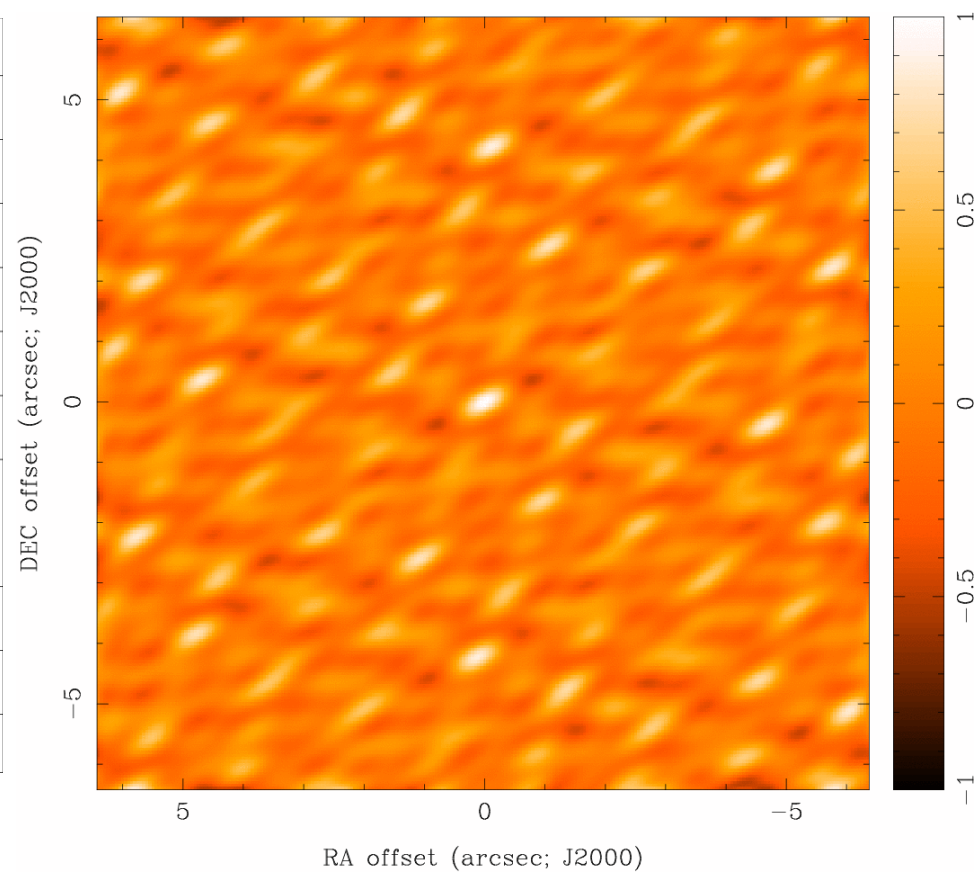
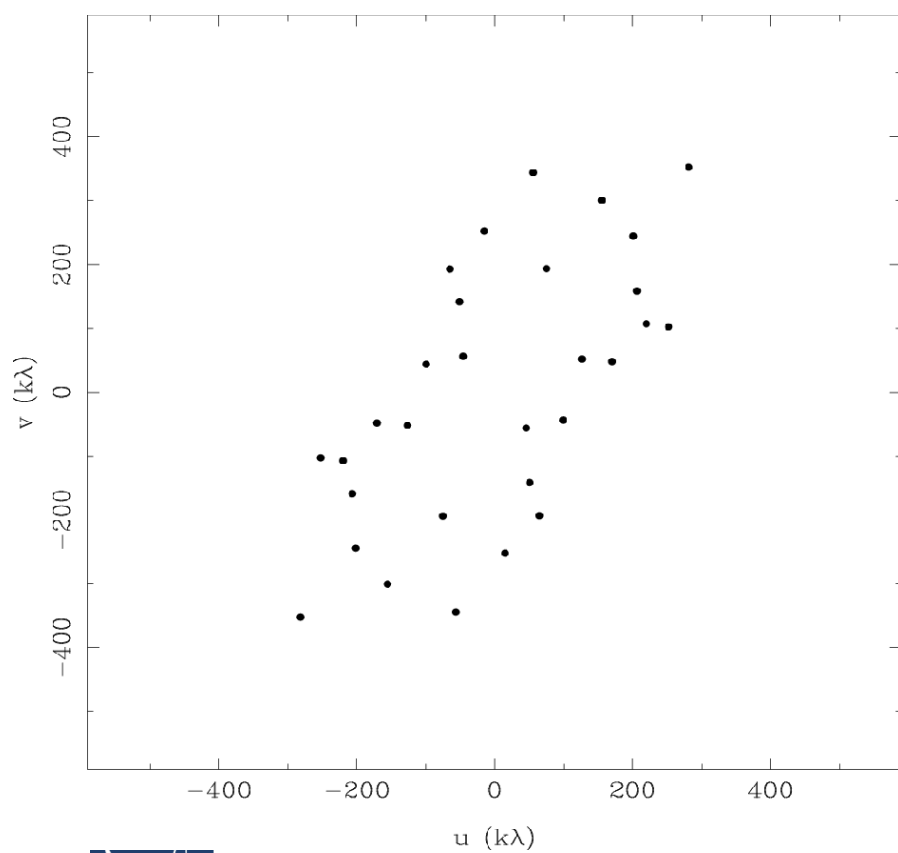
# Dirty Beam Shape and N Antennas

5 Antennas (10 baselines)



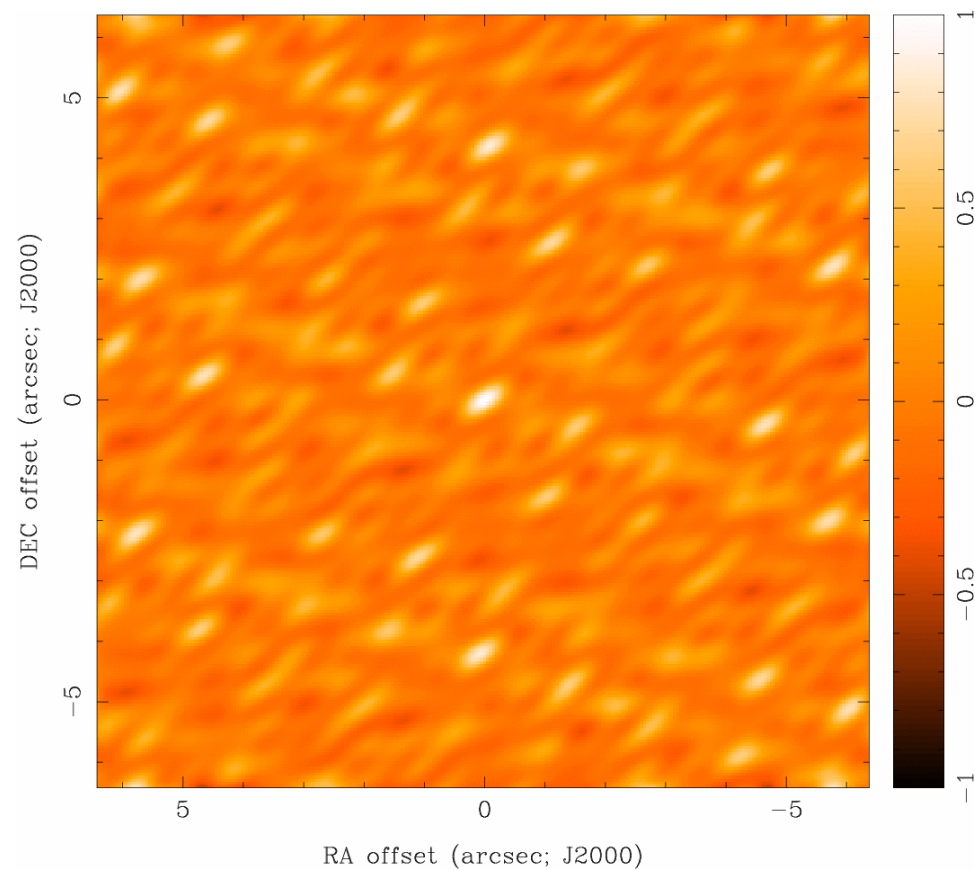
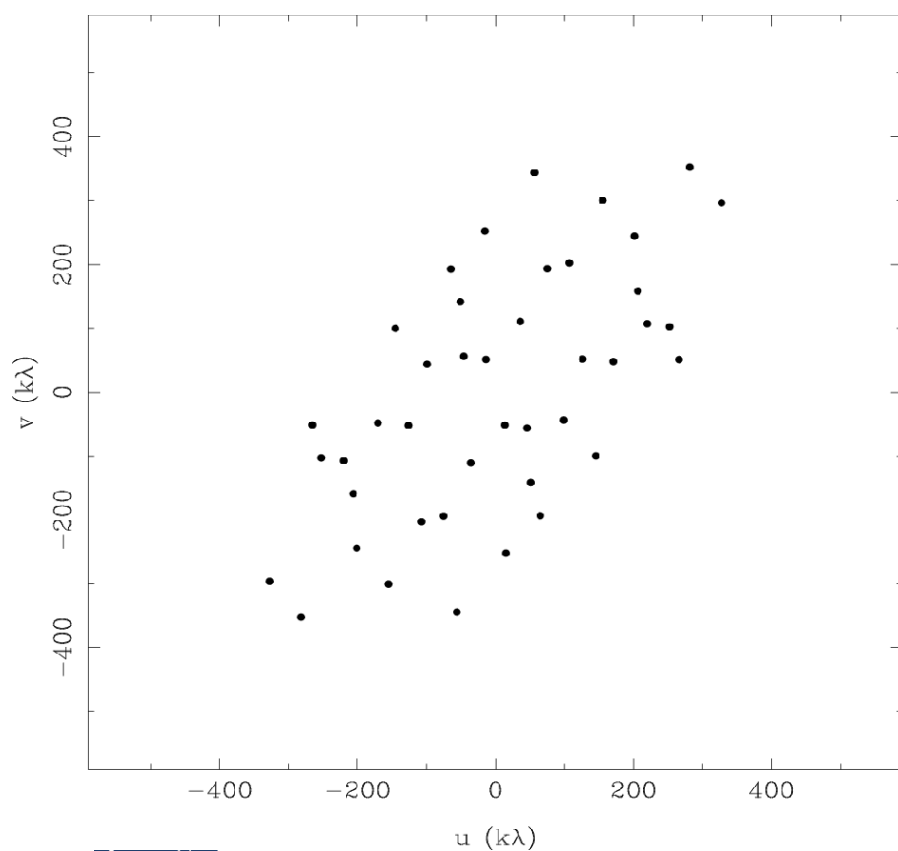
# Dirty Beam Shape and N Antennas

6 Antennas (15 baselines)



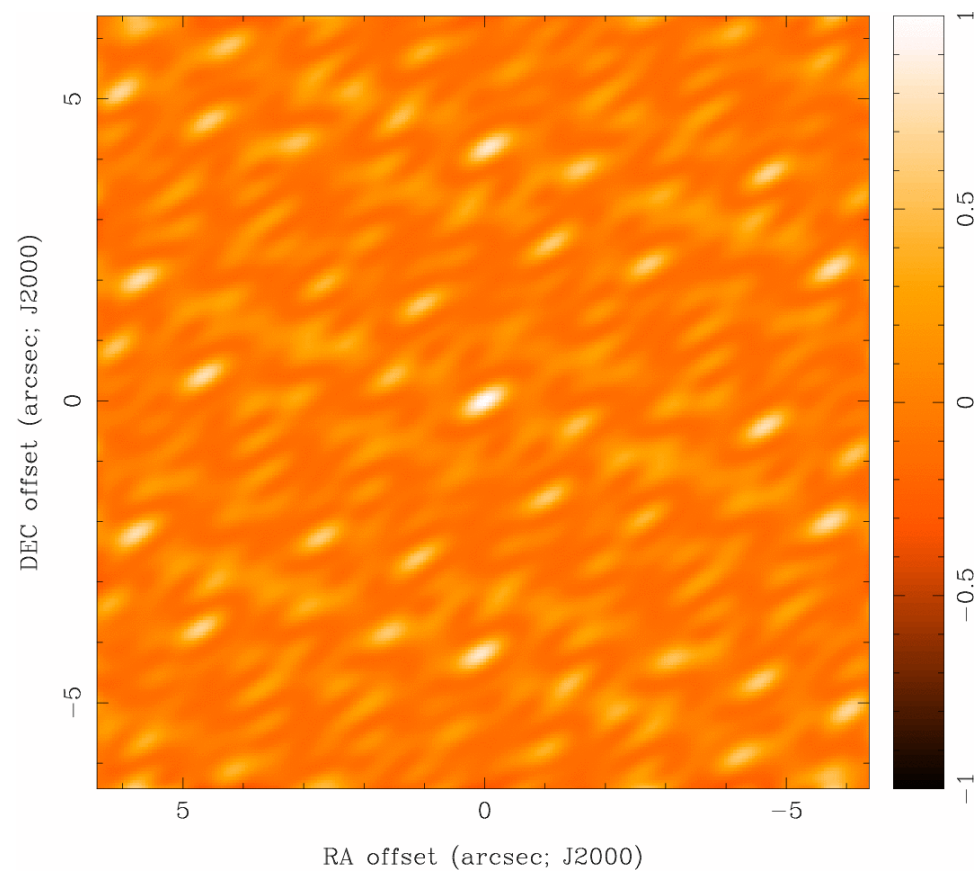
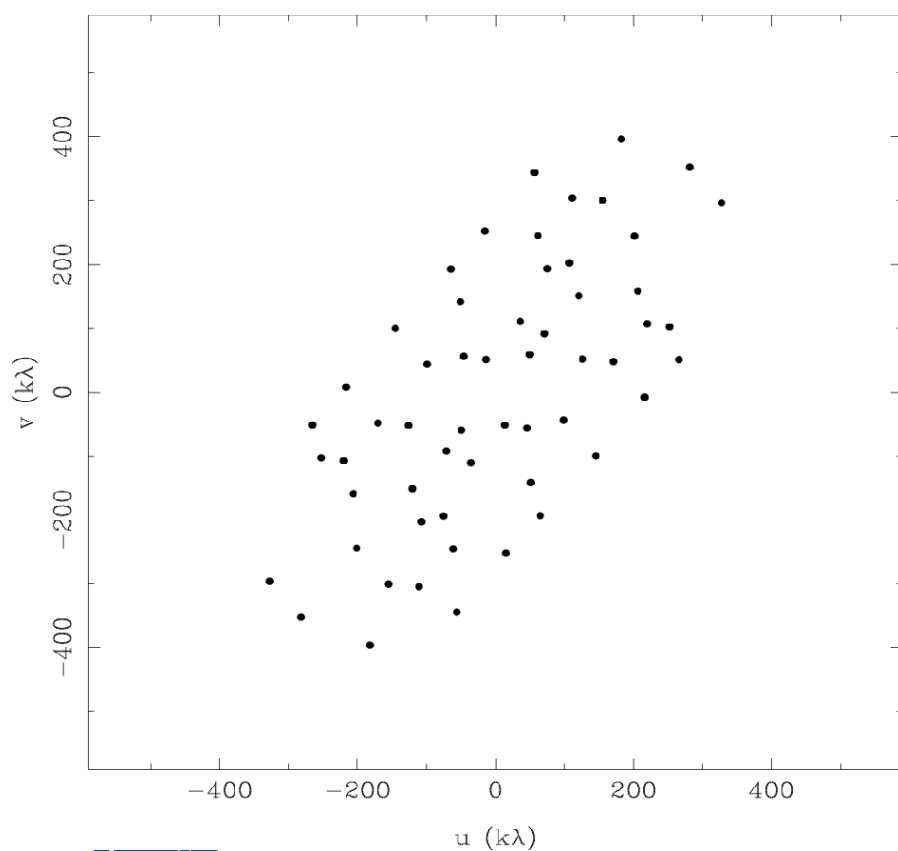
# Dirty Beam Shape and N Antennas

7 Antennas (21 baselines)



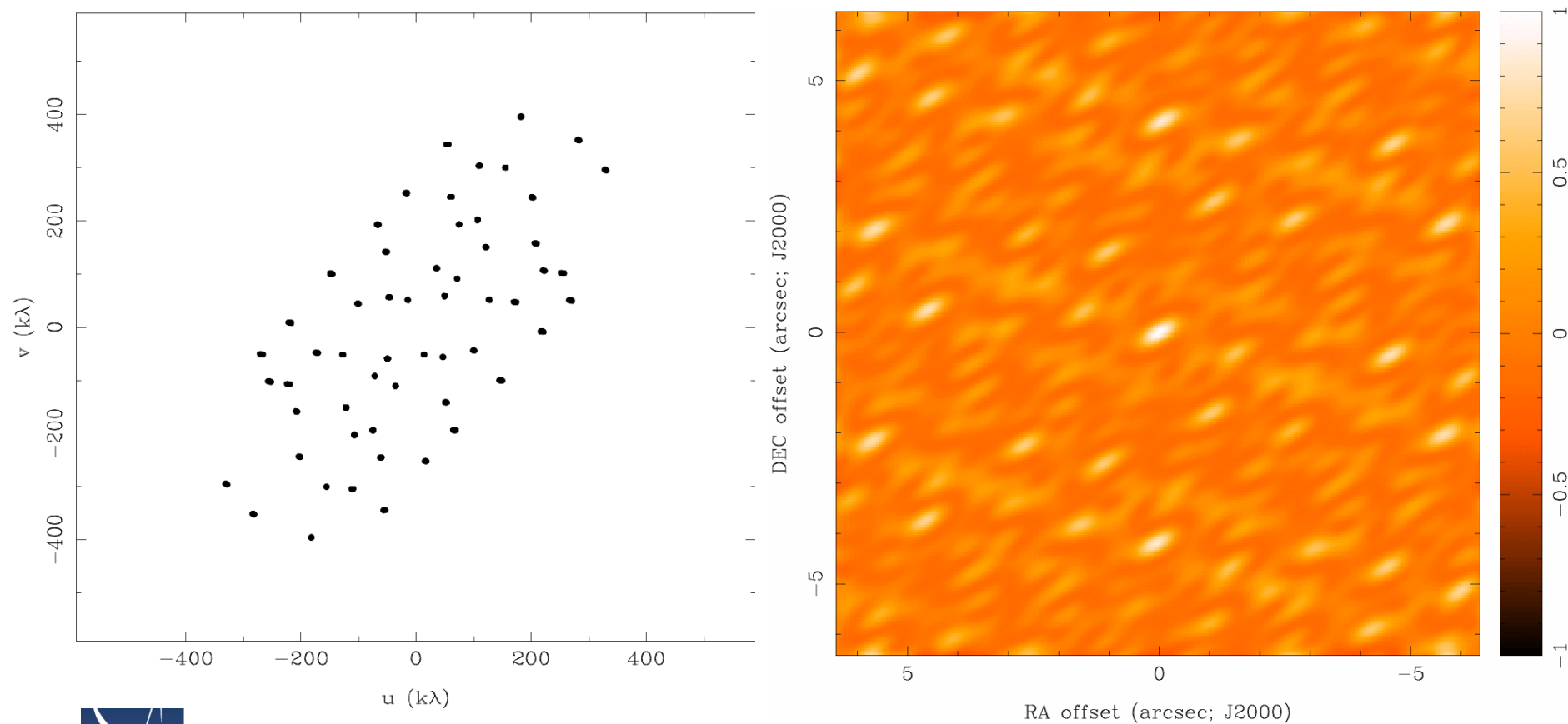
# Dirty Beam Shape and N Antennas

8 Antennas (28 baselines)



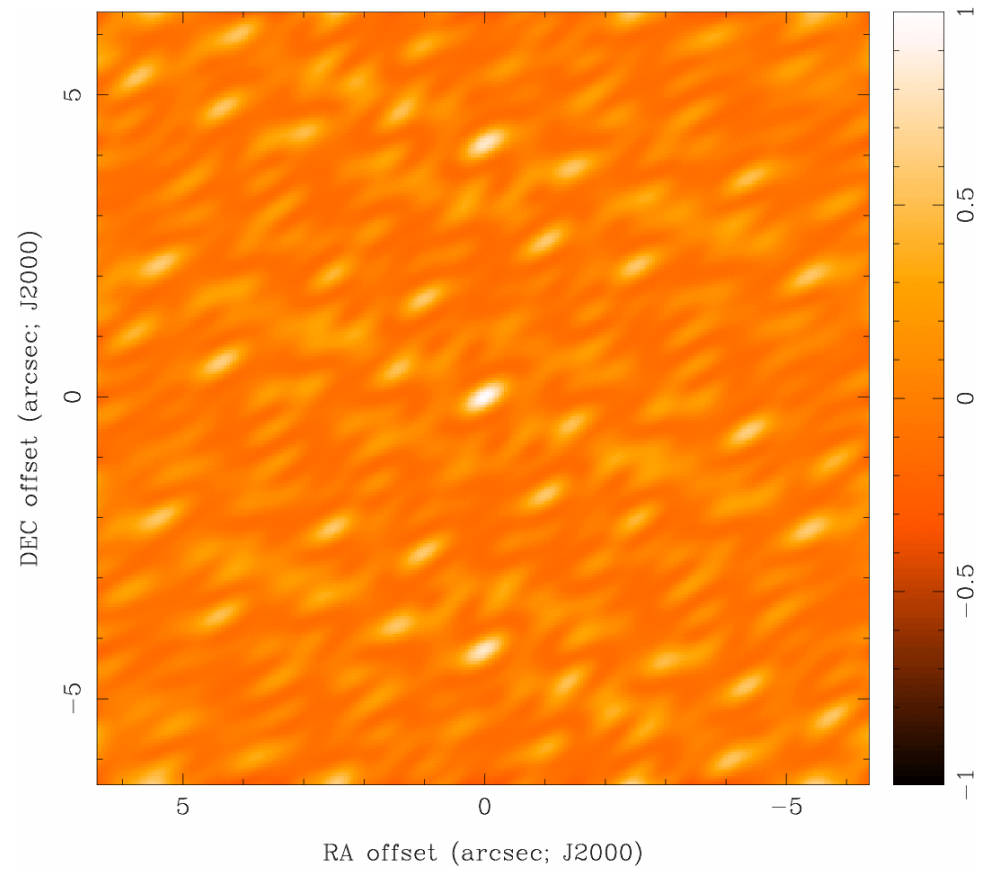
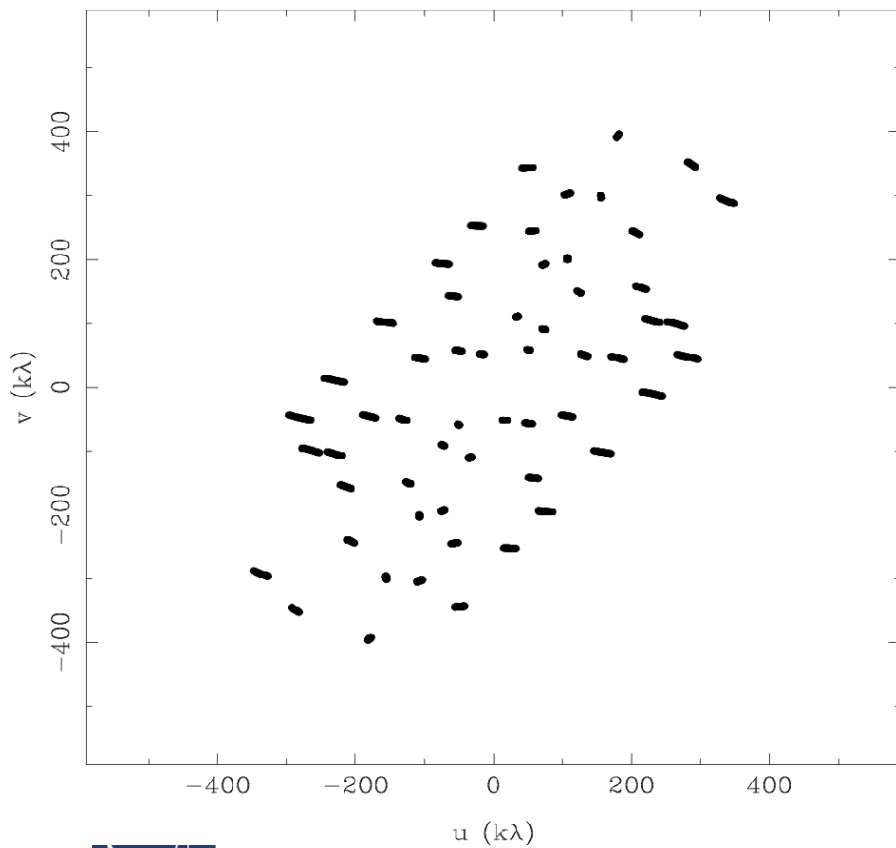
# Dirty Beam Shape and N Antennas

8 Antennas x 6 Samples



# Dirty Beam Shape and N Antennas

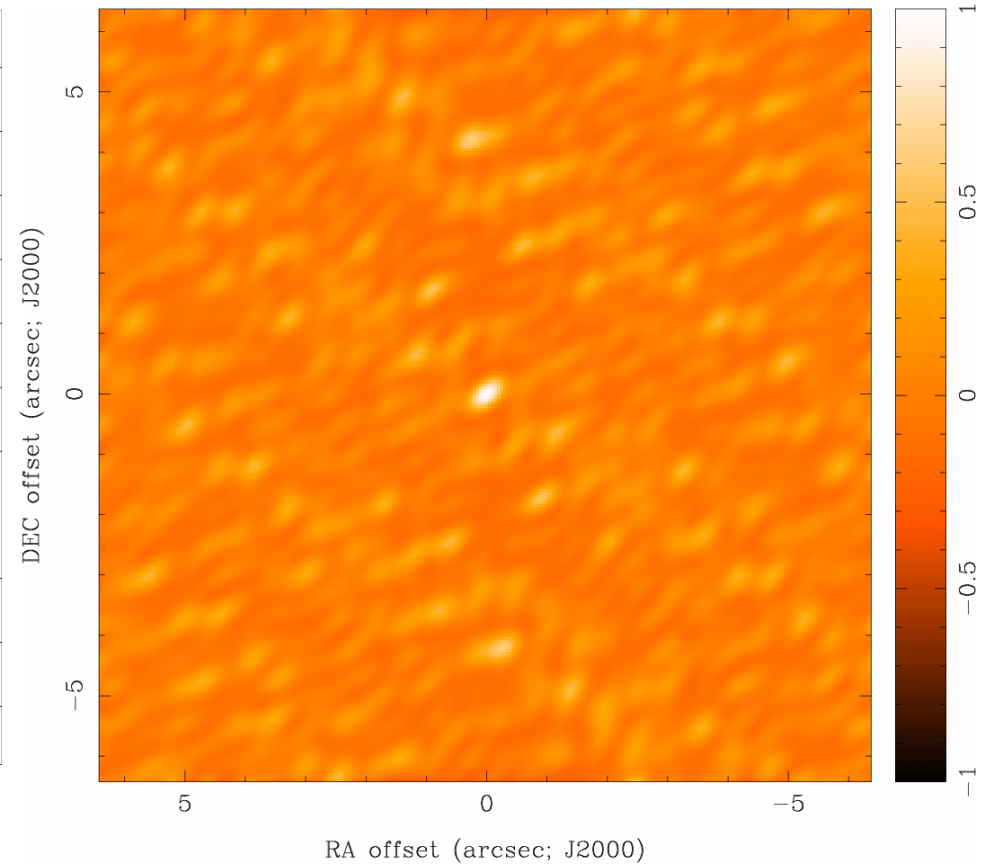
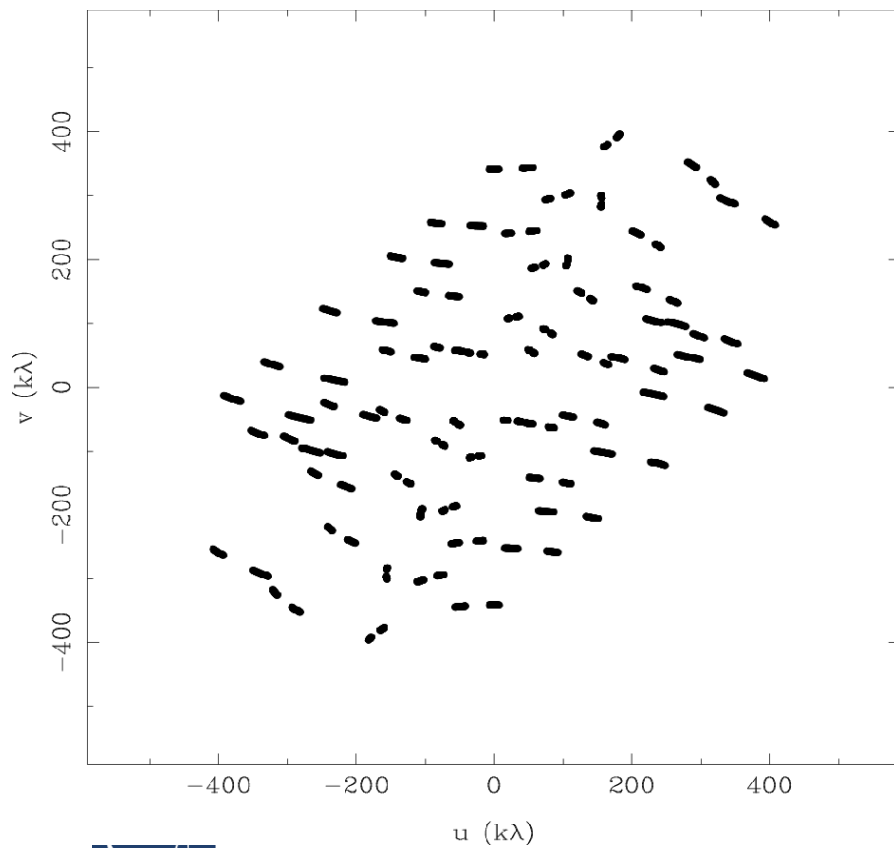
Earth Rotation! 8 Antennas x 30 Samples





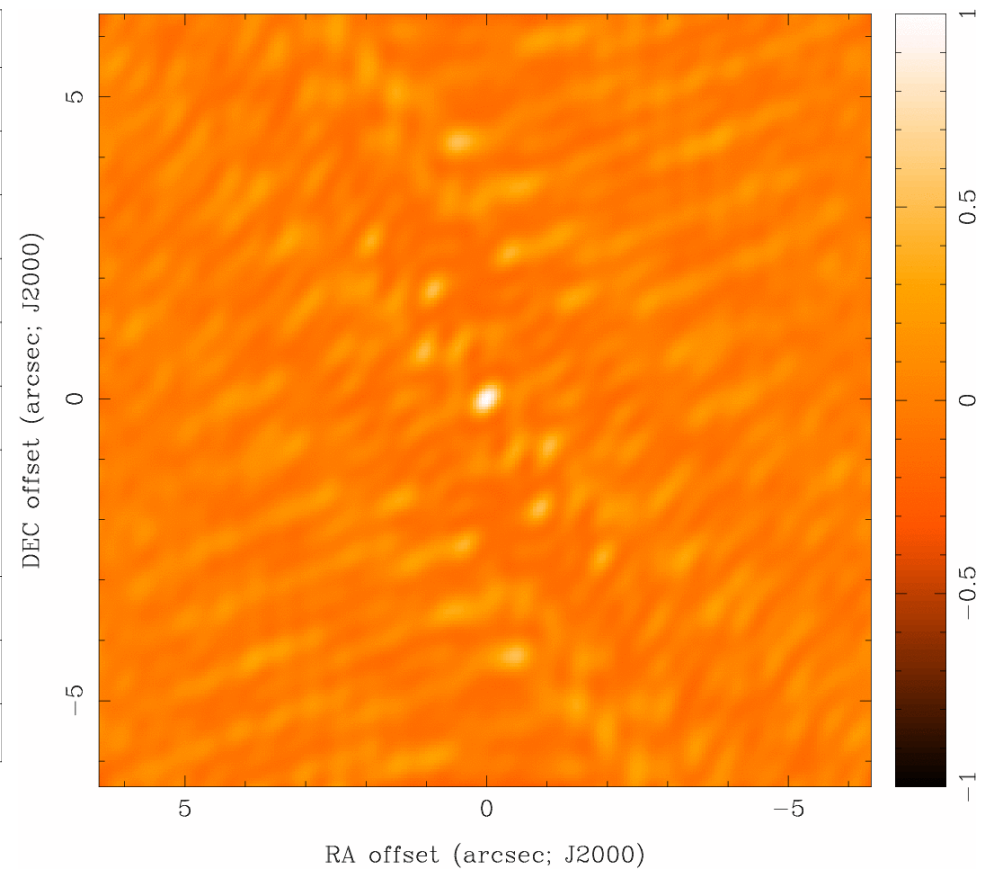
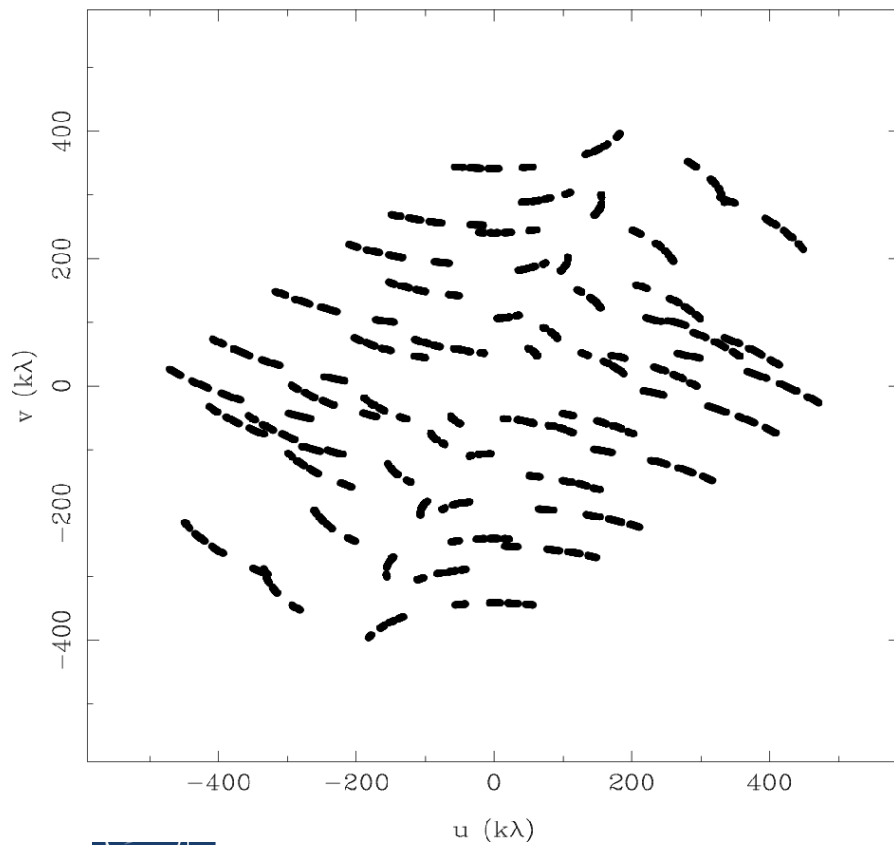
# Dirty Beam Shape and N Antennas

Earth Rotation! 8 Antennas x 60 Samples



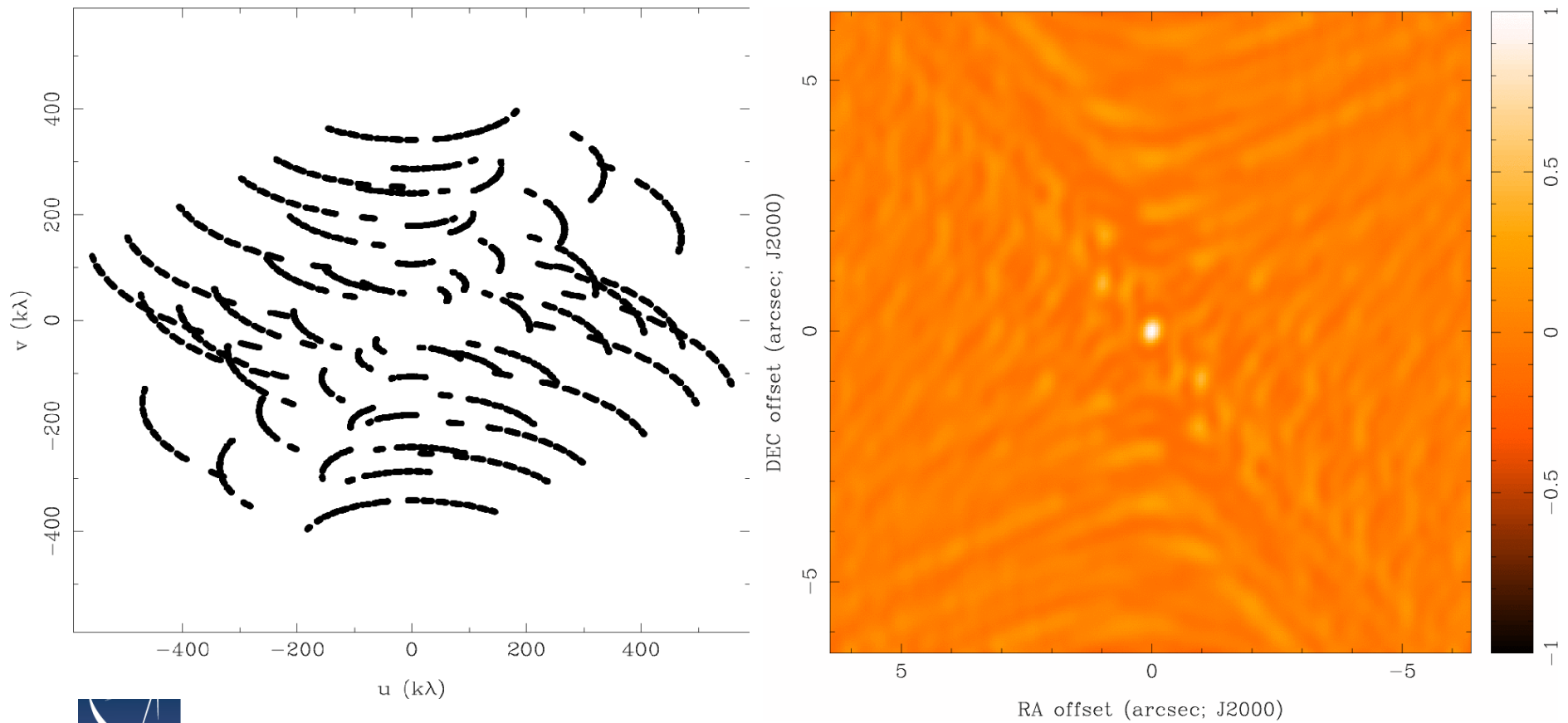
# Dirty Beam Shape and N Antennas

Earth Rotation! 8 Antennas x 120 Samples



# Dirty Beam Shape and N Antennas

Earth Rotation! 8 Antennas x 240 Samples



# Dirty Images from a Dirty Beam

- We sample the Fourier domain at discrete points

$$B(u, v) = \sum_k (u_k, v_k)$$

- The inverse Fourier Transform is

$$T^D(x, y) = FT^{-1}\{B(u, v) \times V(u, v)\}$$

- The convolution theorem tells us

$$T^D(x, y) = b(x, y) \otimes T(x, y)$$

- Where the point spread function is

$$b(x, y) = FT^{-1}\{B(u, v)\}$$

- Fourier transform of sampled visibilities yields the true sky brightness convolved with the point spread function (“dirty beam”)
- The “dirty image” is the true image convolved with the “dirty beam”

