

Introduction to Radio Interferometry



Danielle Lucero

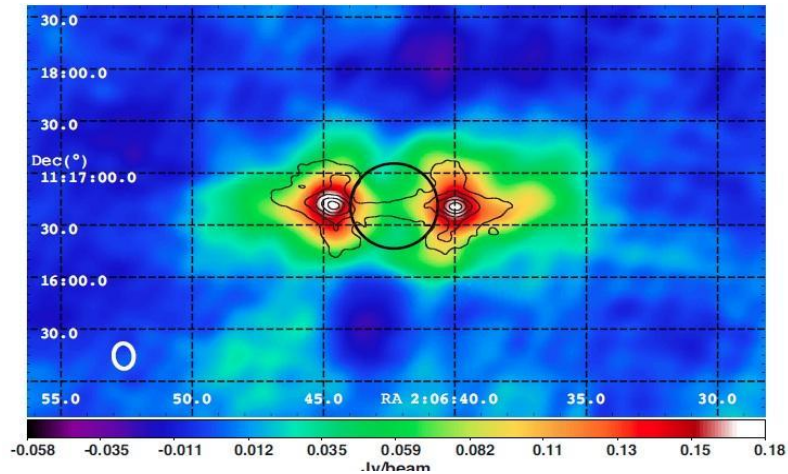
Authors: Alison Peck, Jim Braatz, Ashley Bemis, Sabrina Stierwalt

Atacama Large Millimeter/submillimeter Array
Karl G. Jansky Very Large Array
Very Long Baseline Array

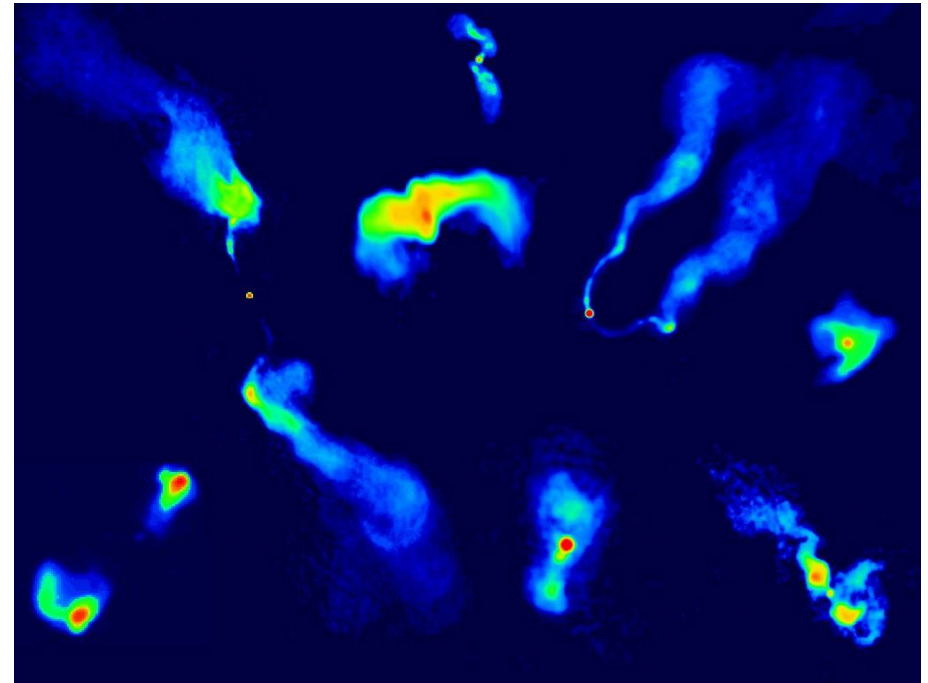


What can we observe? (MHz-GHz range)

Jupiter's radiation belt at 100MHz

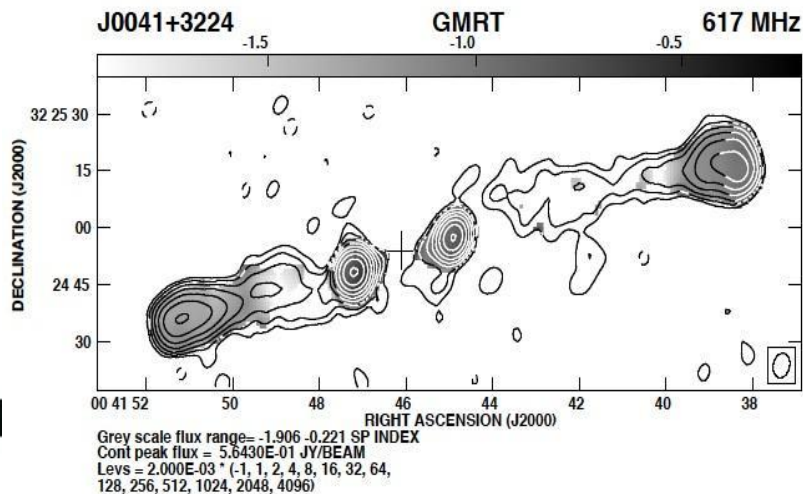


Relic emission from old radio galaxies



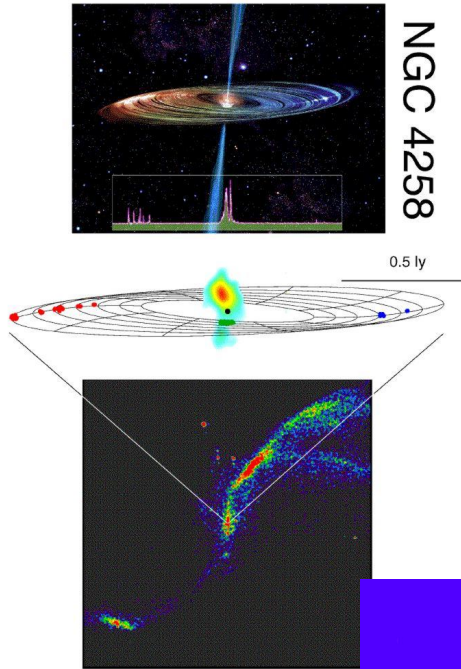
Synchrotron emission from extended radio galaxies (5 GHz)

Images from NRAO Image Gallery: <http://images.nrao.edu/>



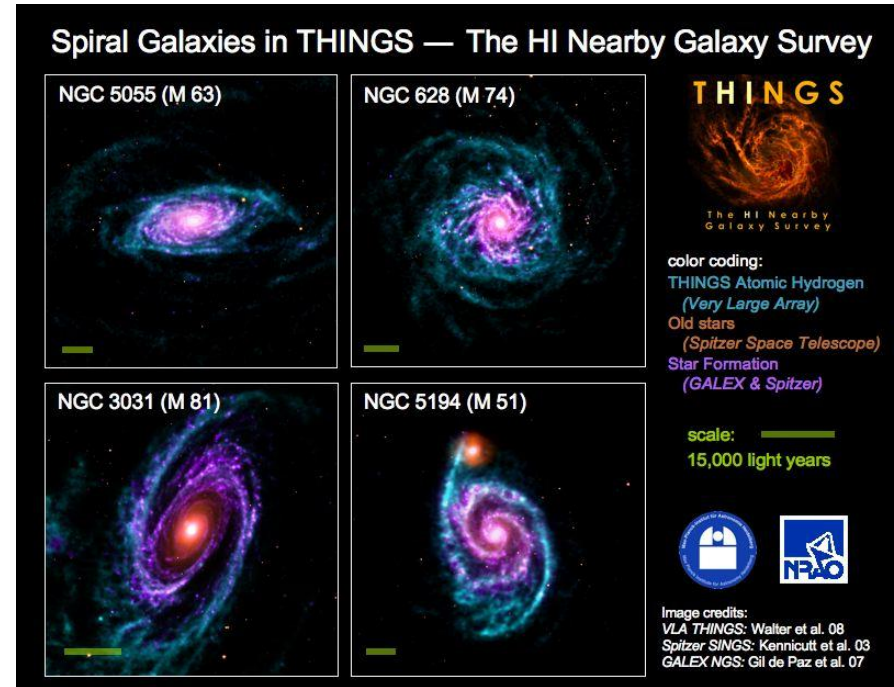
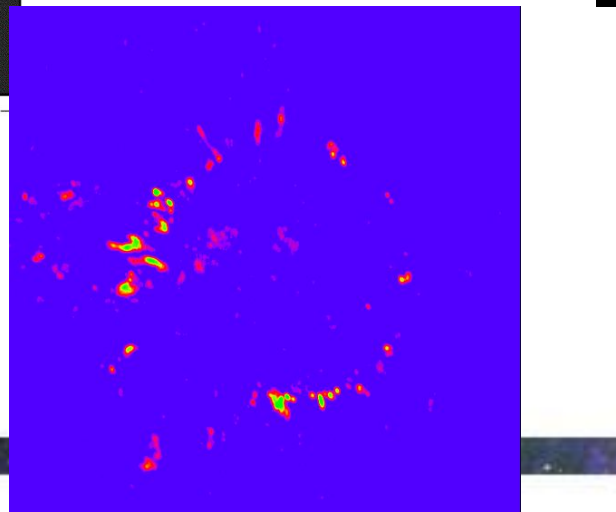
What can we observe?

At low frequencies (MHz-GHz):

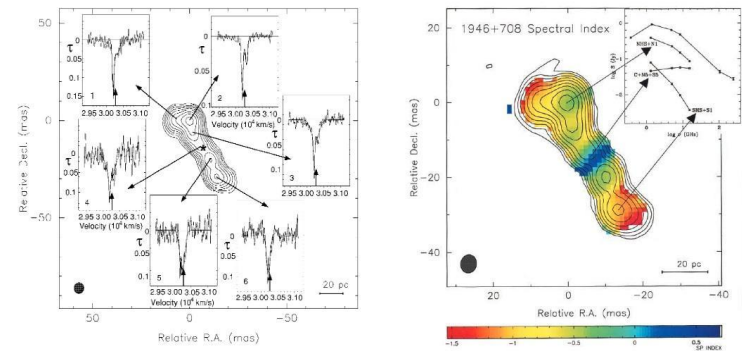


NGC 4258

H₂O, OH or SiO masers in galaxies and stars

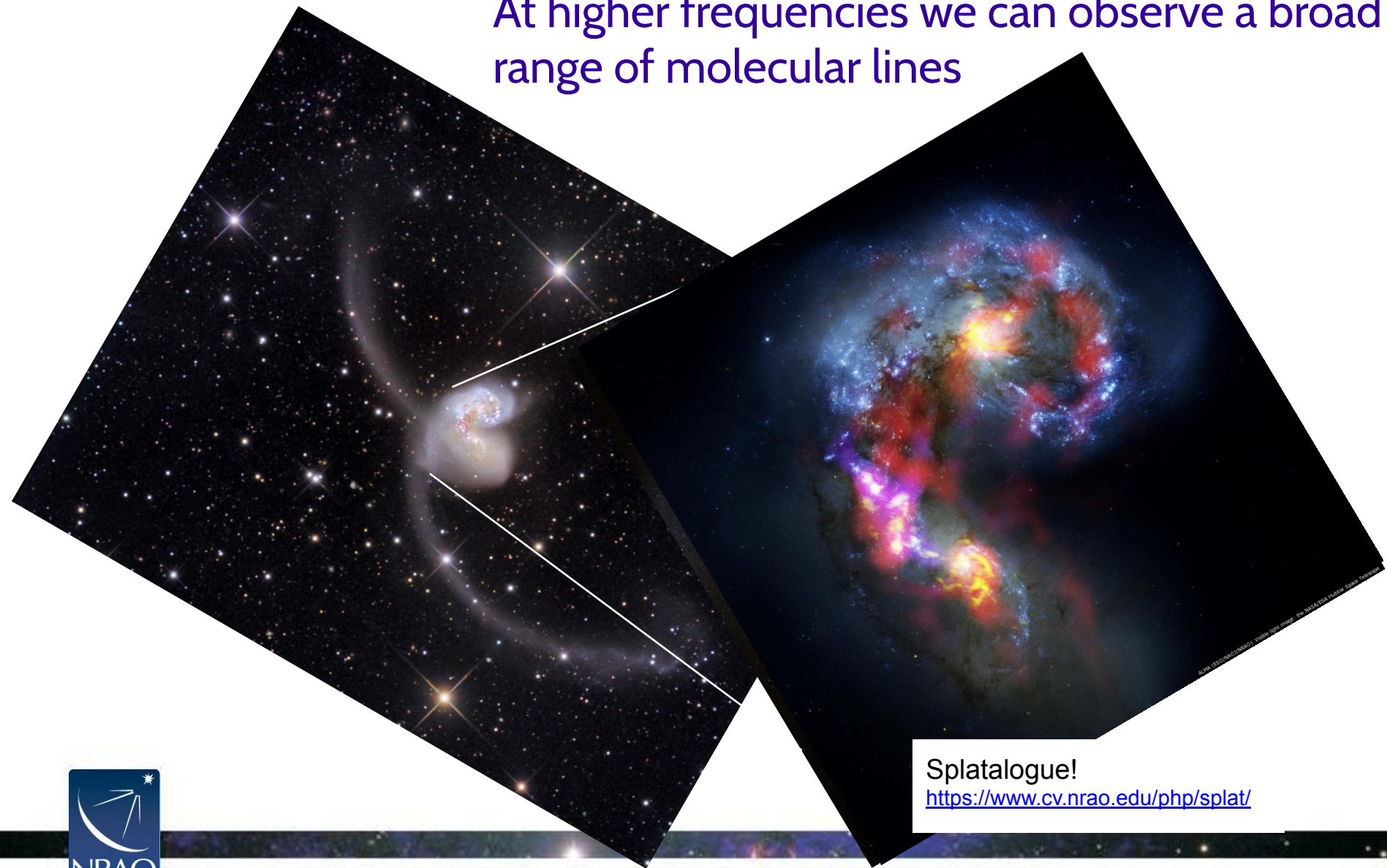


HI emission and absorption, free-free absorption in galaxies



What can we observe?

At higher frequencies we can observe a broad range of molecular lines



Splatalogue!

<https://www.cv.nrao.edu/php/splat/>

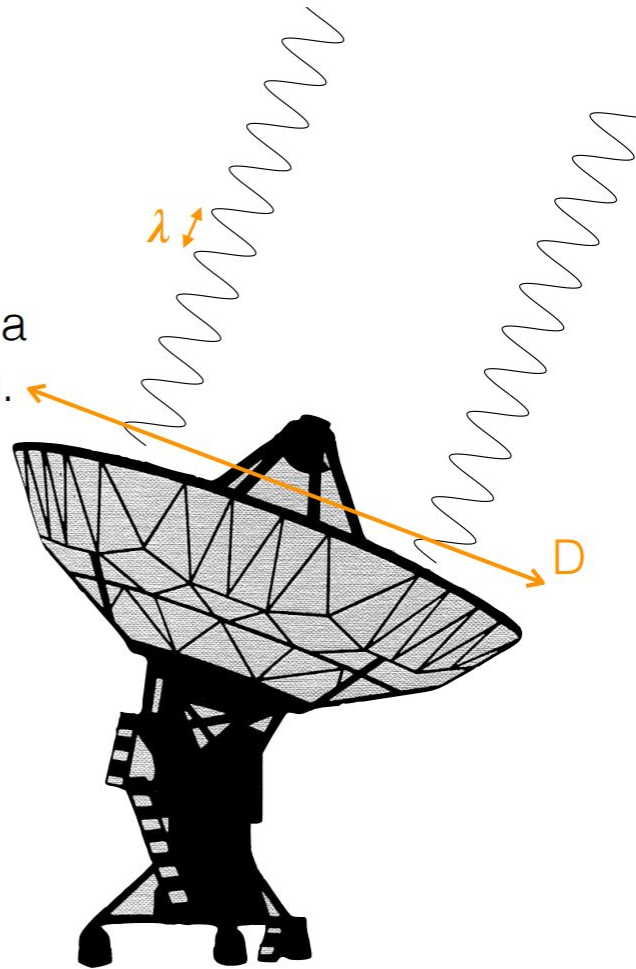


Long wavelength means no glass mirrors

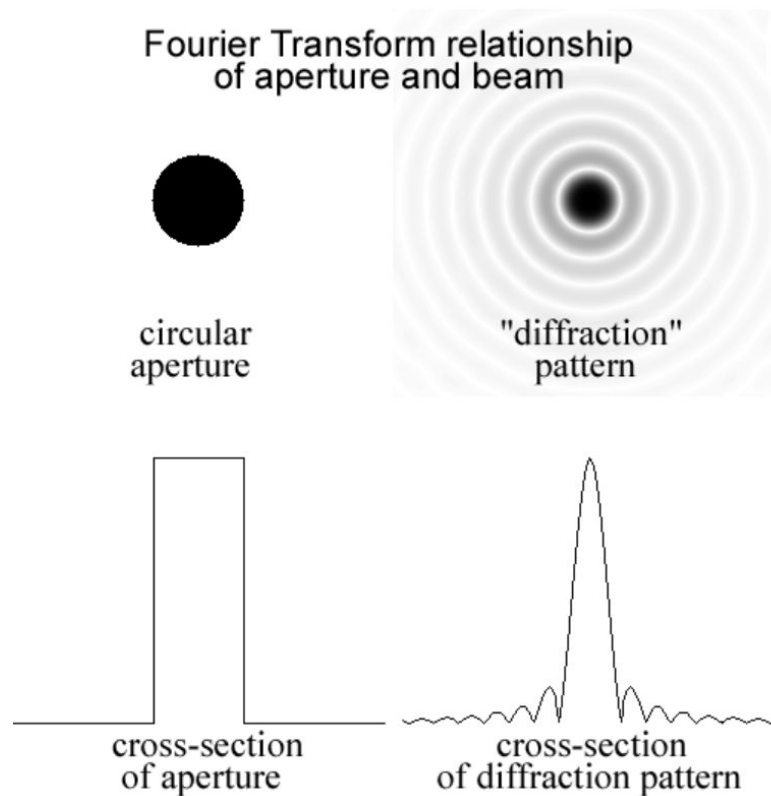


Single Dish

Diffraction theory: this telescope (by itself) has a resolution $\sim \lambda/D$ radians.



Associated with the collecting area (effective area) is the *beam pattern*, also called the *primary beam*, which is just the *Fourier Transform* of the aperture, as shown in the figure below.



Resolution of Observations

Angular resolution for most telescopes is $\sim \lambda/D$

D is the diameter of the telescope and λ is the wavelength of observation

For the Hubble Space Telescope:

$$\lambda \sim 1 \mu\text{m} / D \text{ of } 2.4\text{m} = \text{resolution} \sim 0.13''$$

To reach that resolution at $\lambda \sim 1\text{mm}$, we would need a 2 km-diameter dish!

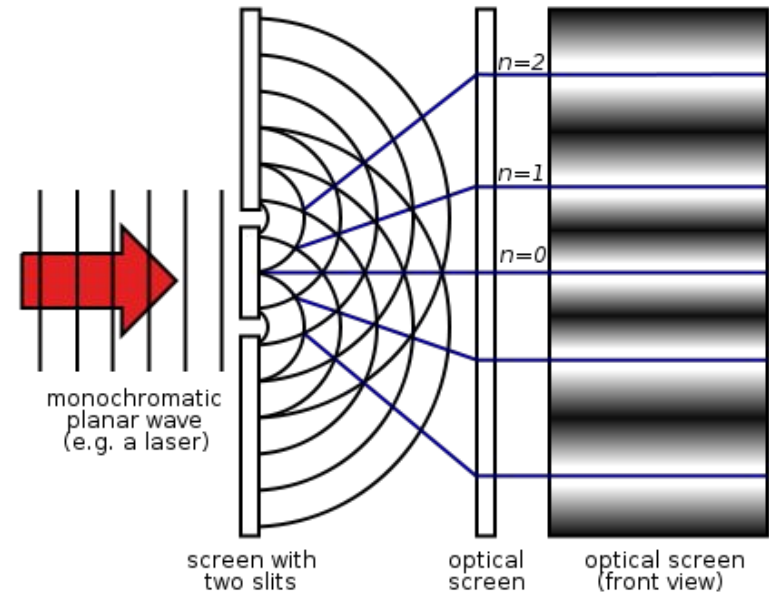
Instead, we use arrays of smaller dishes to achieve the same high angular resolution at radio frequencies

This is interferometry!



What is an interferometer?

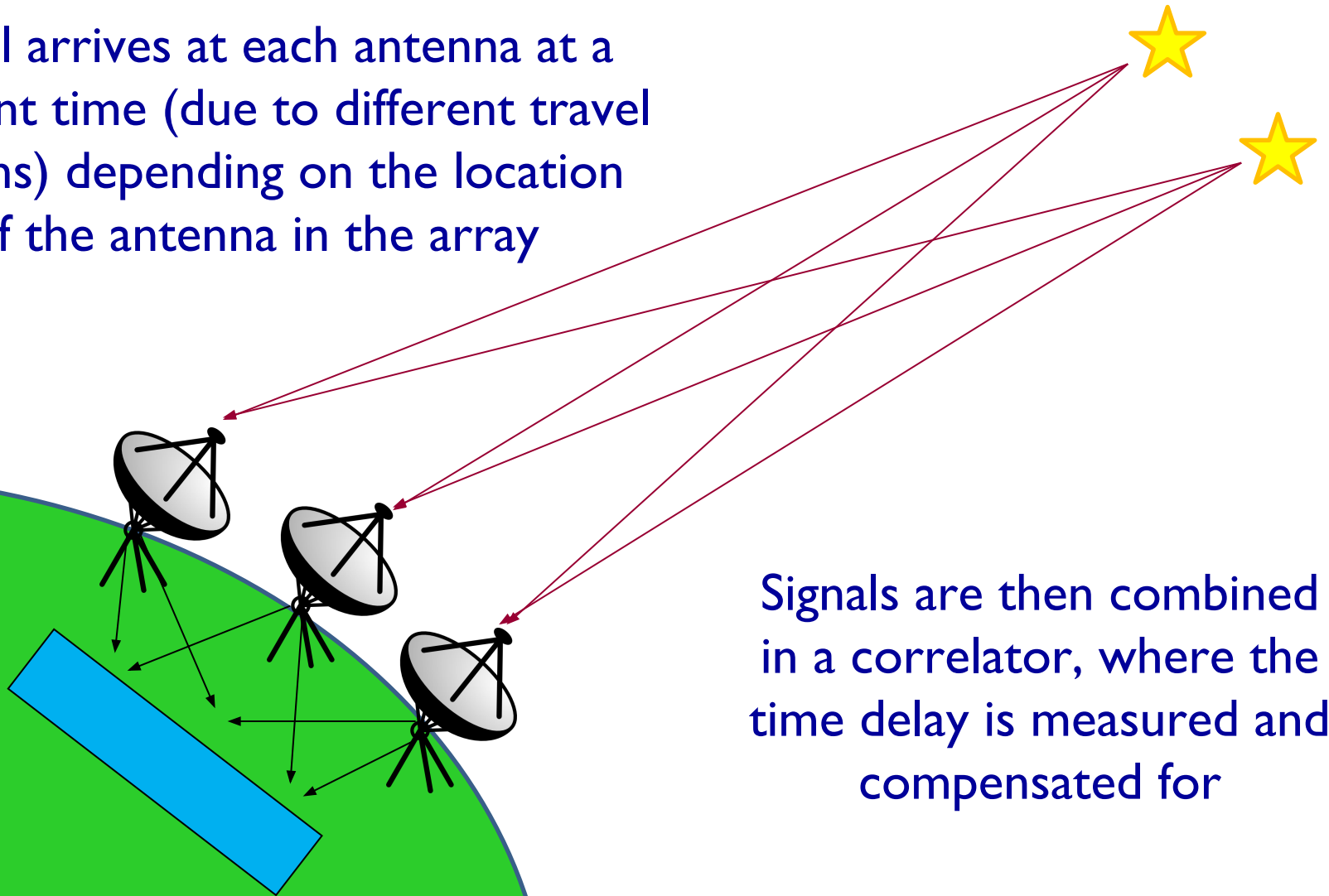
An *interferometer* measures the interference pattern produced by multiple apertures, much like a 2-slit experiment



However, the interference patterns measured by radio telescopes are produced by **multiplying - not adding - the wave signals measured at the different telescopes (i.e. apertures)*

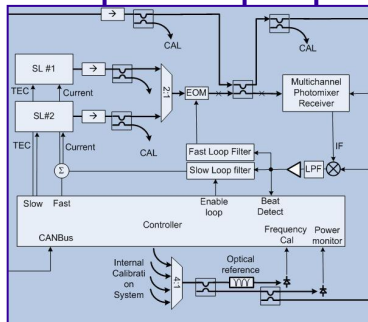
How Do We Use Interferometry?

Signal arrives at each antenna at a different time (due to different travel lengths) depending on the location of the antenna in the array



Signals are then combined in a correlator, where the time delay is measured and compensated for

Some Instrument Details



To precisely measure arrival times we need very accurate clocks

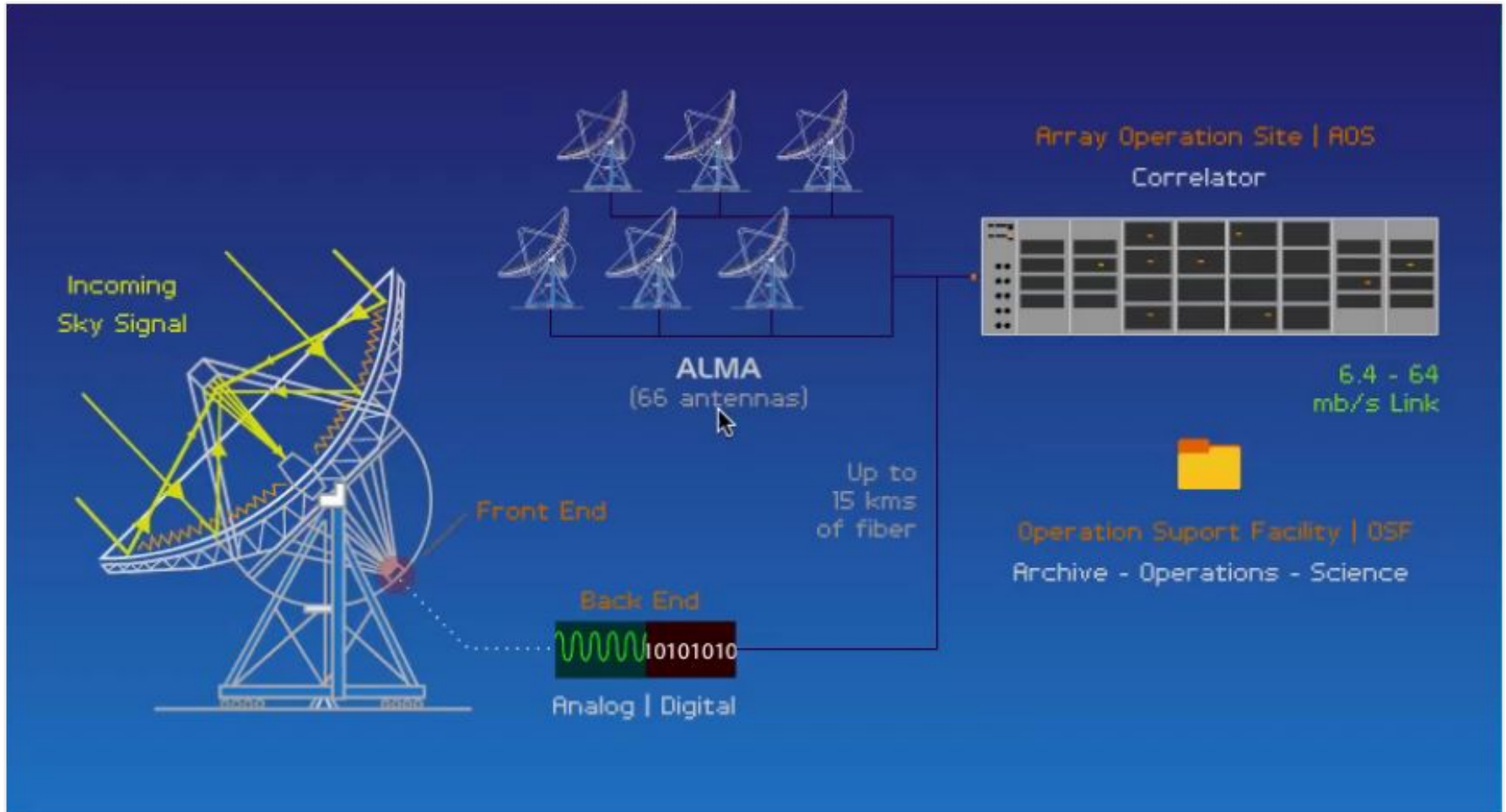
At Band 10 one wavelength error = 1 picosecond = 10^{-12} s (!!)

Need \ll 1 wavelength timing precision, so each antenna has an on-board clock with high sampling rates

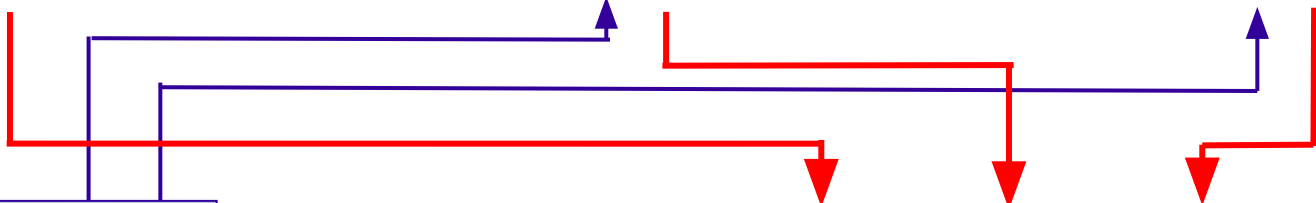
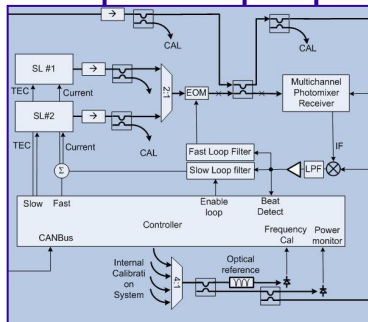
Once determined, the reference time is distributed to all antennas



An Interferometer In Action



Some Instrument Details



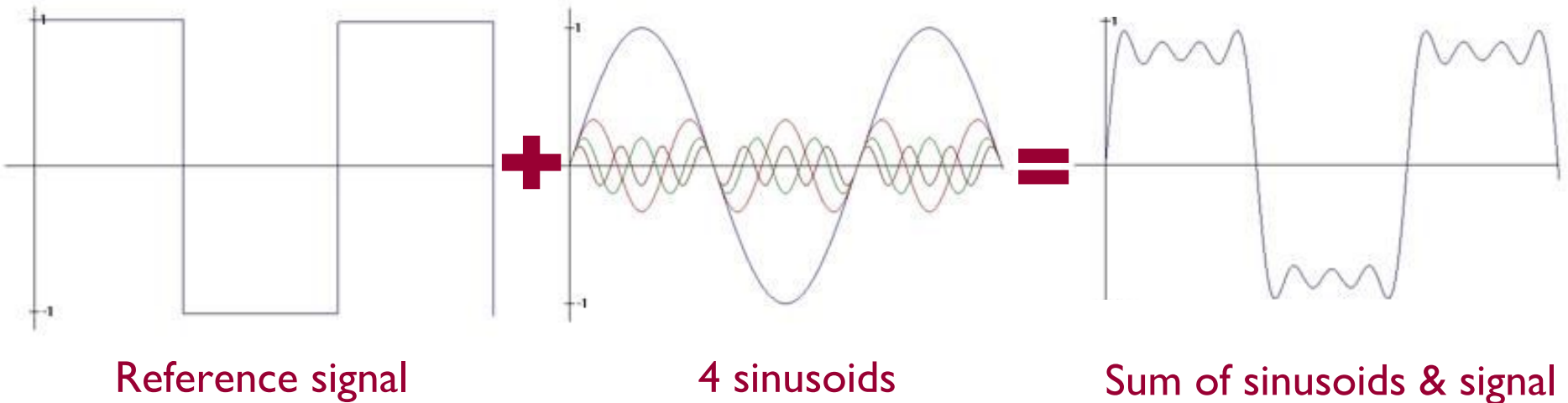
Signals from each antenna are digitized and sent to the correlator for multiplication & averaging

For ~50 antennas, the data rate is 600 GB/sec for the correlator to process



Introducing the Fourier Transform

Fourier theory states that any well behaved signal (including images) can be expressed as the sum of sinusoids



The Fourier transform is the mathematical tool that decomposes a signal into its sinusoidal components

The Fourier transform contains *all* of the information of the original signal

- Fourier Transform Wikipedia Page:
https://en.wikipedia.org/wiki/Fourier_transform
- Here is a nifty simple interactive demonstration of Fourier Transforms. <http://www.jezzamon.com/fourier/>



Visibility and Sky Brightness

*The van
Cittert-Zernike
theorem*

- **Visibility as a function of baseline coordinates (u,v) is the Fourier transform of the sky brightness distribution as a function of the sky coordinates (x,y)**

$$V(u, v) \xrightarrow{\text{FT}} T(x, y)$$

$$V(u, v) = \text{the complex visibility function} = \iint T(x, y) e^{2\pi i(ux+vy)} dx dy$$

$$T(x, y) = \text{the sky brightness distribution} = \iint V(u, v) e^{-2\pi i(ux+vy)} du dv$$



The Fourier Transform relates the measured interference pattern to the radio intensity on the sky

Fourier

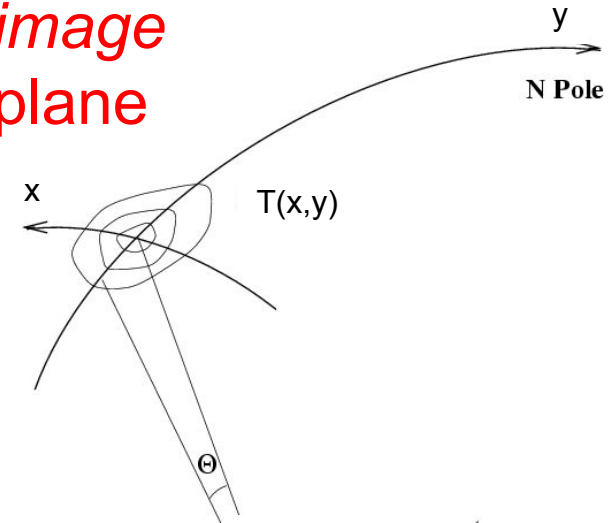
$$V(u, v) = \iint T(x, y) e^{2\pi i(ux+vy)} dx dy$$

Image

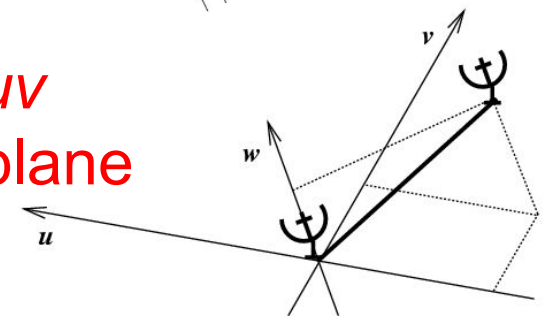
$$T(x, y) = \iint V(u, v) e^{-2\pi i(ux+vy)} du dv$$

(for more info, see e.g. Thompson, Moran & Swenson)

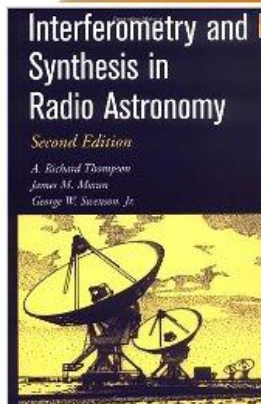
image plane



uv plane

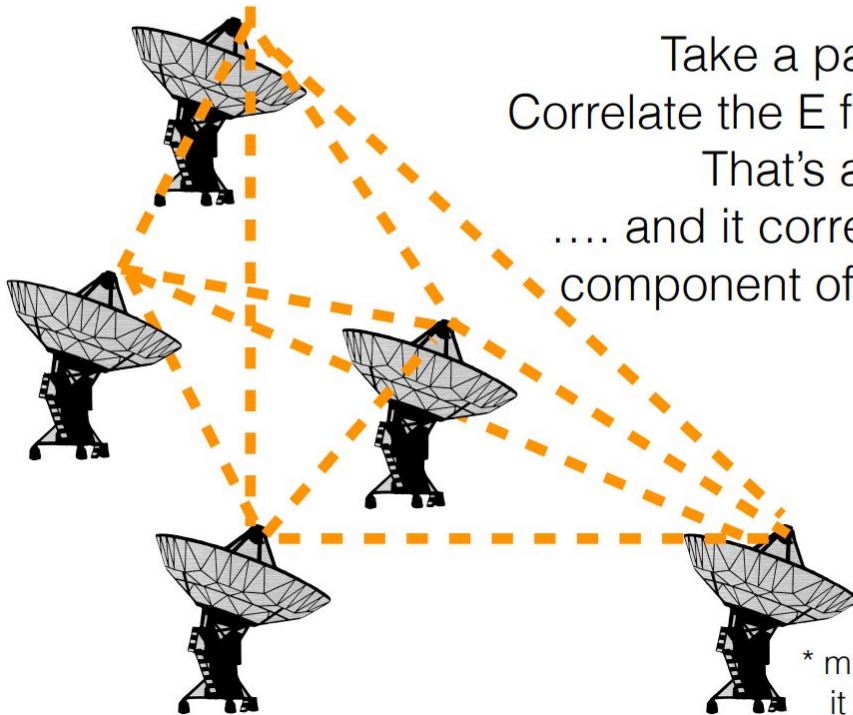


Click to LOOK INSIDE!



Interferometer theory, very loosely.

correlation* of E field at Earth = FT of brightness
distribution of the sky.



Take a pair of antennas.
Correlate the E fields at each antenna.
That's a "visibility" ...
.... and it corresponds to a Fourier
component of the sky brightness.

* mutual coherence function, but
it looks a lot like a correlation

What Are Visibilities?

Each $V(u,v)$ contains information on $T(x,y)$ everywhere

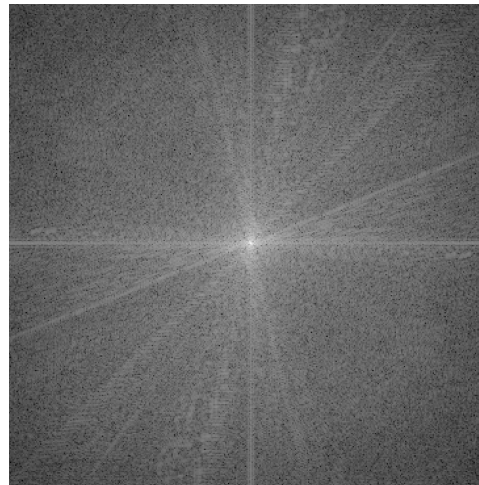
Each $V(u,v)$ is a complex quantity

Expressed as (real, imaginary) or (amplitude, phase)

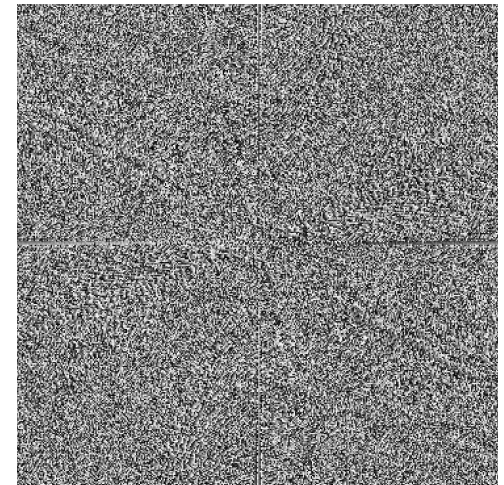


$T(x,y)$

FT
→

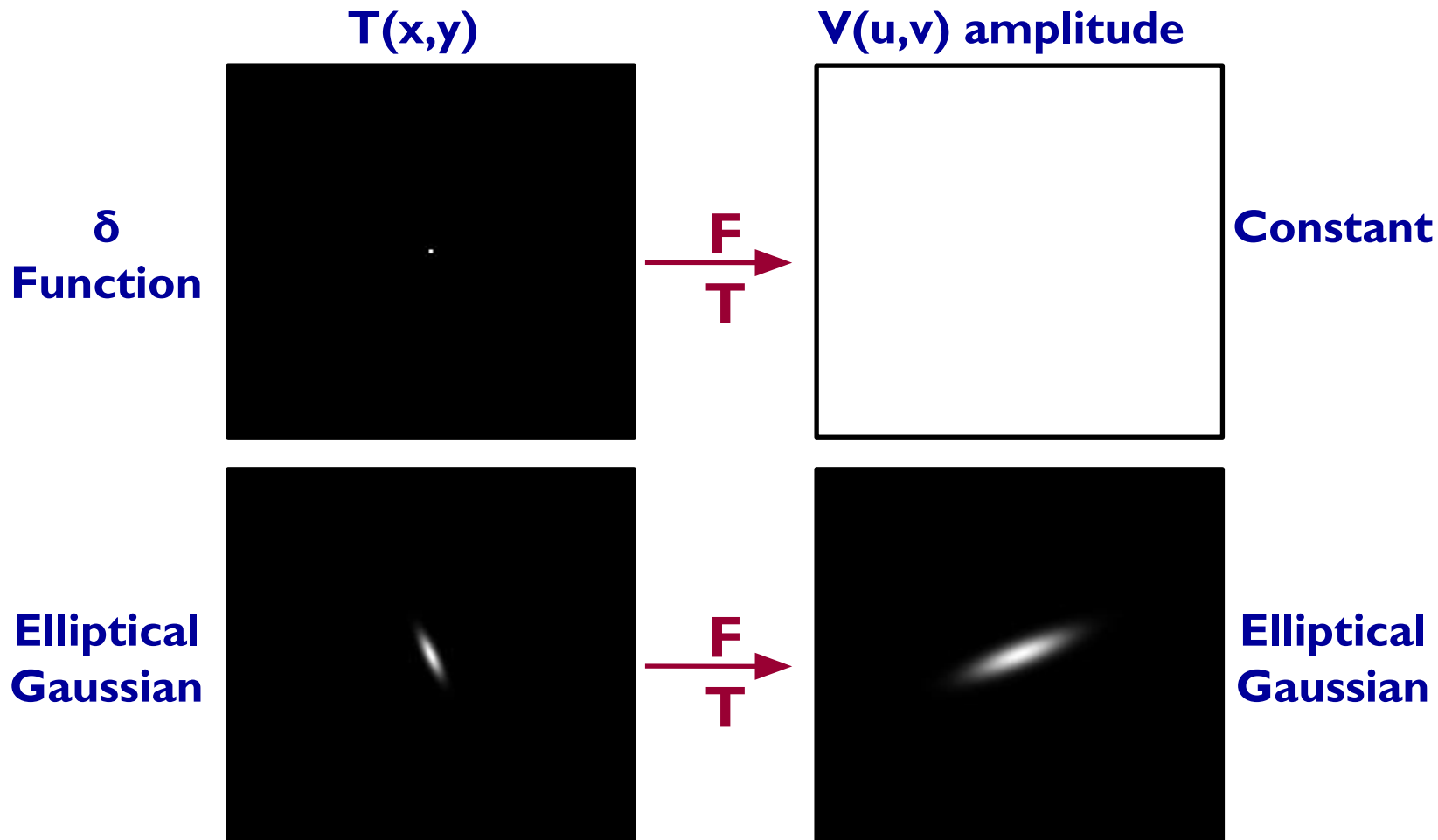


$V(u,v)$ amplitude



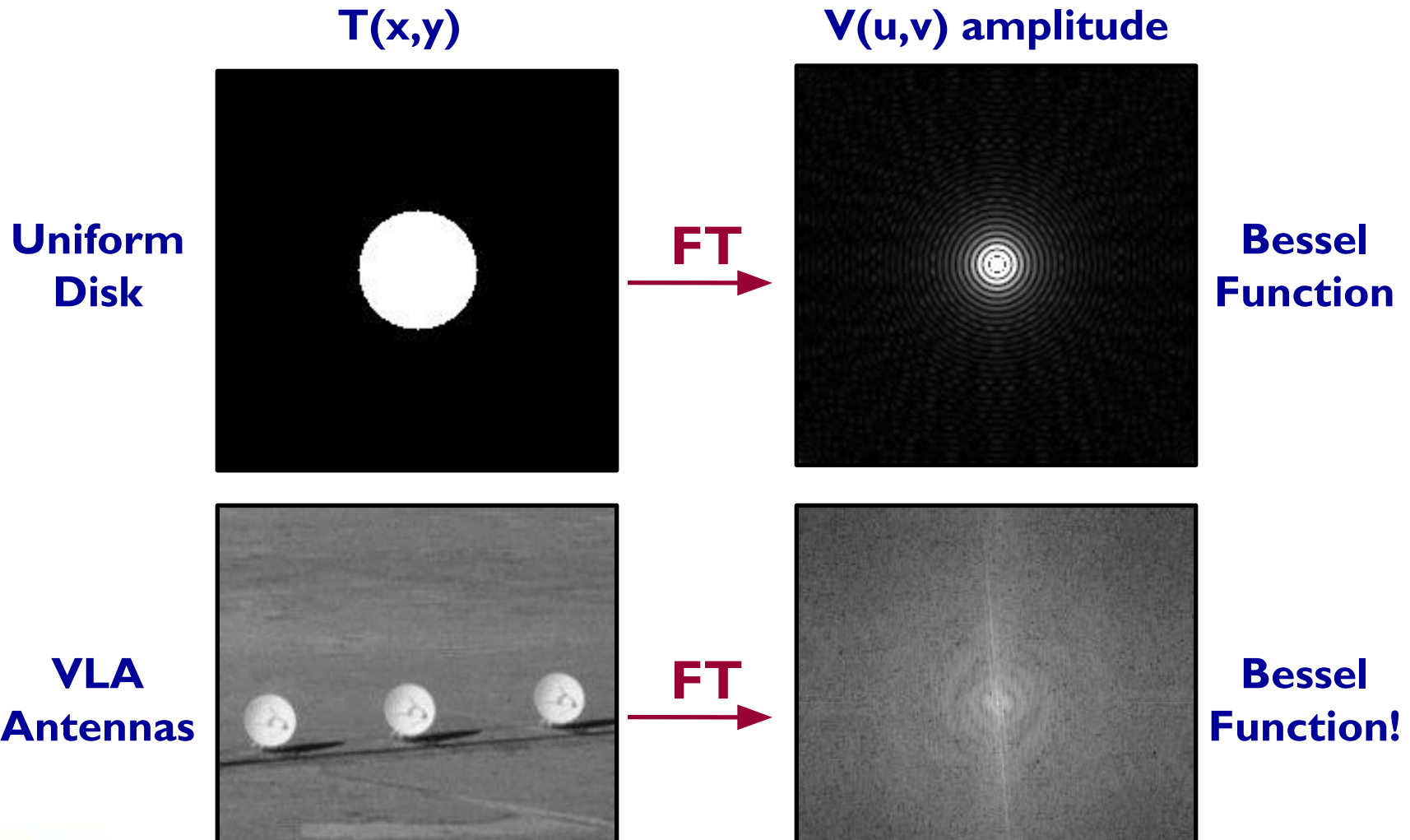
$V(u,v)$ phase

Examples of 2D Fourier Transforms



Rules of the Fourier Transform:
Narrow features transform to wide features (and vice versa)

Examples of 2D Fourier Transforms



Rules of the Fourier Transform:

Sharp features (edges) result in many high spatial features

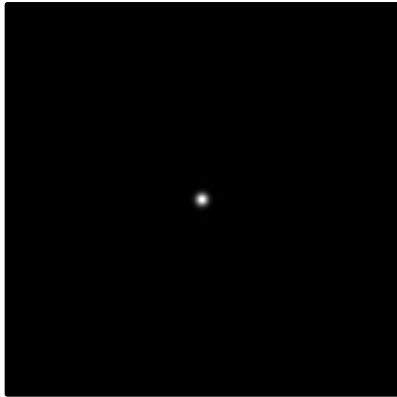
Examples of 2D Fourier Transforms

$T(x,y)$

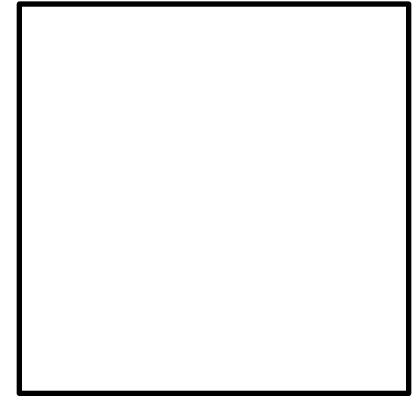
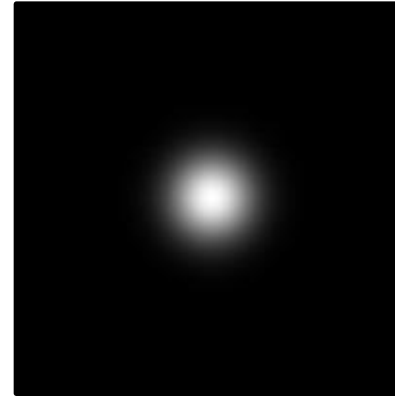
$V(u,v)$ amplitude

$V(u,v)$ phase

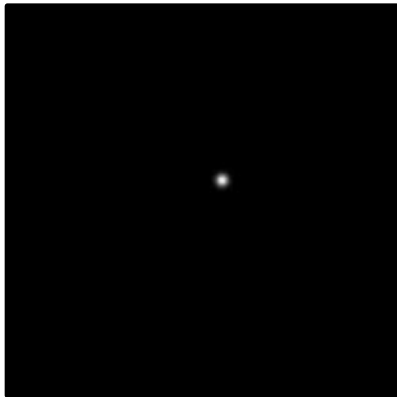
Centered
Gaussian



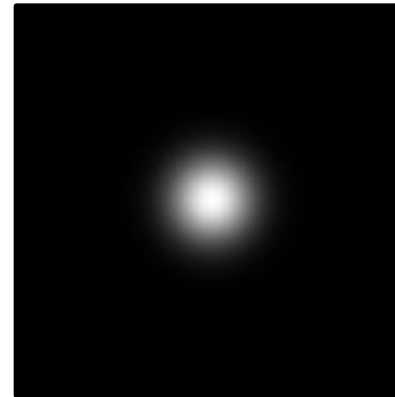
FT
→



Offset
Gaussian



FT
→



Rules of the Fourier Transform:

Amplitude tells you 'how much' of a spatial frequency

Phase tells you 'where' the spatial frequency is

Some Comments on Visibilities

- The Visibility is a unique function of the source brightness.
- The two functions are related through a Fourier transform. $V_v(u, v) \Leftrightarrow I(l, m)$
- An interferometer, at any one time, makes one measure of the visibility, at baseline coordinate (u,v).
- ‘Sufficient knowledge’ of the visibility function (as derived from an interferometer) will provide us a ‘reasonable estimate’ of the source brightness.
- How many is ‘sufficient’, and how good is ‘reasonable’?
- These simple questions do not have easy answers...



Basics of Aperture Synthesis

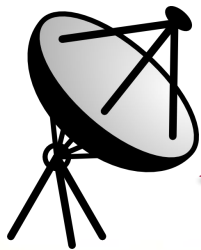
Idea: Sample $V(u,v)$ at an enough (u,v) points using distributed small aperture antennas to synthesize a large aperture antenna of size (u_{\max}, v_{\max})

One pair of antennas = one baseline

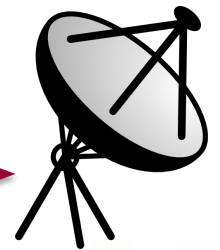
For **N** antennas, we get **$N(N-1)$** samples at a time

How do we fill in the rest of the (u,v) plane?

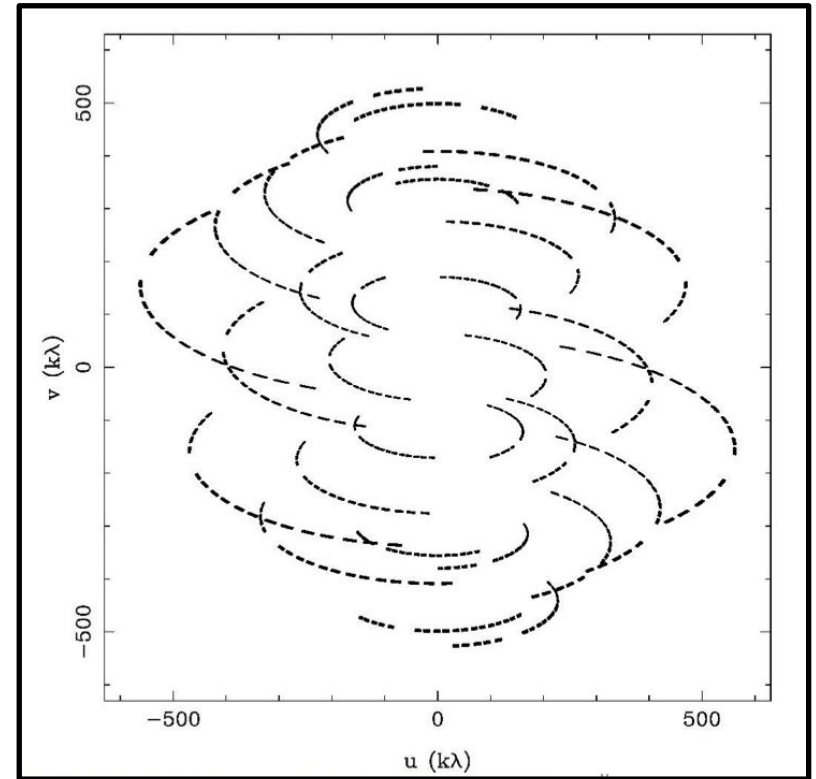
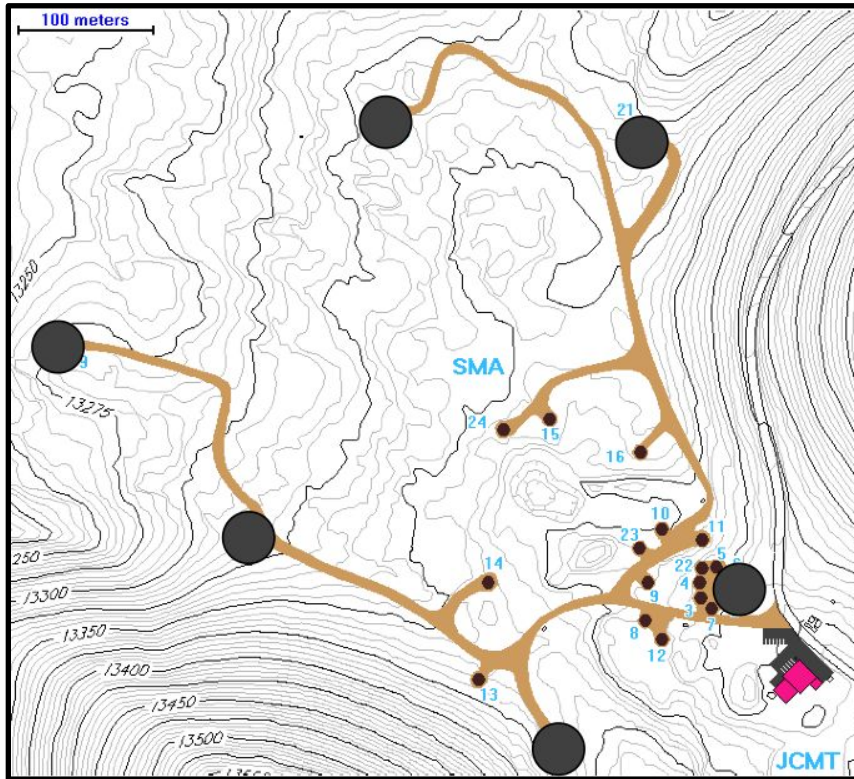
1. Earth's rotation
2. Reconfigure physical layout of N antennas



One baseline = 2 (u,v) points



(u,v) Plane Sampling



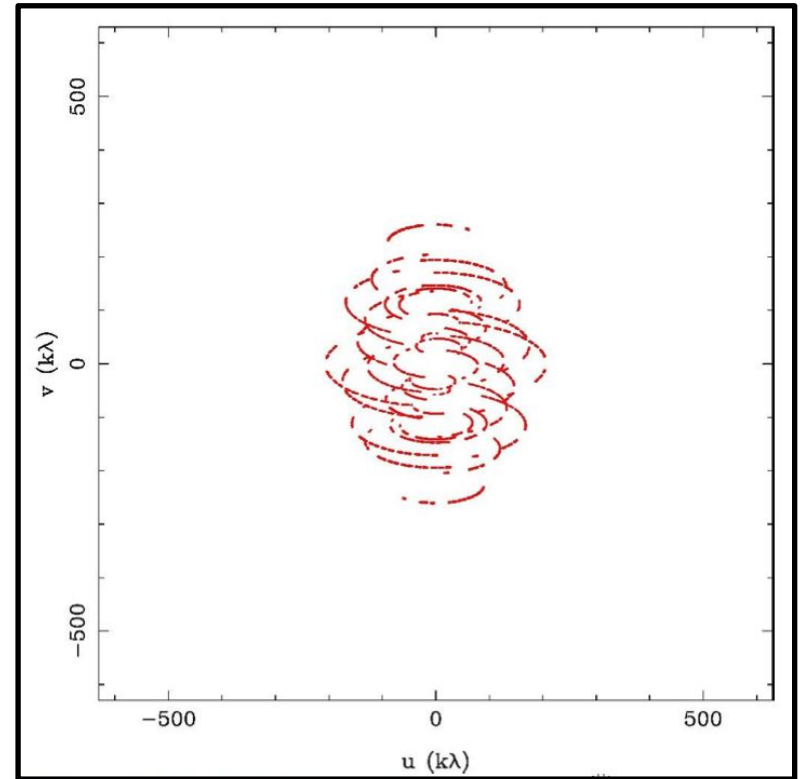
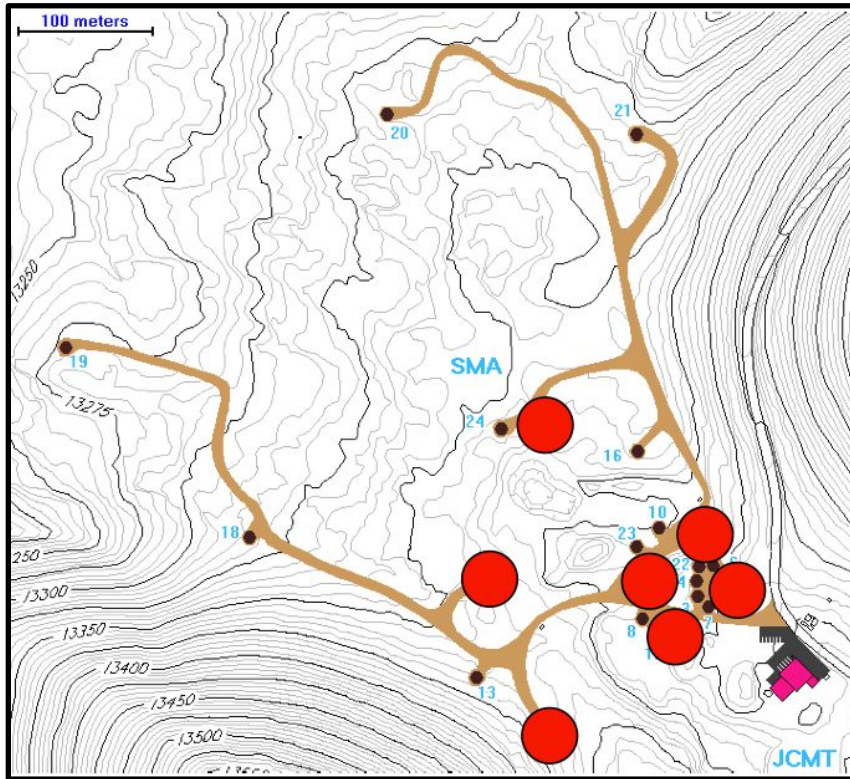
Very Extended SMA configuration

(most extended baselines)

345 GHz, DEC = +22



(u,v) Plane Sampling



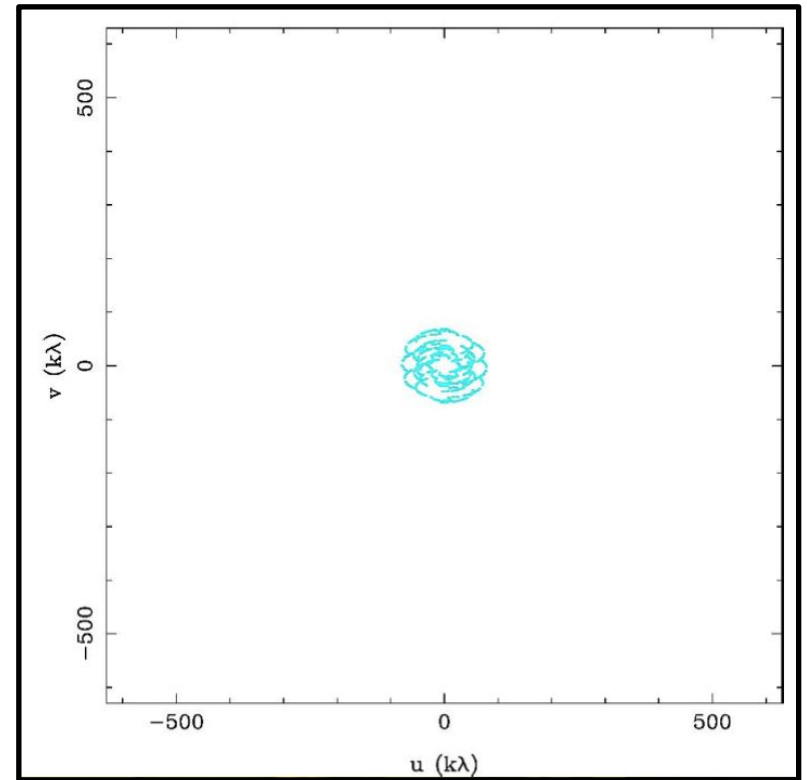
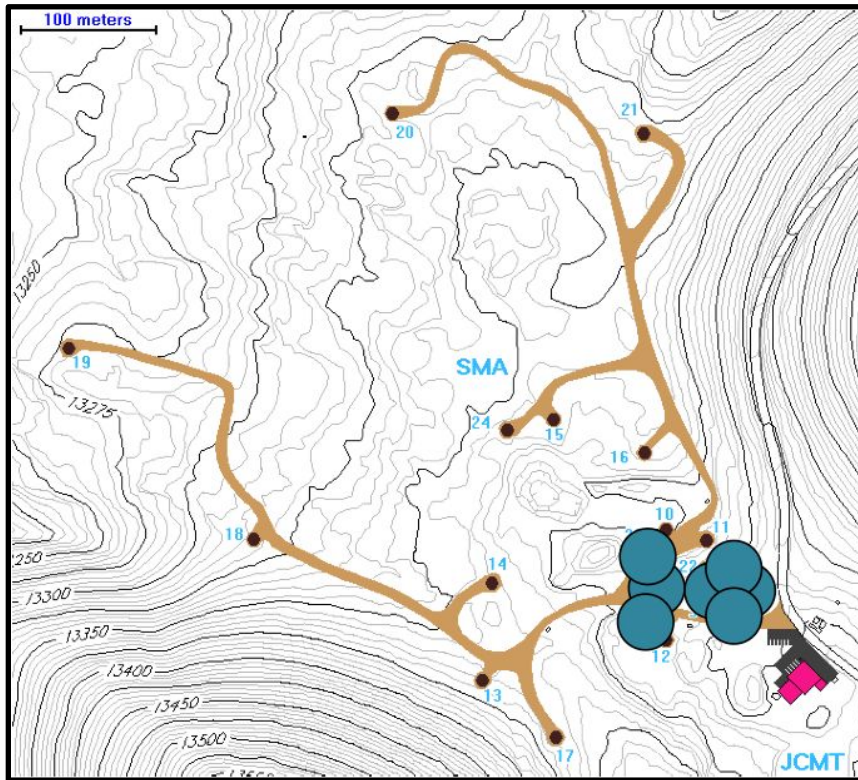
Extended SMA configuration

(extended baselines)

345 GHz, DEC = +22



(u,v) Plane Sampling



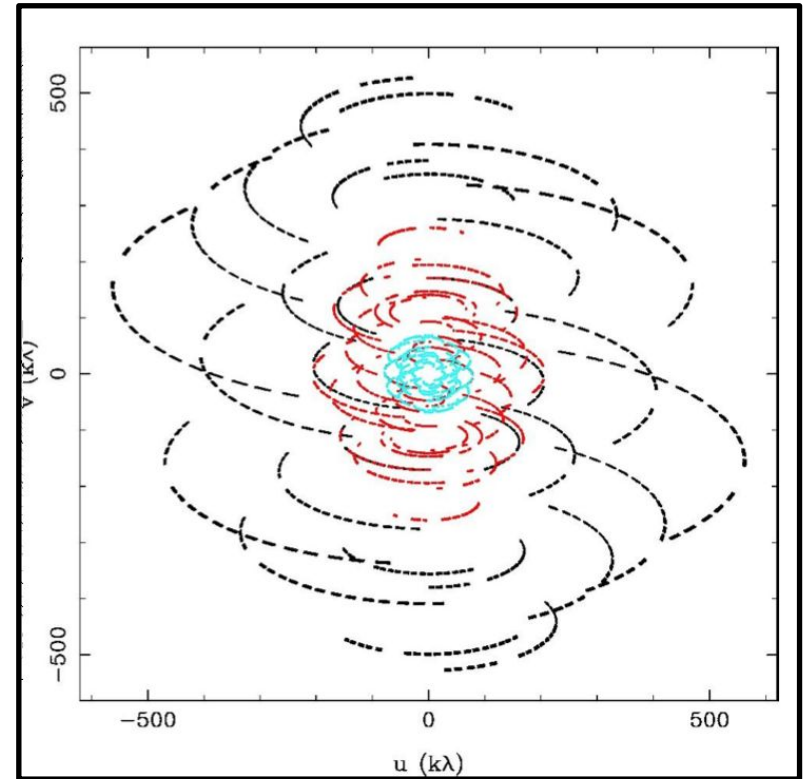
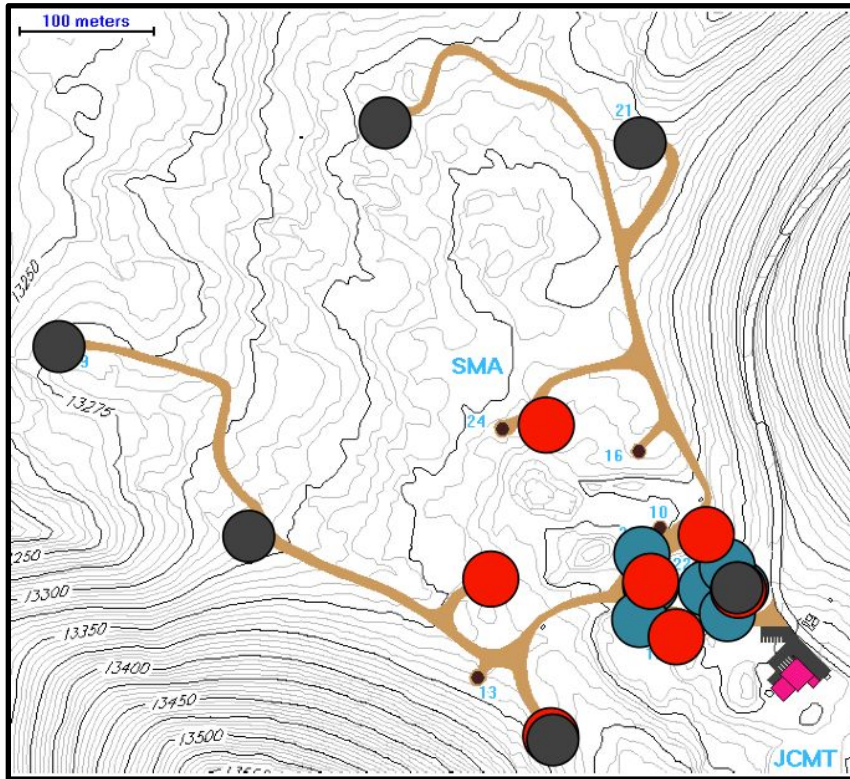
Compact SMA configuration

(compact baselines)

345 GHz, DEC = +22



(u,v) Plane Sampling

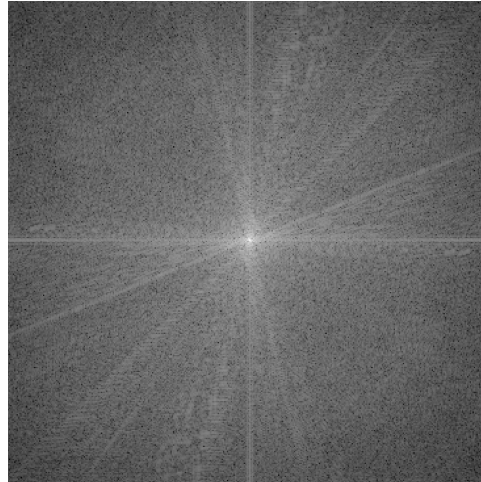


Combine multiple configurations to get the most complete coverage of the (u,v) plane

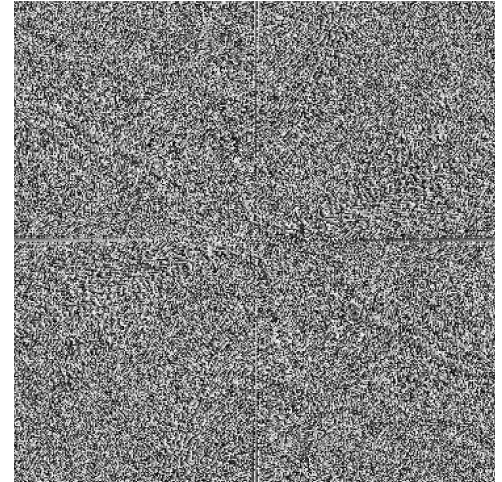


$T(x,y)$

FT
→



$V(u,v)$ amplitude



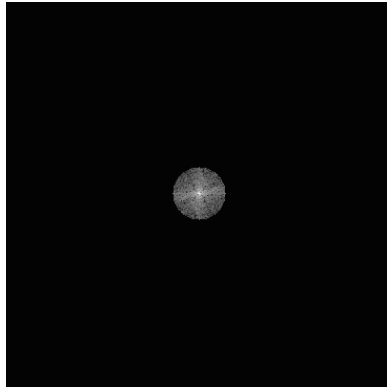
$V(u,v)$ phase

Implications of (u,v) Coverage

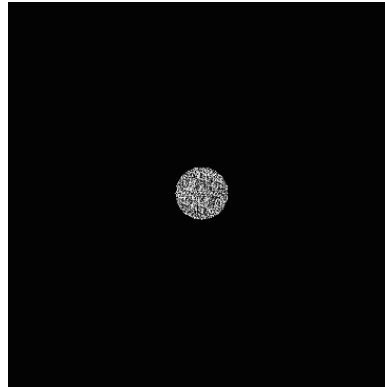
What does it mean if our (u,v) coverage is not complete?

Missing High
Spatial
Frequencies

$V(u,v)$ amplitude



$V(u,v)$ phase



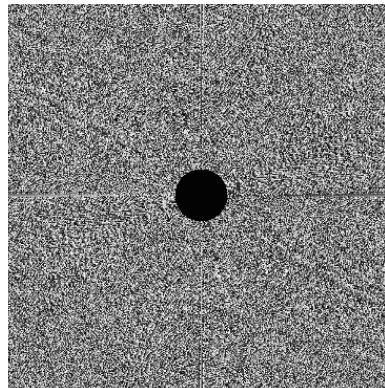
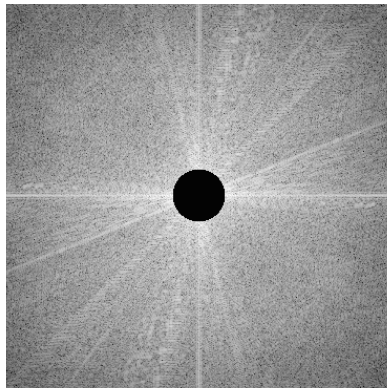
FT



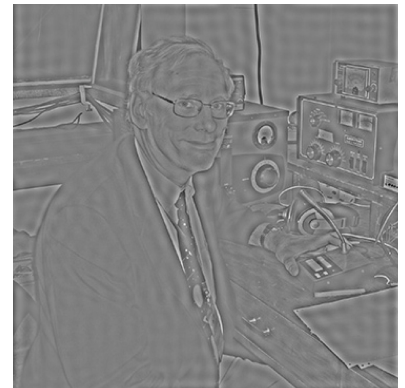
$T(x,y)$



Missing Low
Spatial
Frequencies



FT



Characteristic Angular Scales

Angular resolution of telescope array:

$$\sim \lambda/B_{\max} \quad (B_{\max} = \text{longest baseline})$$

Maximum angular scale:

$$\sim \lambda/B_{\min} \quad (B_{\min} = \text{shortest distance between antennas})$$

Field of view (FOV):

$$\sim \lambda/D \quad (D = \text{antenna diameter})$$

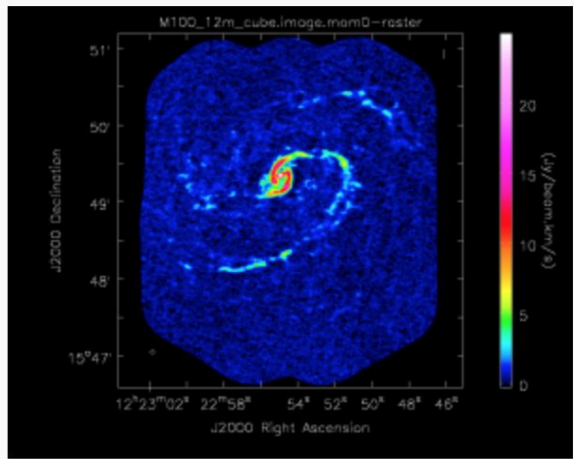
*Sources more extended than the FOV can be observed using multiple pointing centers in a mosaic

An interferometer is sensitive to a range of angular sizes: $\lambda/B_{\max} < \theta < \lambda/B_{\min}$

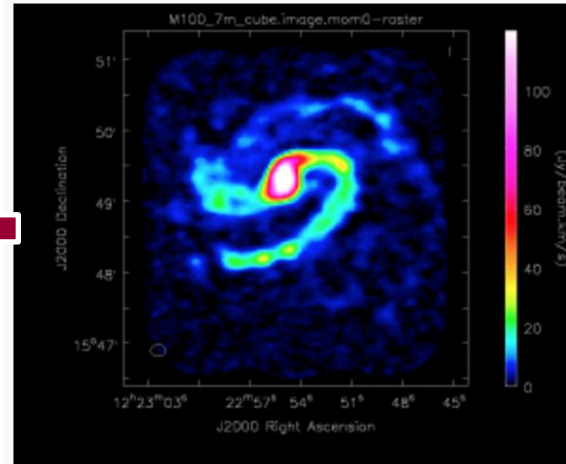


Characteristic Angular Scales: M100

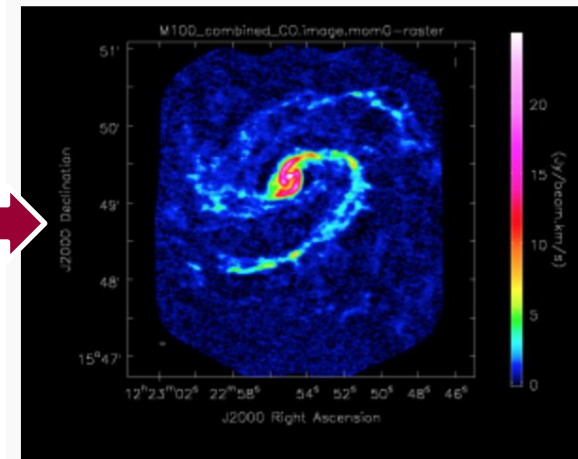
ALMA 12m



ACA 7m



Combined



ALMA 12m shows smaller spatial scales (denser, clumpier emission)
ACA 7m data shows larger spatial scales (diffuse, extended emission)

To get both — you need a combined image!

Interferometry: Spatial Scales

- The **sensitivity** is given by the number of antennas times their area.
- The **field of view** is given by the beam of a single antenna (corresponding to the resolution for a single dish telescope or the primary beam).
- The **resolution** is given by the largest distance between antennas (called the synthesized beam).
- The **largest achievable angular scale** that can be imaged is given by the shortest distance between antennas.



Angular Scales — A Proposal Tip!

Interferometers act as spatial filters - shorter baselines are sensitive to larger targets, so remember ...

Spatial scales larger than the smallest baseline cannot be imaged.

Spatial scales smaller than the largest baseline cannot be resolved.

Table A-1: Angular Resolutions (AR) and Maximum Recoverable Scales (MRS) for the Cycle 8 configurations

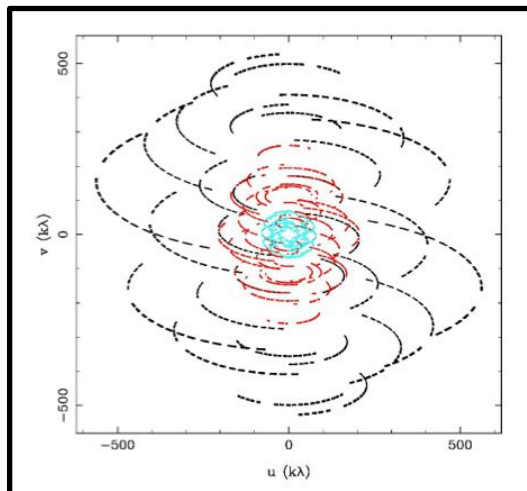
Config	Lmax		Band 3	Band 4	Band 5	Band 6	Band 7	Band 8	Band 9	Band 10
	Lmin		100 GHz	150 GHz	185 GHz	230 GHz	345 GHz	460 GHz	650 GHz	870 GHz
7-m	45 m	AR	12.5"	8.4"	6.8"	5.5"	3.6"	2.7"	1.9"	1.4"
	9 m	MRS	66.7"	44.5"	36.1"	29.0"	19.3"	14.5"	10.3"	7.7"
C-1	161 m	AR	3.4"	2.3"	1.8"	1.5"	1.0"	0.74"	0.52"	0.39"
	15 m	MRS	28.5"	19.0"	15.4"	12.4"	8.3"	6.2"	4.4"	3.3"
C-2	314 m	AR	2.3"	1.5"	1.2"	1.0"	0.67"	0.50"	0.35"	0.26"
	15 m	MRS	22.6"	15.0"	12.2"	9.8"	6.5"	4.9"	3.5"	2.6"
C-3	500 m	AR	1.4"	0.94"	0.77"	0.62"	0.41"	0.31"	0.22"	0.16"
	15 m	MRS	16.2"	10.8"	8.7"	7.0"	4.7"	3.5"	2.5"	1.9"
C-4	784 m	AR	0.92"	0.61"	0.50"	0.40"	0.27"	0.20"	0.14"	0.11"
	15 m	MRS	11.2"	7.5"	6.1"	4.9"	3.3"	2.4"	1.7"	1.3"
C-5	1.4 km	AR	0.54"	0.36"	0.30"	0.24"	0.16"	0.12"	0.084"	0.063"
	15 m	MRS	6.7"	4.5"	3.6"	2.9"	1.9"	1.5"	1.0"	0.77"
C-6	2.5 km	AR	0.31"	0.20"	0.17"	0.13"	0.089"	0.067"	0.047"	0.035"
	15 m	MRS	4.1"	2.7"	2.2"	1.8"	1.2"	0.89"	0.63"	0.47"
C-7	3.6 km	AR	0.21"	0.14"	0.11"	0.092"	0.061"	0.046"	0.033"	0.024"
	64 m	MRS	2.6"	1.7"	1.4"	1.1"	0.75"	0.56"	0.40"	0.30"
C-8	8.5 km	AR	0.096"	0.064"	0.052"	0.042"	0.028"	N/A	N/A	N/A
	110 m	MRS	1.4"	0.95"	0.77"	0.62"	0.41"	N/A	N/A	N/A

From the ALMA Cycle 6 Proposal Guide



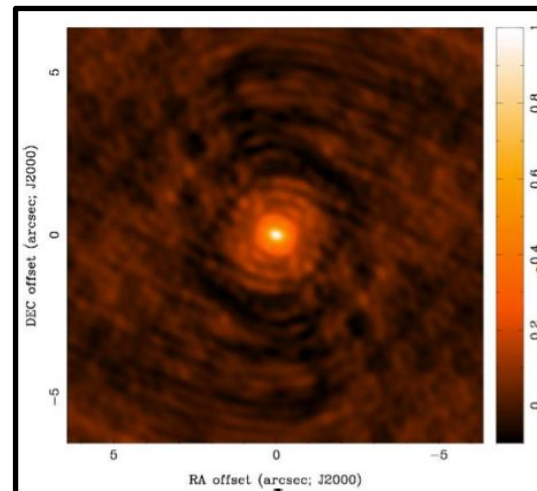
The Dirty Beam

$S(u,v)$

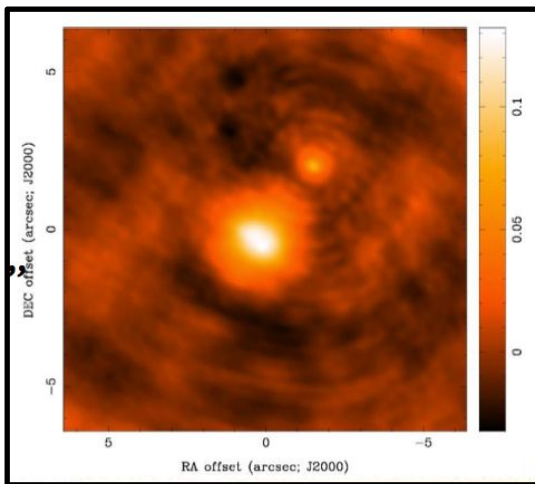


FT
→

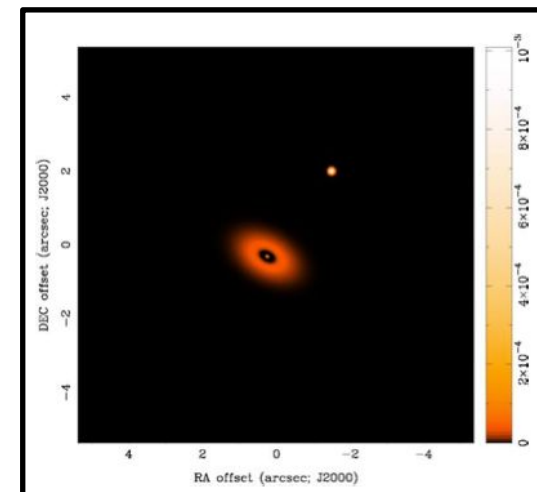
$s(x,y)$
“Dirty Beam”



* (Convolution)



←

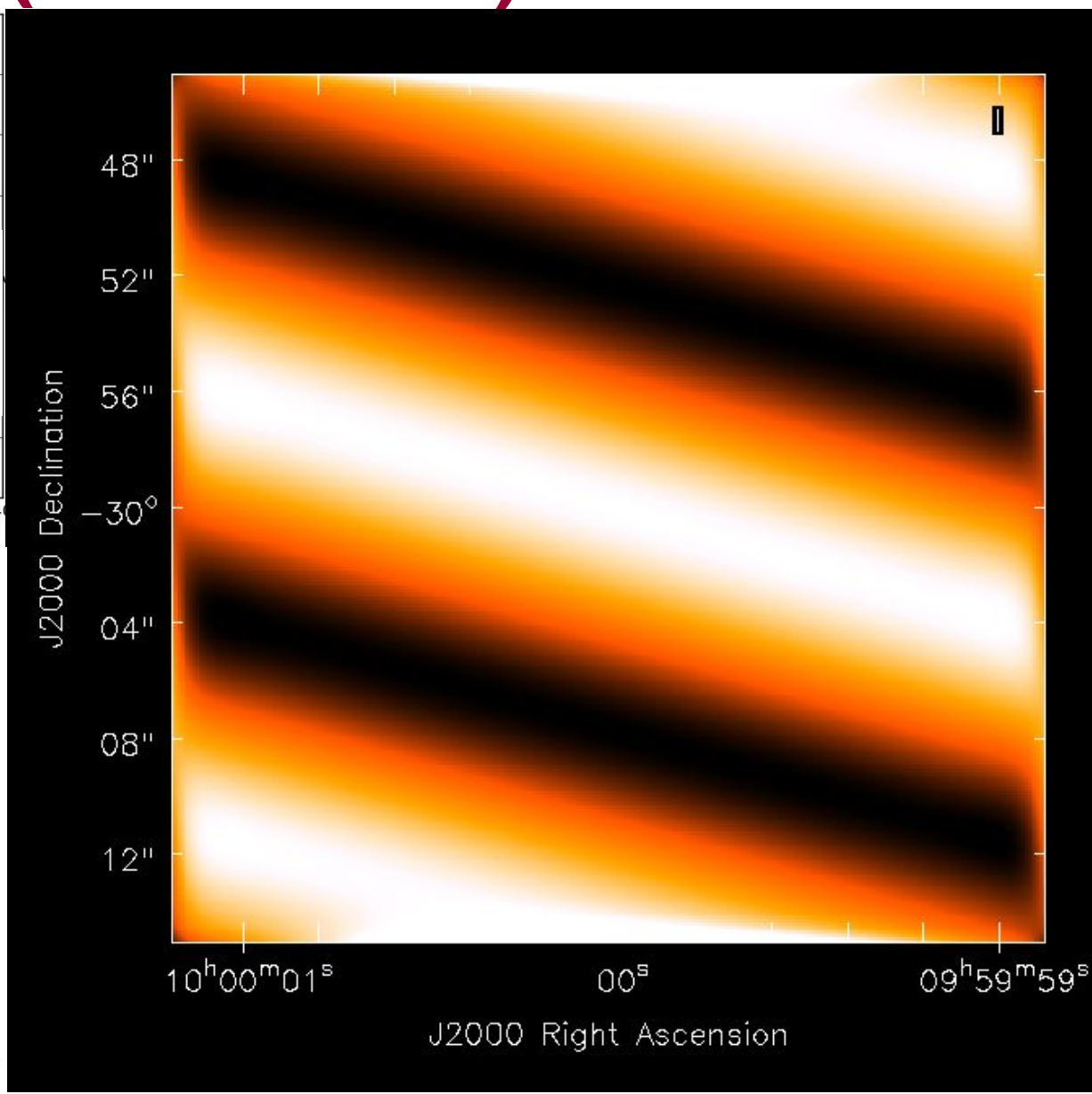
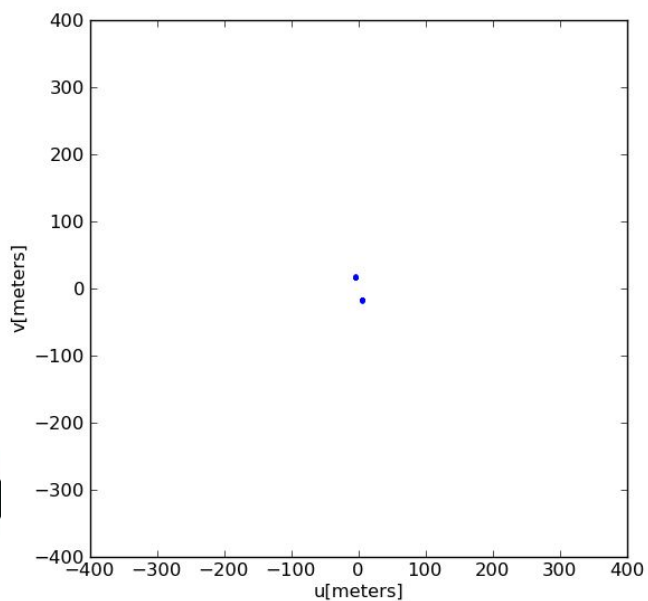
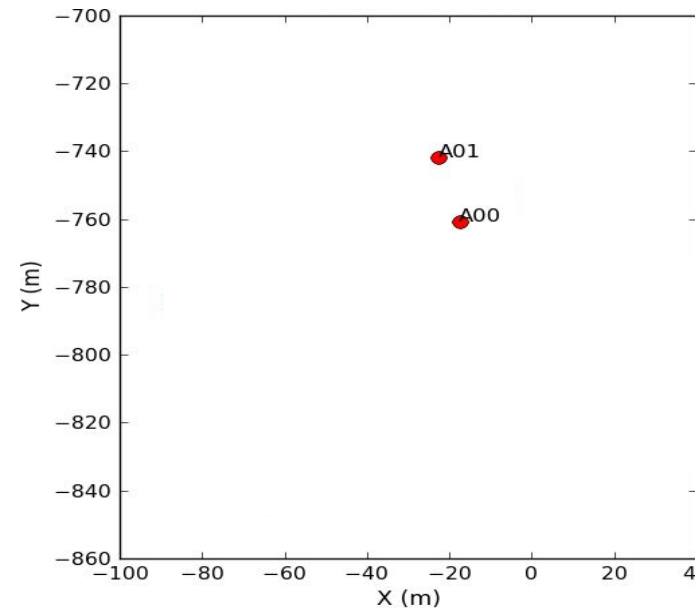


$T_D(x,y)$ “Dirty Image”

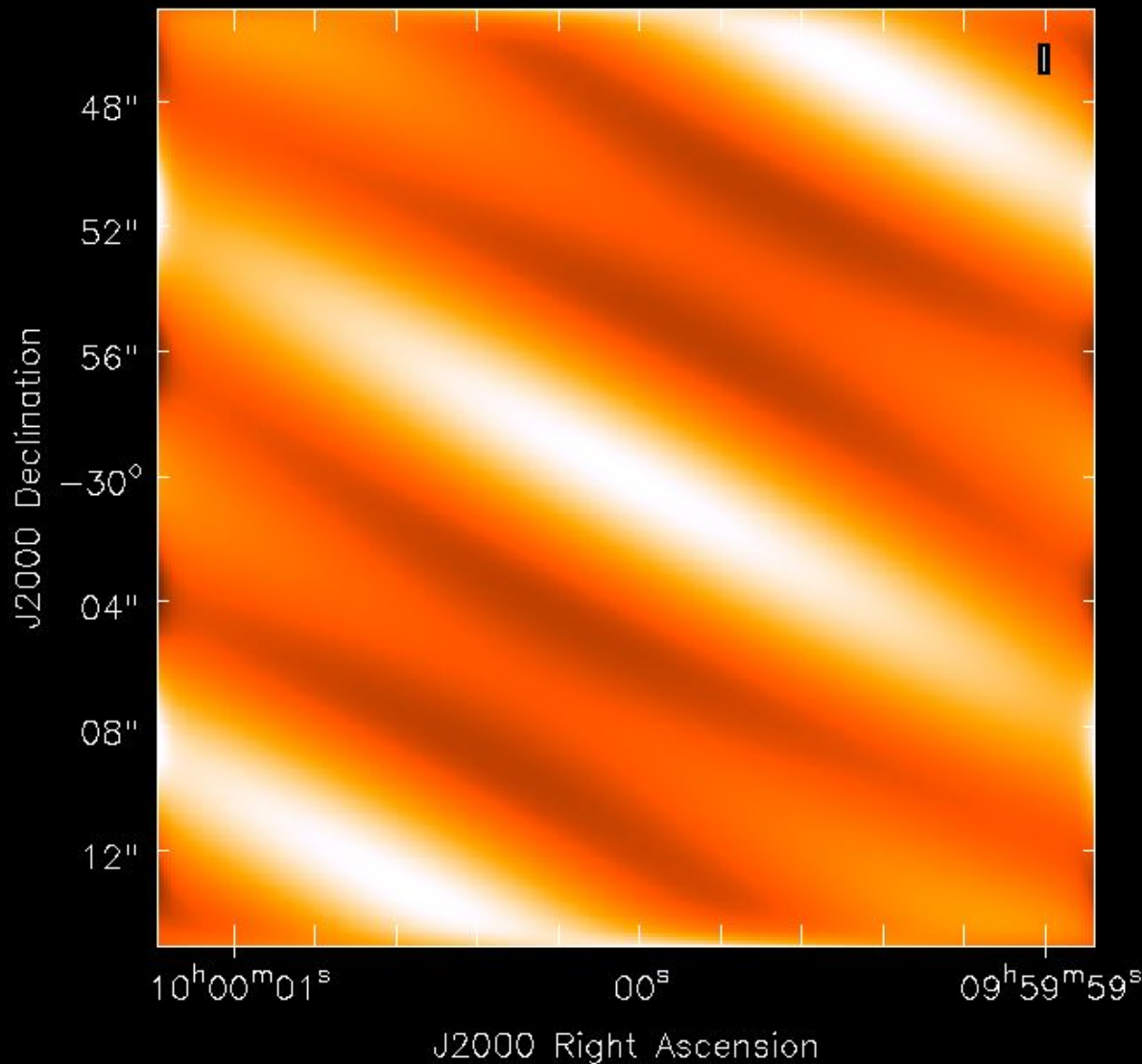
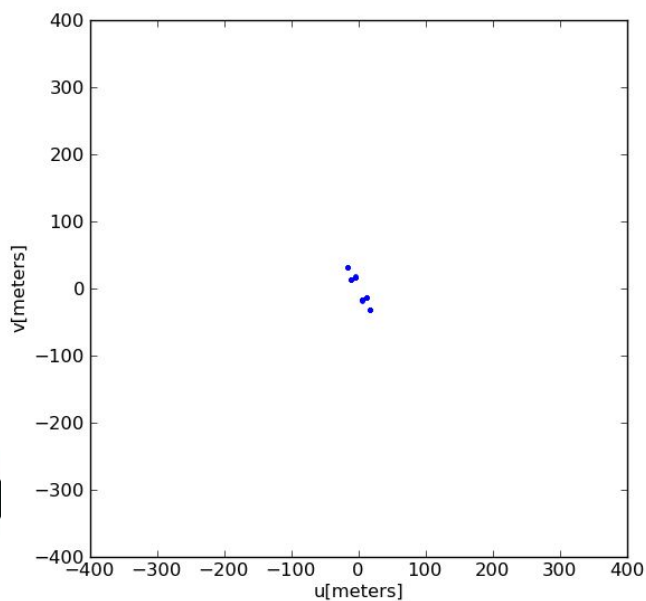
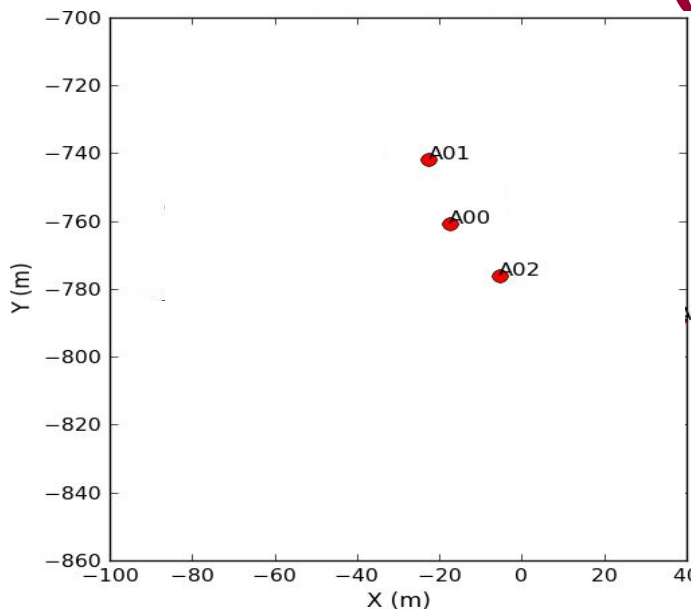
$T(x,y)$



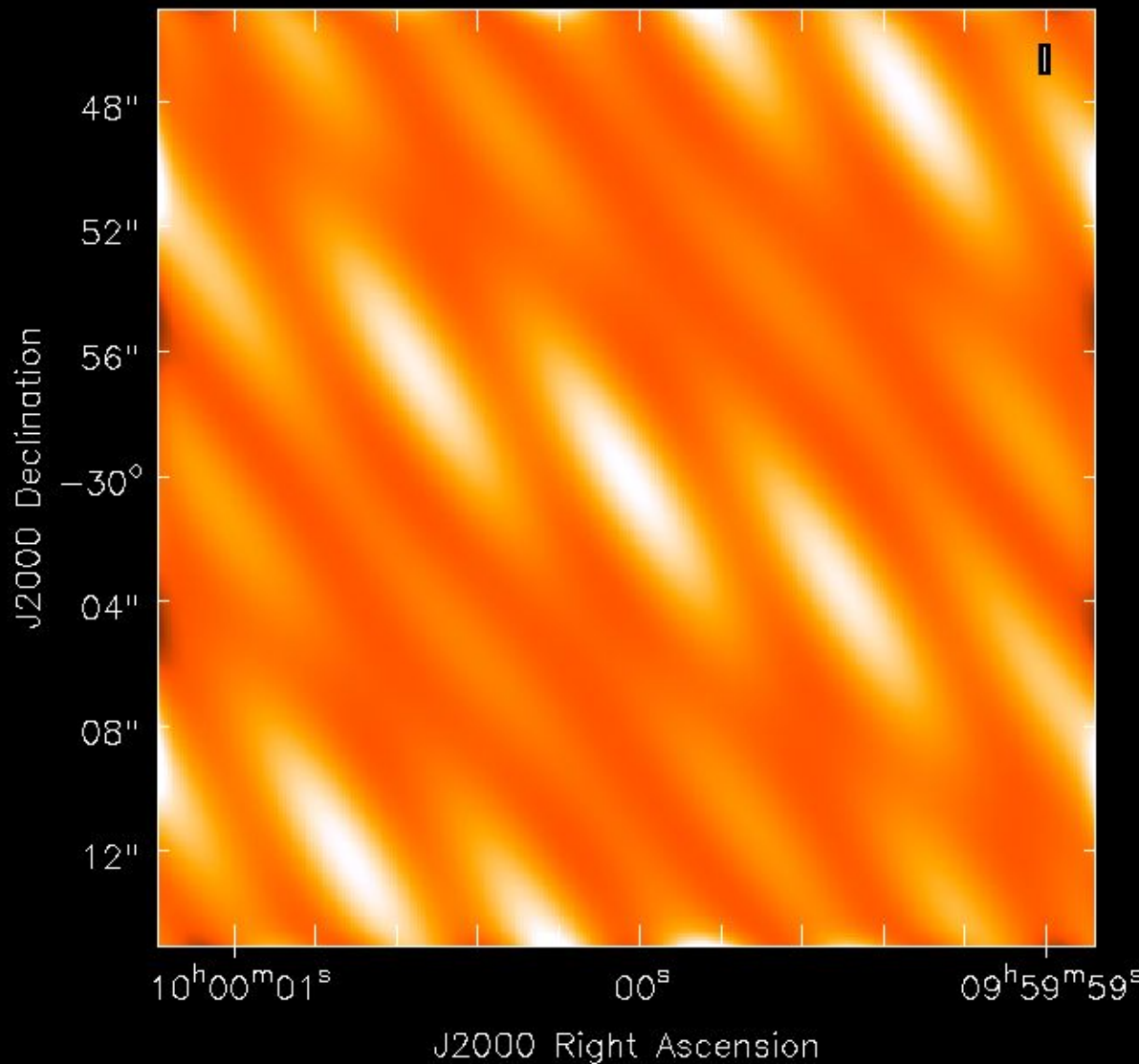
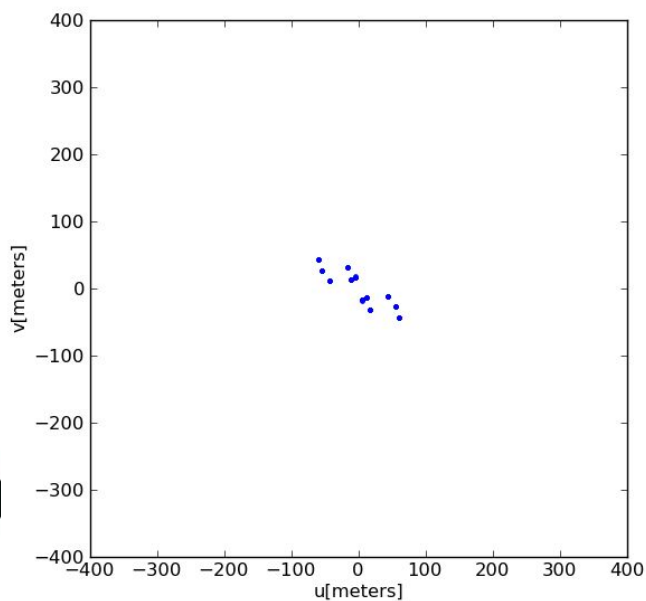
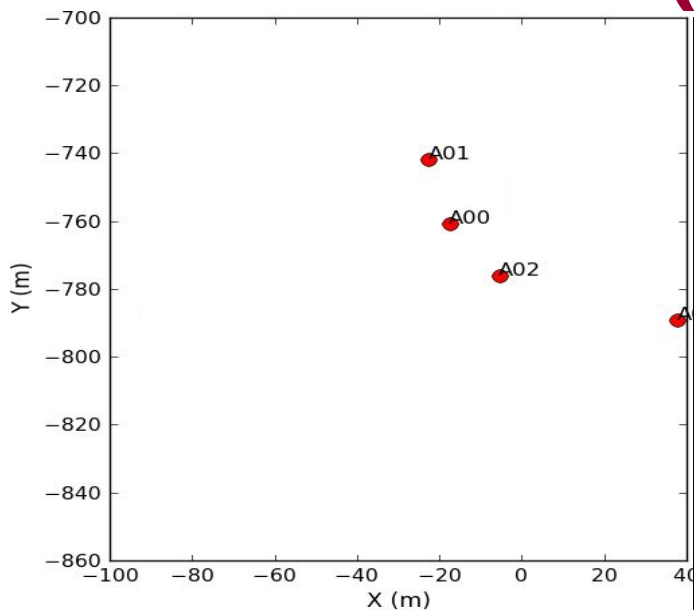
Example: Fringe pattern with 2 Antennas (one baseline)



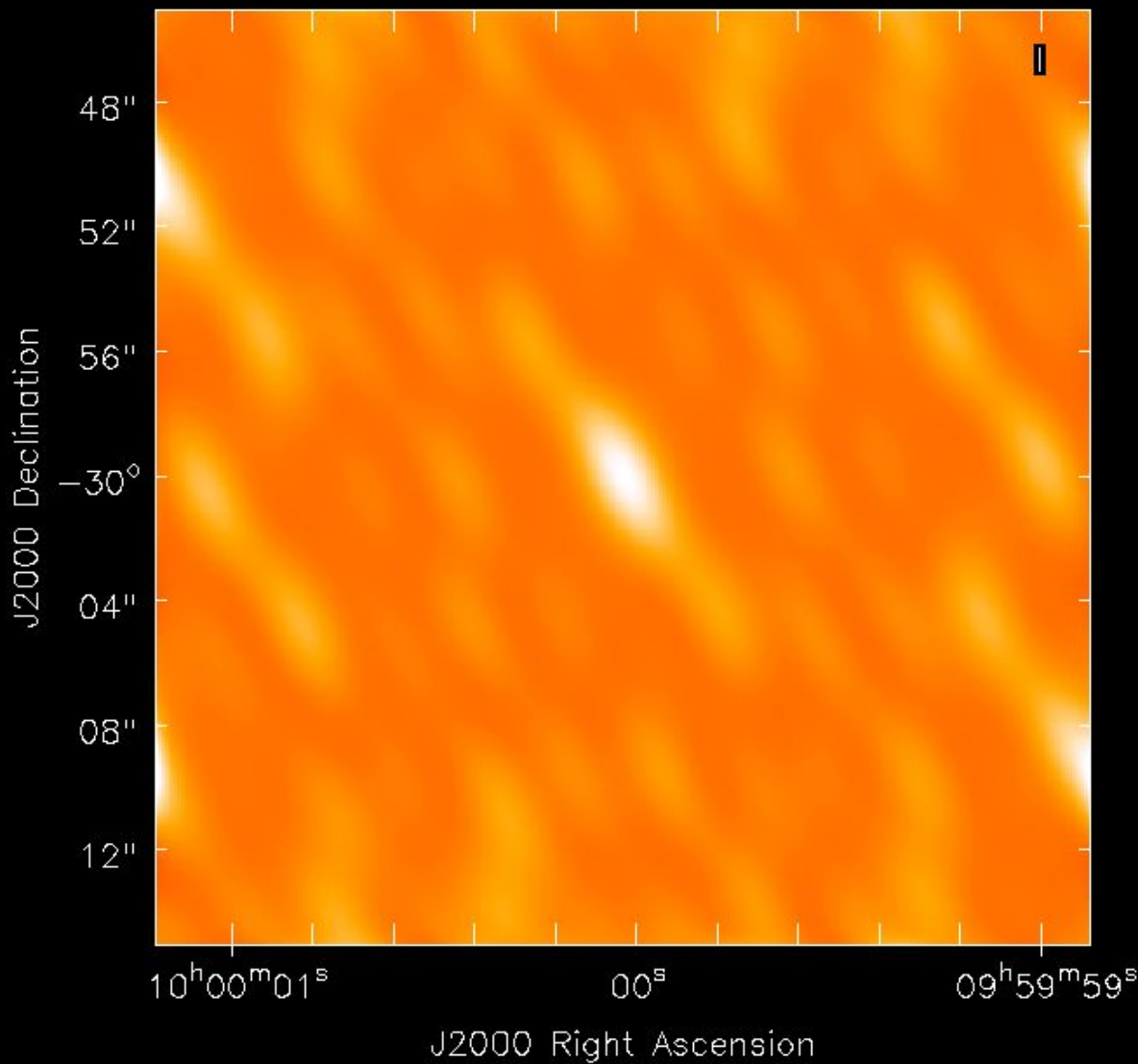
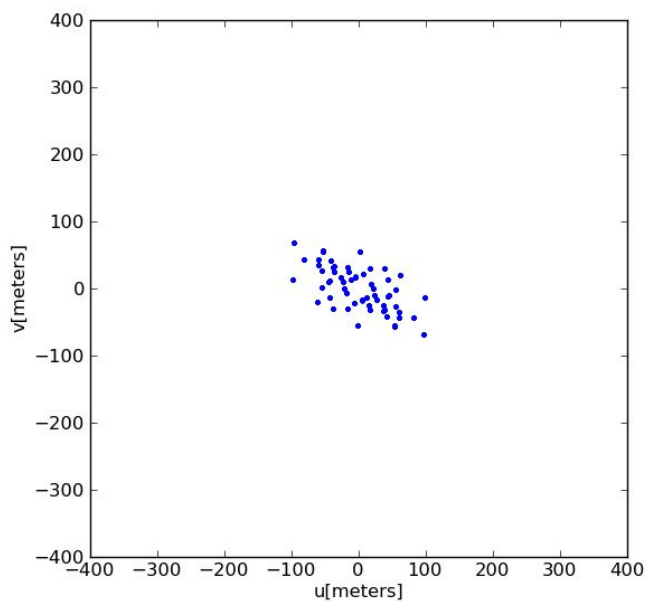
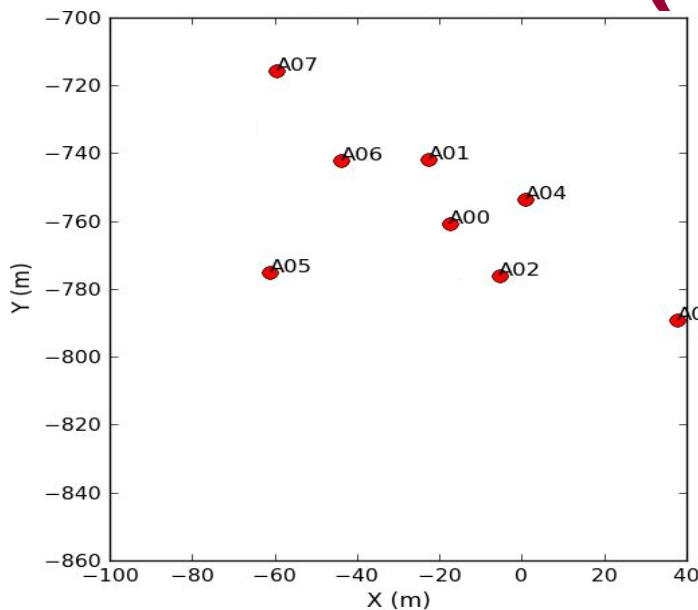
Example: Fringe pattern with 3 Antennas (3 baselines)



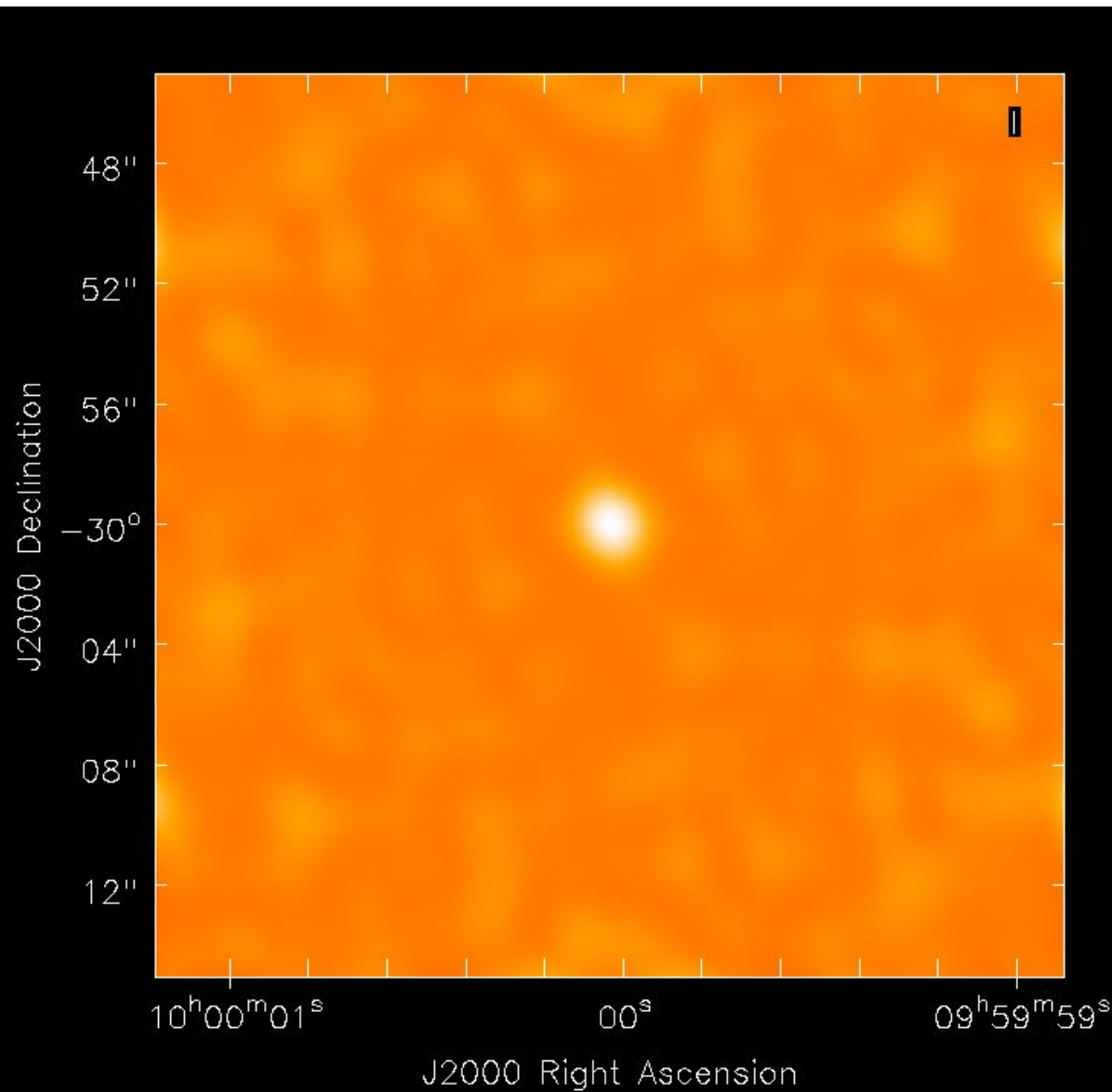
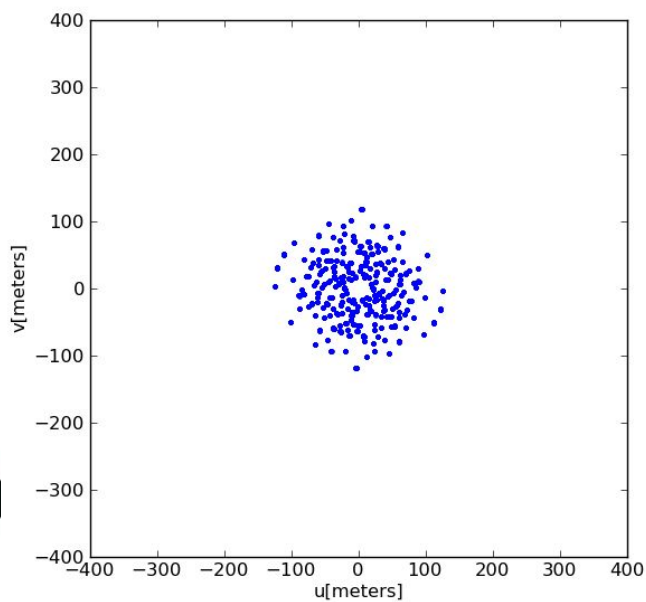
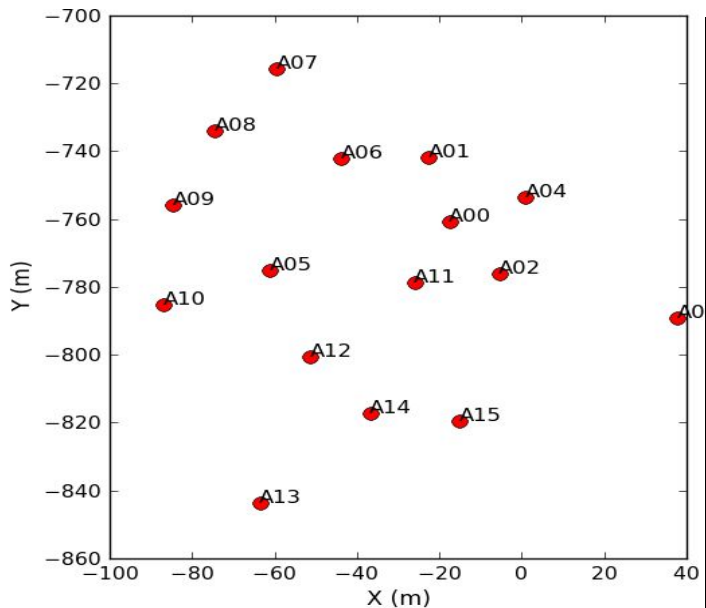
Example: Fringe pattern with 4 Antennas (6 baselines)



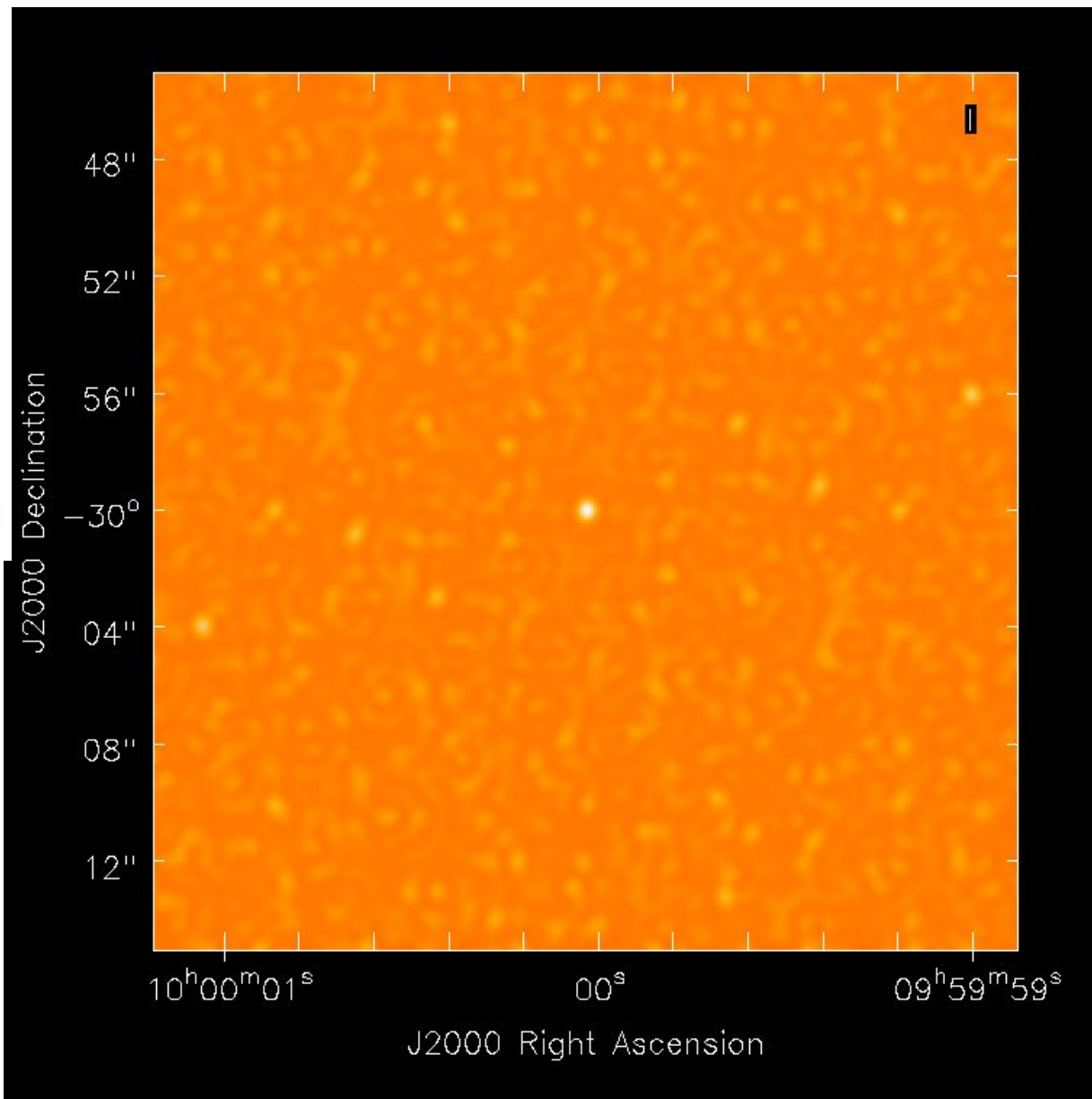
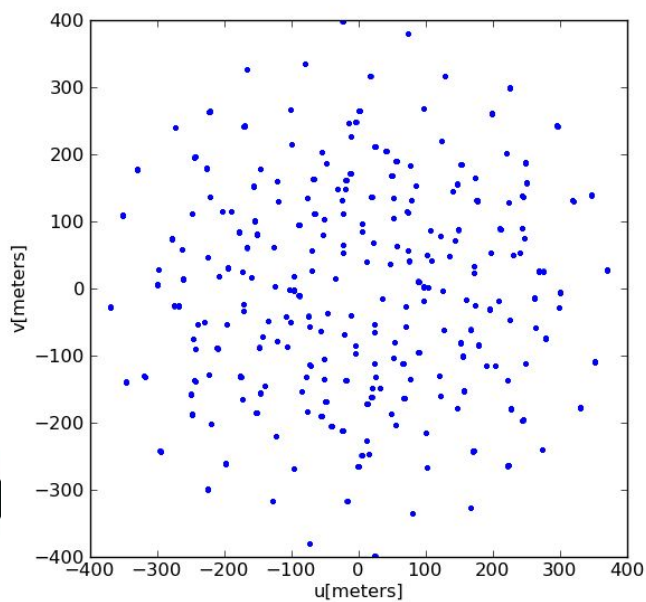
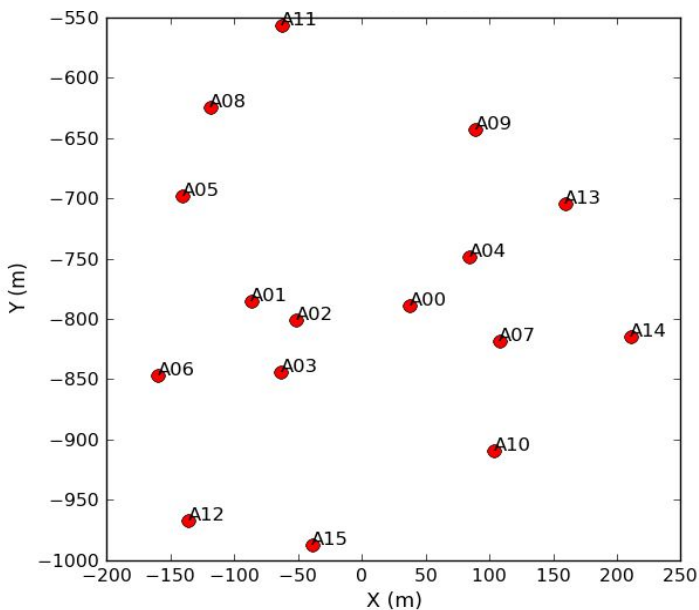
Example: Fringe pattern with 8 Antennas (28 baselines)



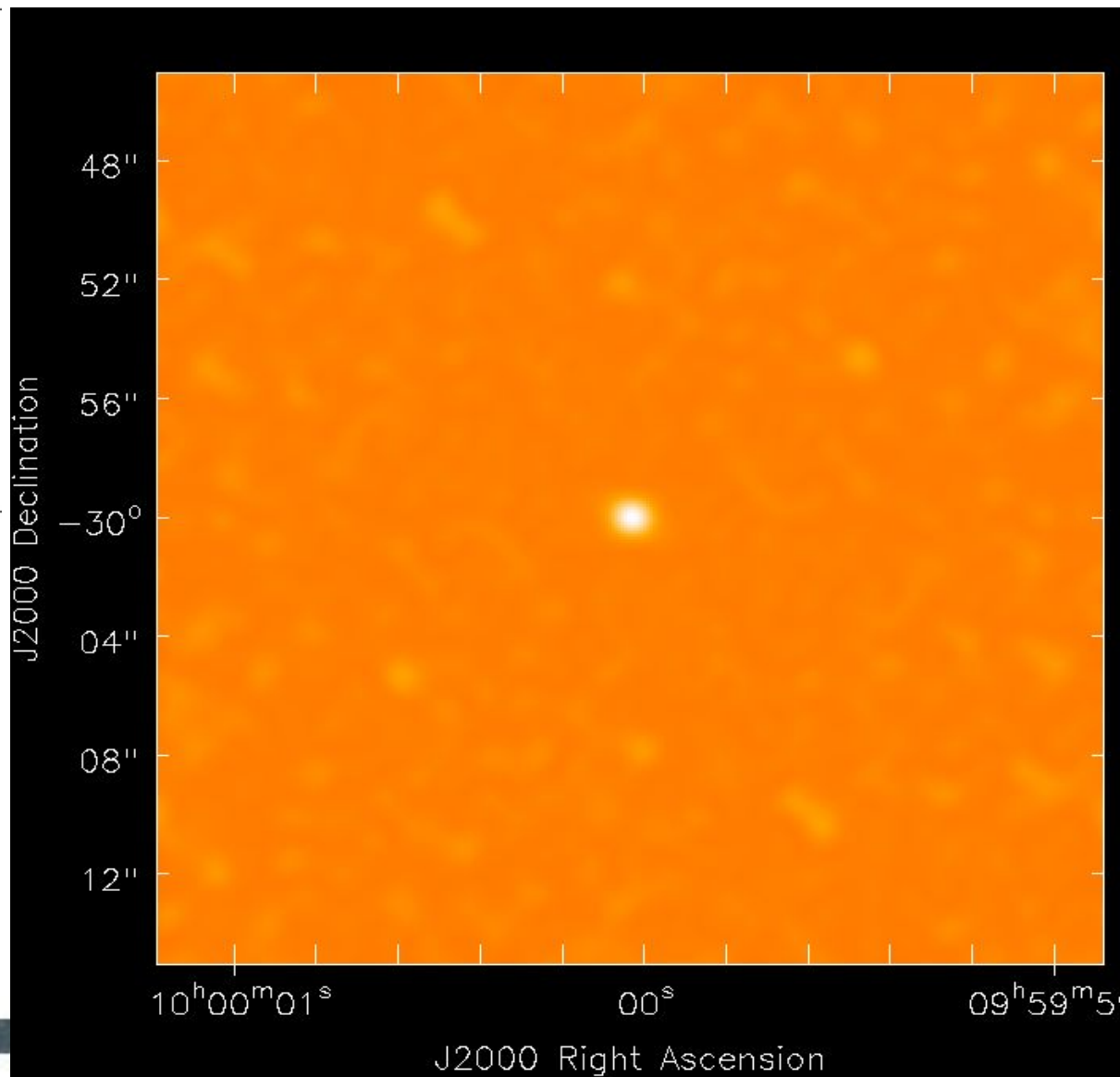
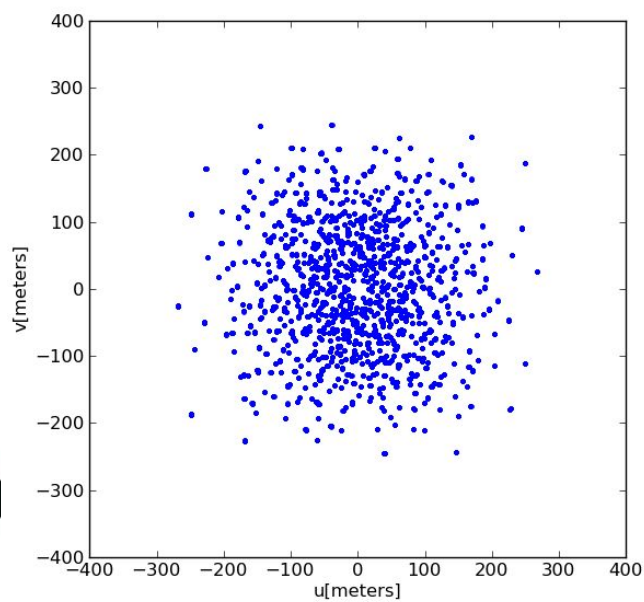
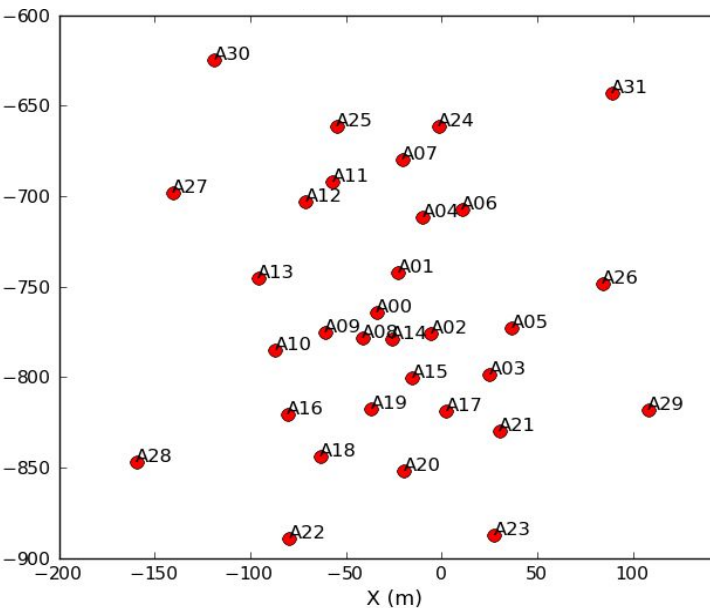
16 Antennas – Compact Configuration



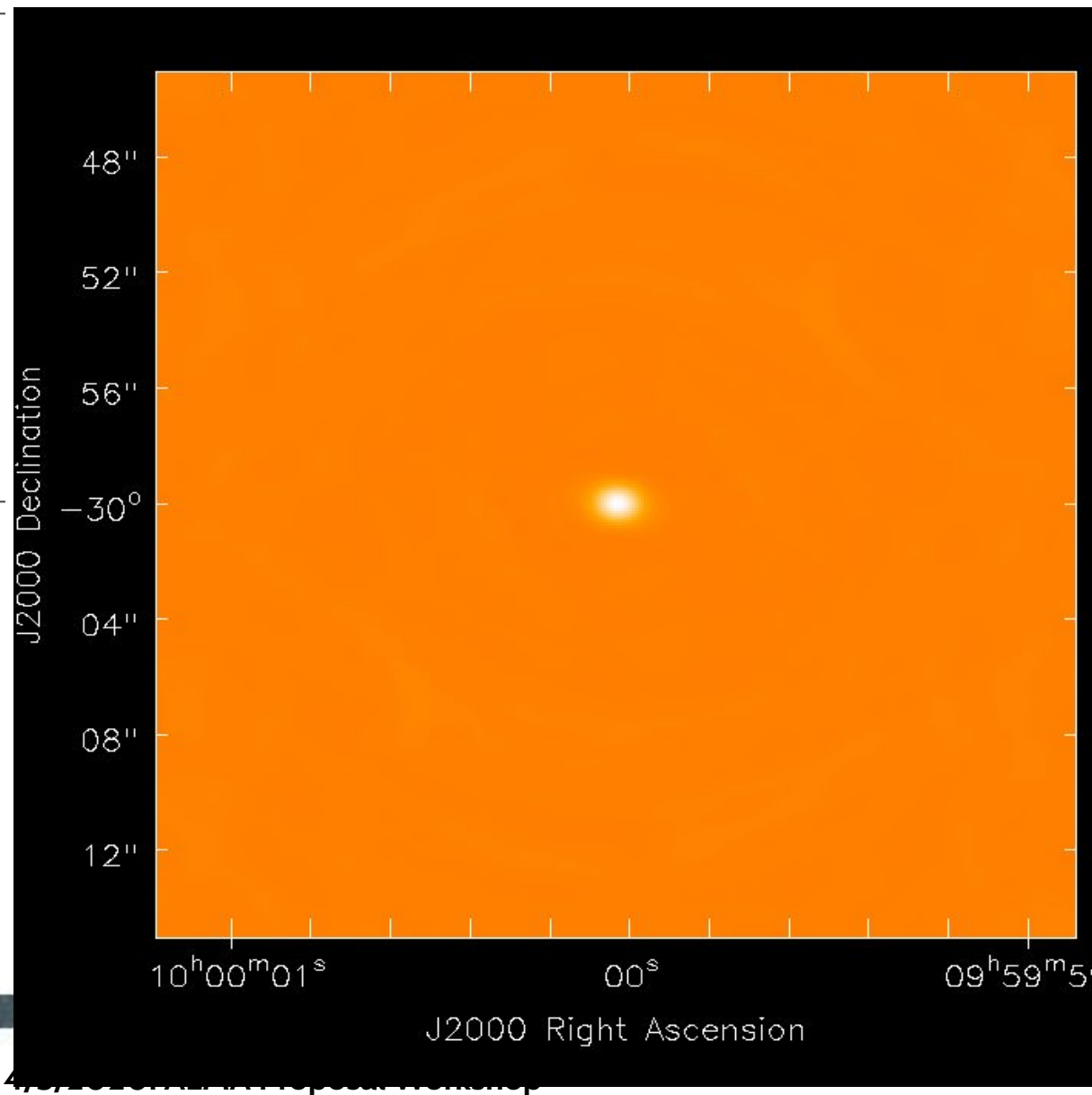
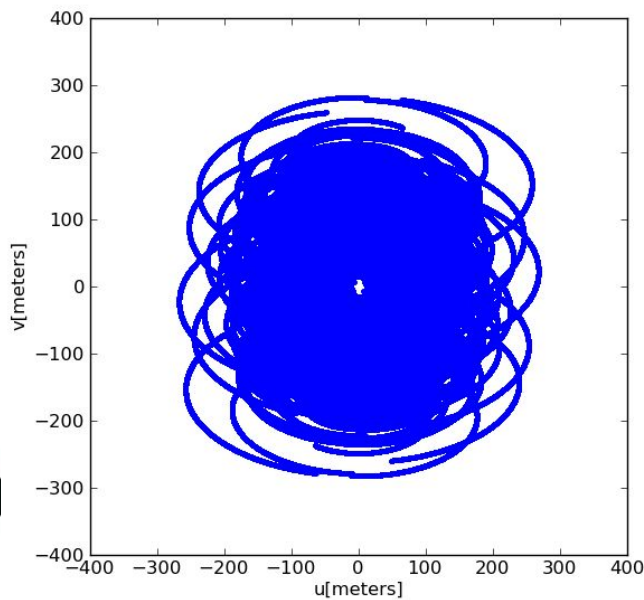
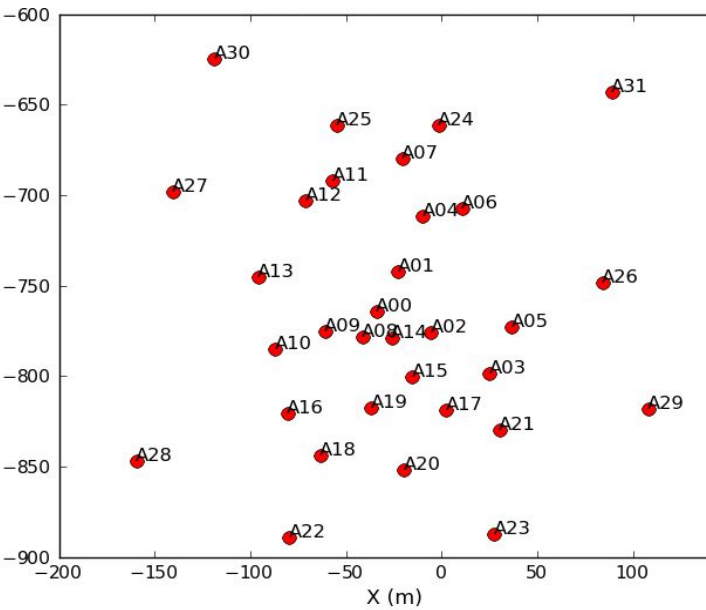
16 Antennas – Extended Configuration



32 Antennas – Instantaneous



32 Antennas – 8 hours



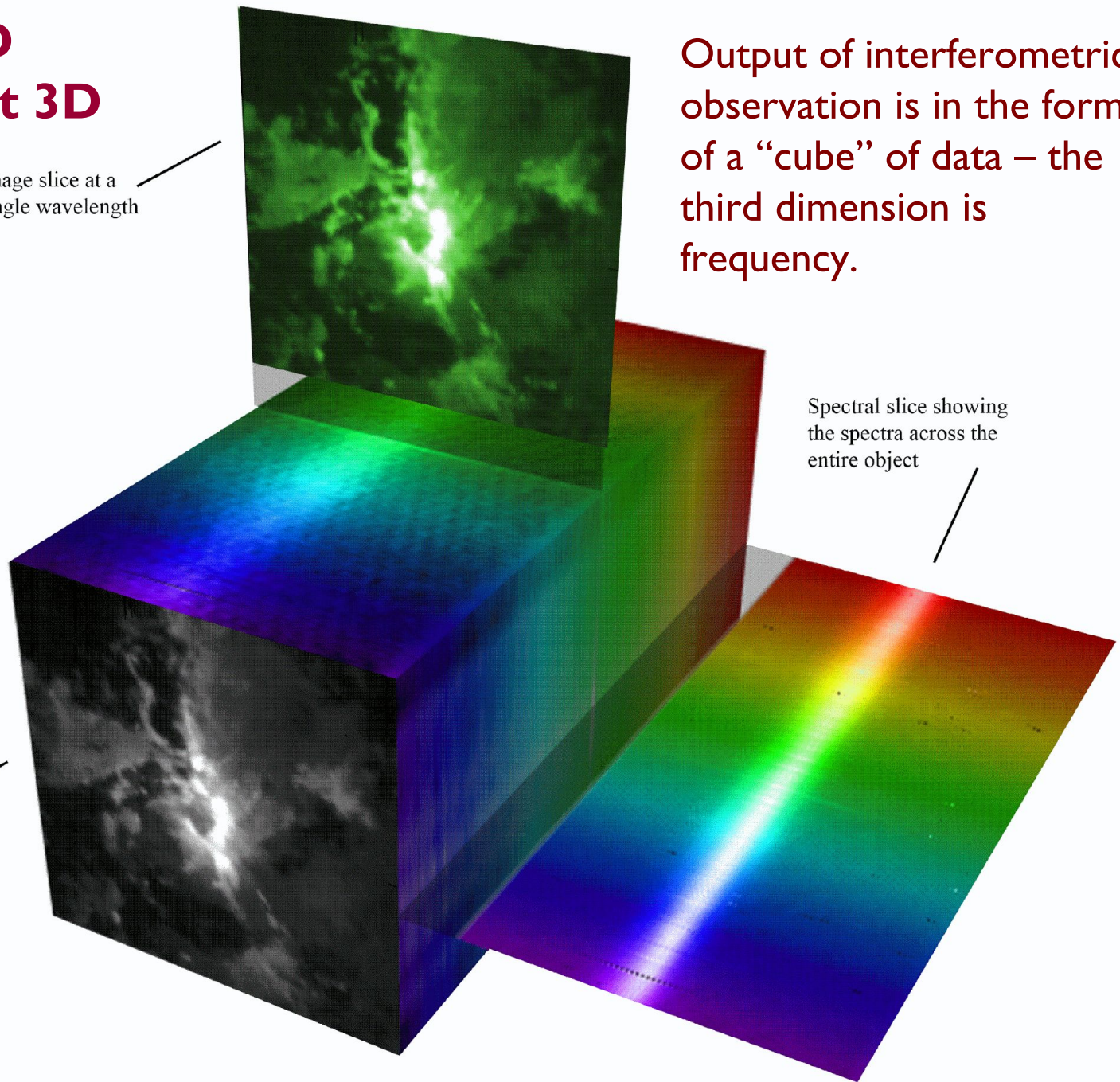
Not only 2D imaging, but 3D

Output of interferometric
observation is in the form
of a “cube” of data – the
third dimension is
frequency.

Image slice at a
single wavelength

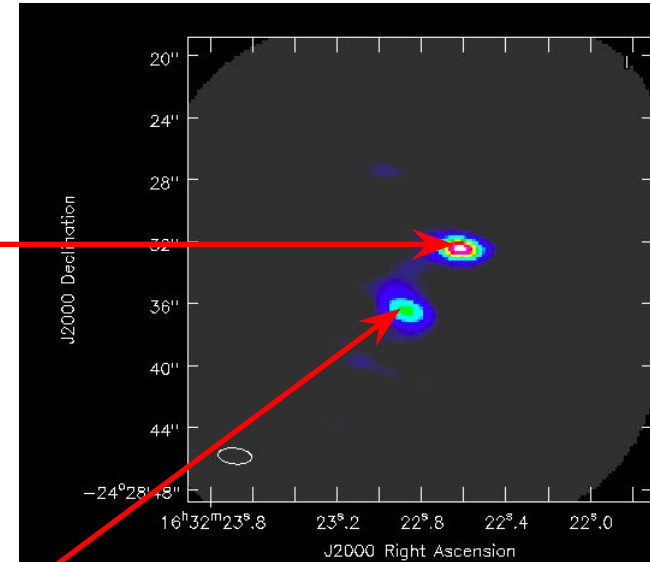
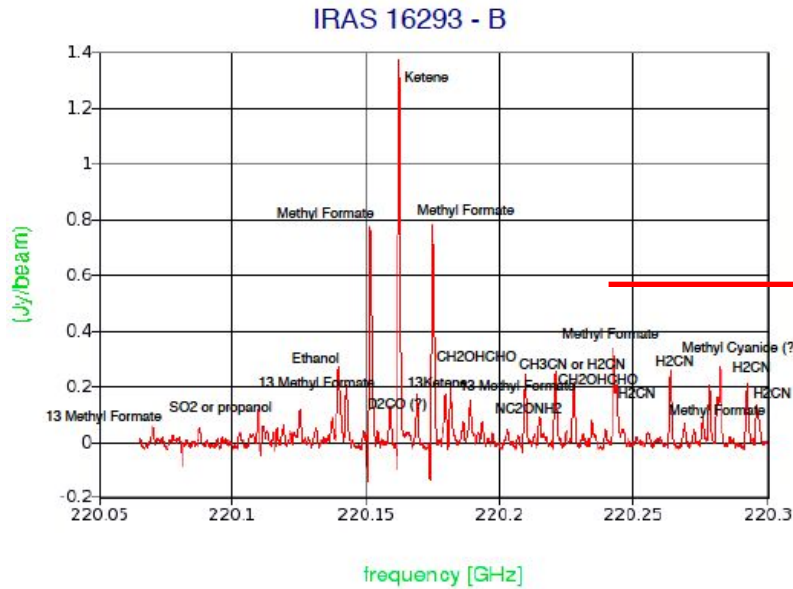
Spectral slice showing
the spectra across the
entire object

Object seen in
combined light



Sometimes the most interesting science lies in the third dimension

Band 6



J. Turner & ALMA CSV team

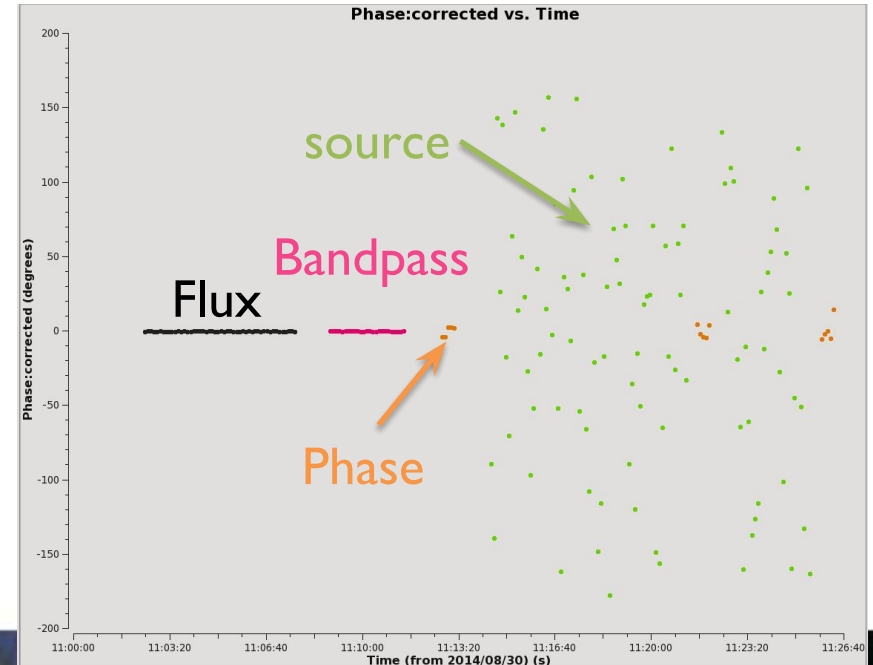
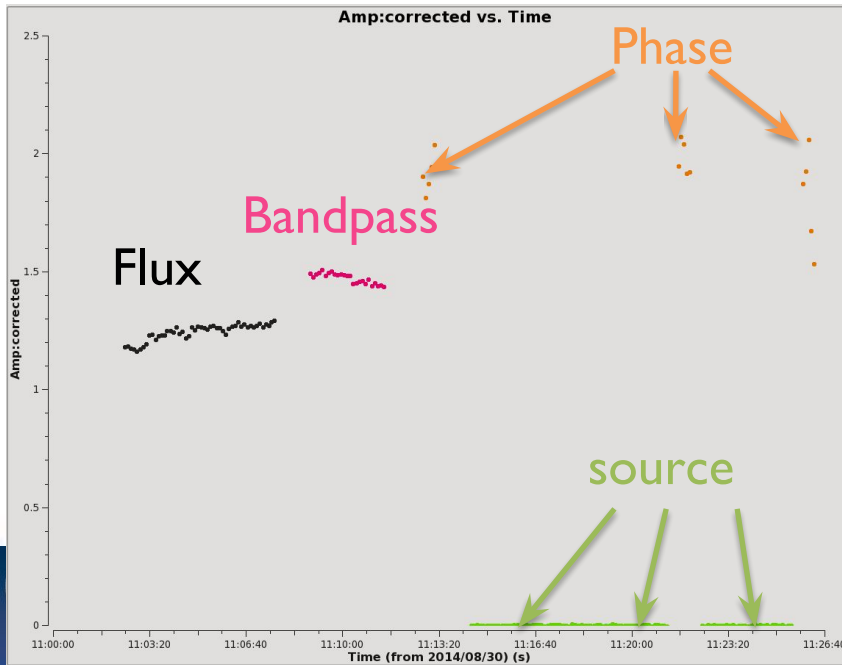
Young Low Mass Stars: IRAS 16293

- Note narrow lines toward pre-protostellar core B (top) with infall apparent in methyl formate and ketene lines.



A Brief Word on Calibration

- Interferometers measure visibilities, i.e., the amplitude and phase of the cross-correlated signals between pairs of antennas, as a function of time and frequency.
- We calibrate these data by determining the complex gains (amplitude and phase), the frequency response (bandpass) and flux scale for each antenna.



Calibration Process

Calibration is the effort to measure and remove the time-dependent and frequency-dependent atmospheric and instrumental variations.

Steps in calibrating interferometric data:

(Note: You don't have to worry about these in your observational set up!)

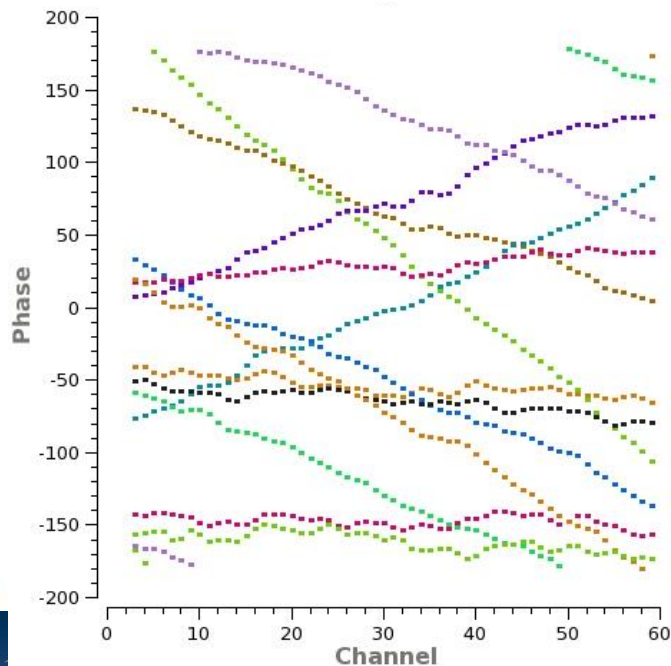
- Bandpass calibration (correct frequency-dependent telescope response)
- Phase and amplitude gain calibration (remove effects of atmospheric water vapor and correct time-varying phases/amplitudes)
- Set absolute flux scale



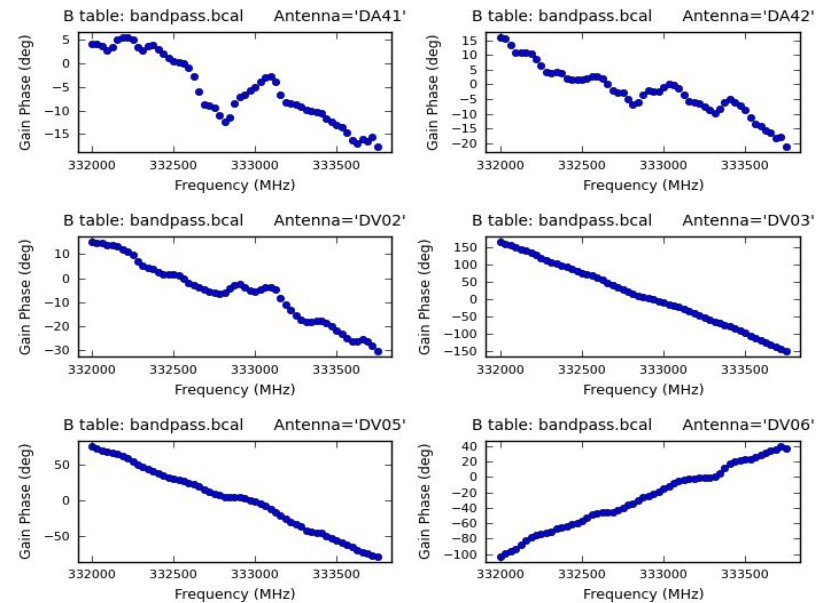
Bandpass Calibration: Phase

- * Analogous to optical “flat fielding” + bias subtraction for each antenna.
- * Primarily correcting for frequency dependent telescope response (i.e. in the correlator/spectral windows)
- * Done once in an SB, uses bright point sources like quasars
- * Typically, baseline responses are inverted to antenna-based correction

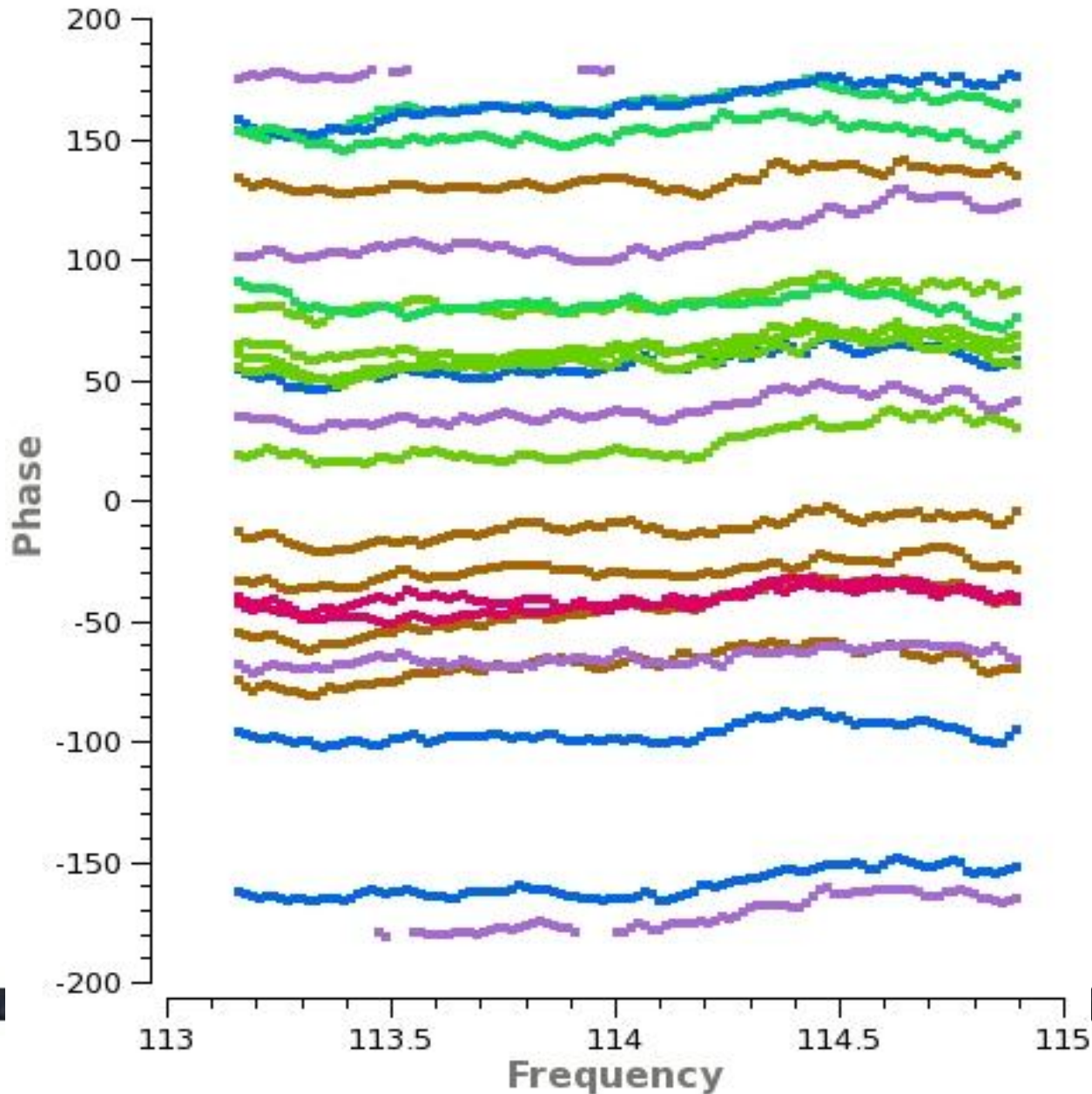
Baselines to one antenna



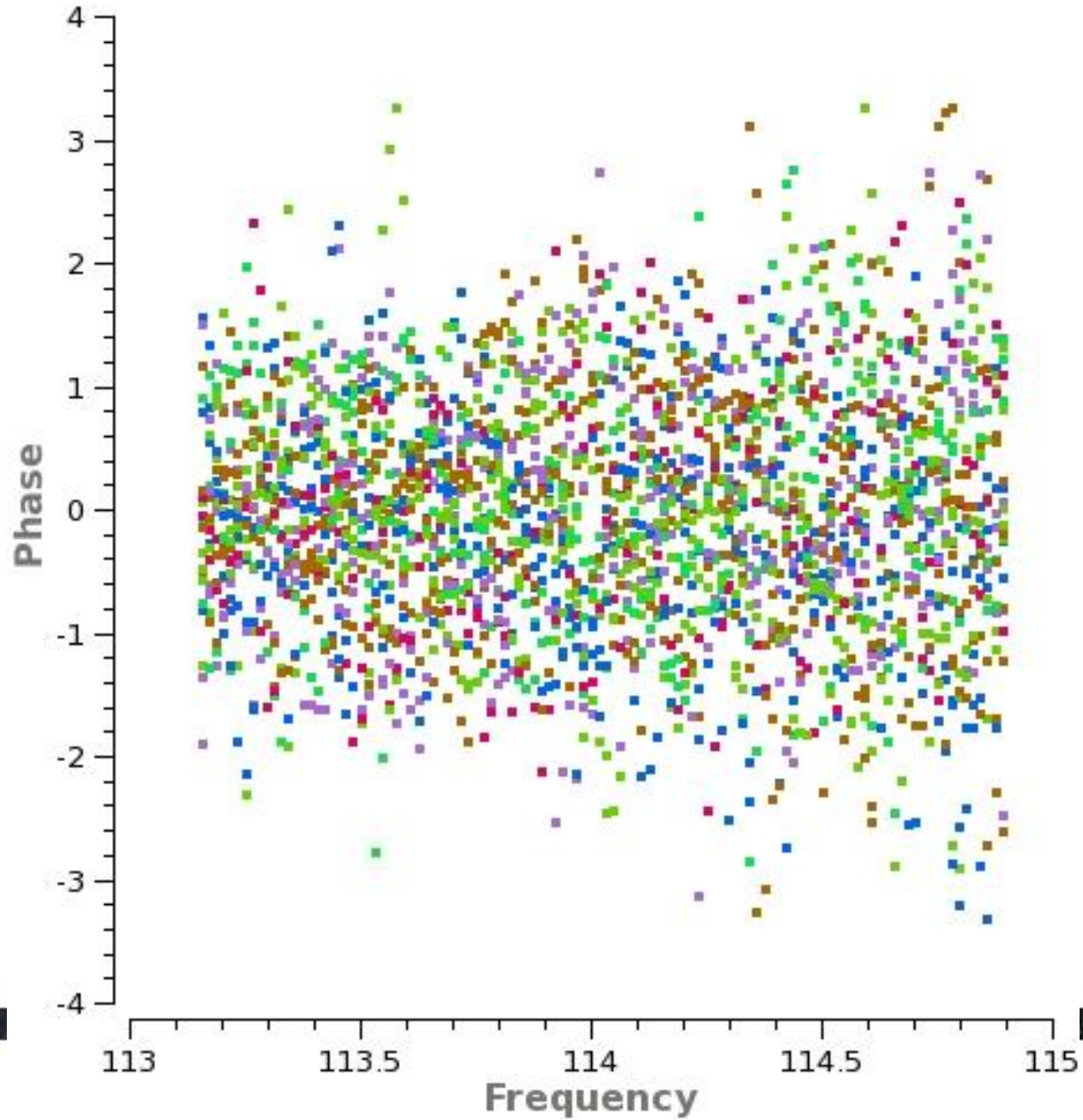
Antenna-based Bandpass Solutions



Bandpass Phase vs. Frequency (Before)

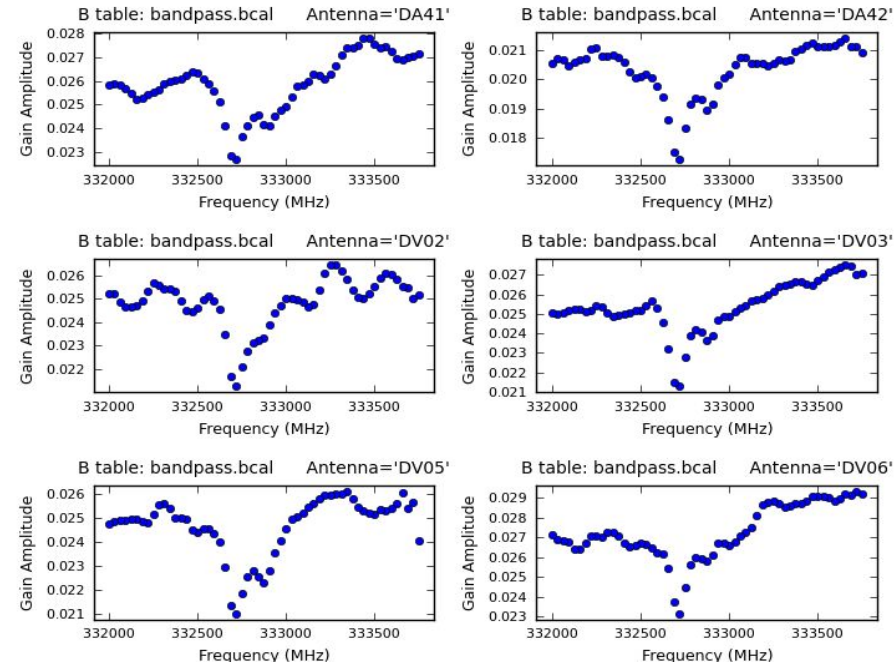
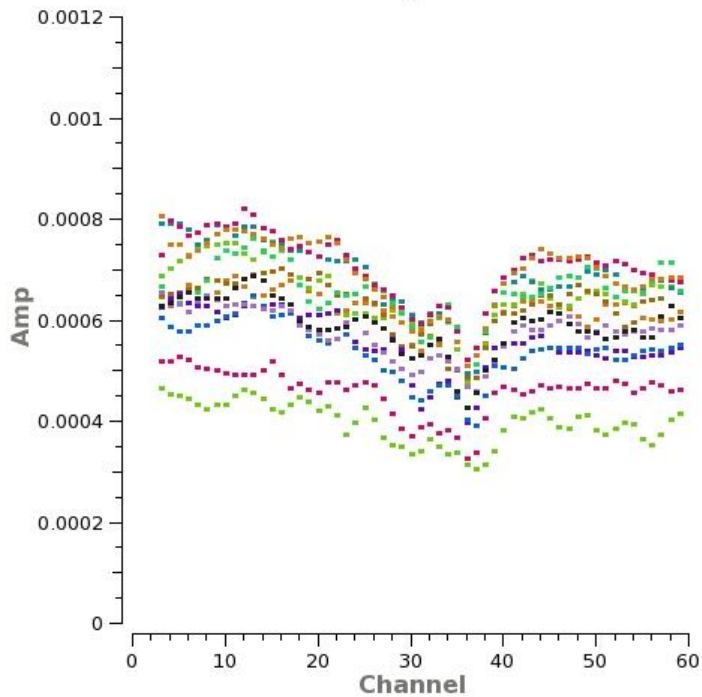


Bandpass Phase vs. Frequency (After)



Bandpass Calibration: Amplitude

Baselines to one antenna



Amplitude Before Bandpass Calibration

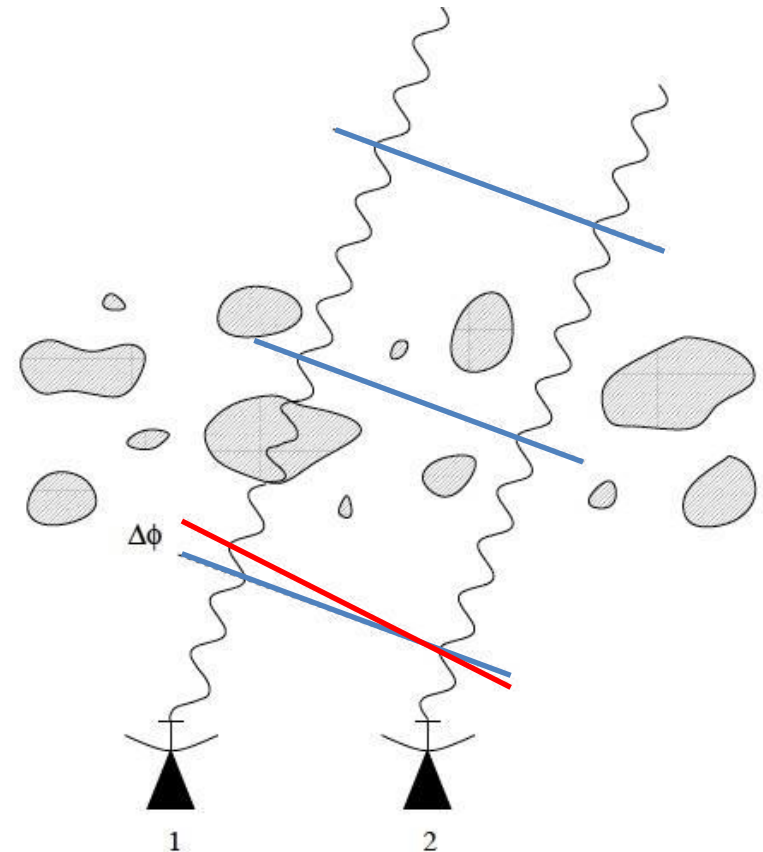
Bandpass solutions for individual antennas



Atmospheric Phase Correction

- Variations in the amount of precipitable water vapor cause phase fluctuations that result in:
 - Low coherence (loss of sensitivity)
 - Radio “seeing” of 1 arcsec at 1 mm
 - Anomalous pointing offsets
 - Anomalous delay offsets

Patches of air with different water vapor content (and hence index of refraction) affect the incoming wave front differently.

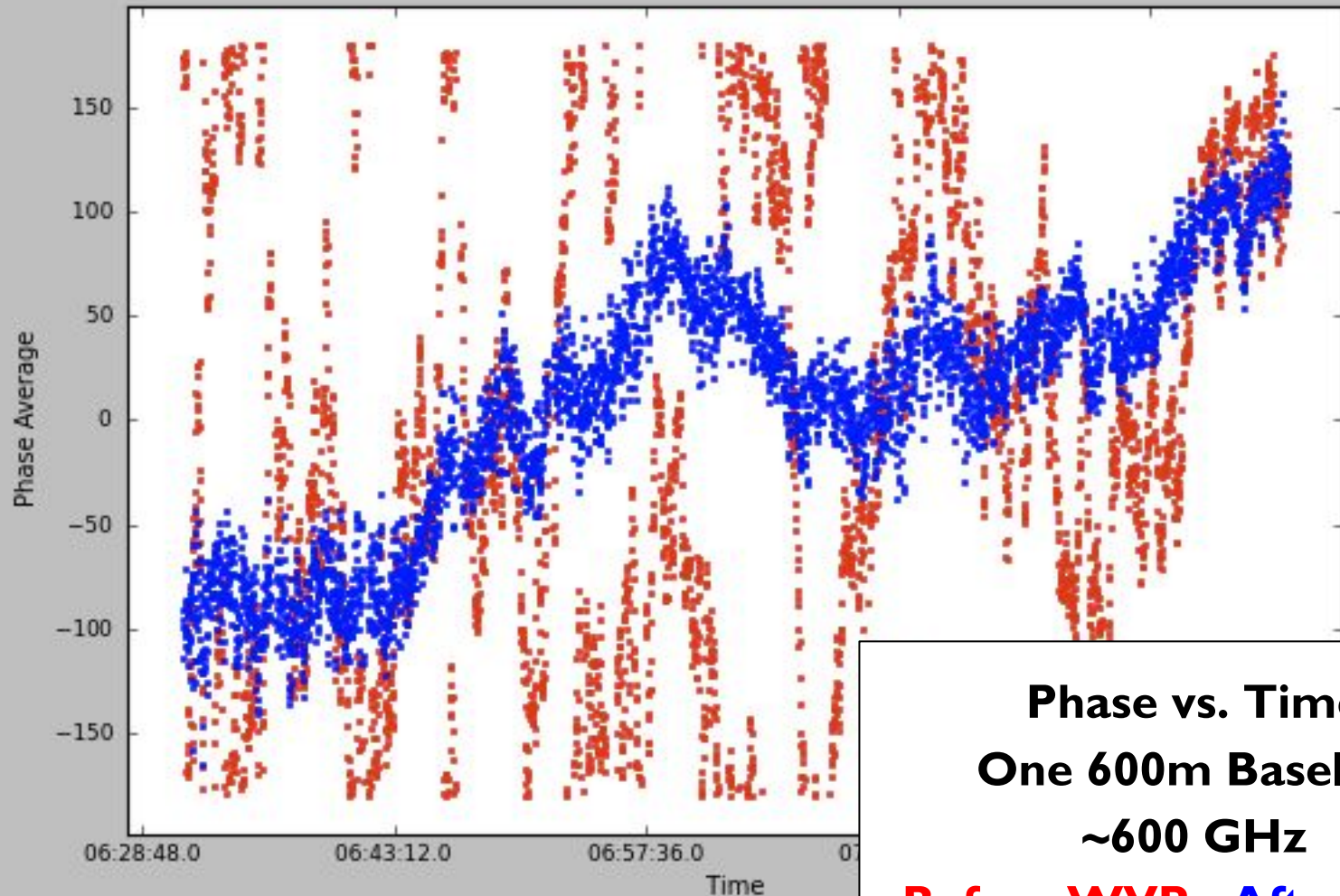


Phase & Amplitude Gain Calibration

Determines the variations of phase and amplitude over time

- First pass is atmospheric correction from Water Vapor Radiometers readings.
- Final correction from gain calibrator (point source near to target) that is observed every few minutes throughout the observation (analogous to repeat trips to a standard star).

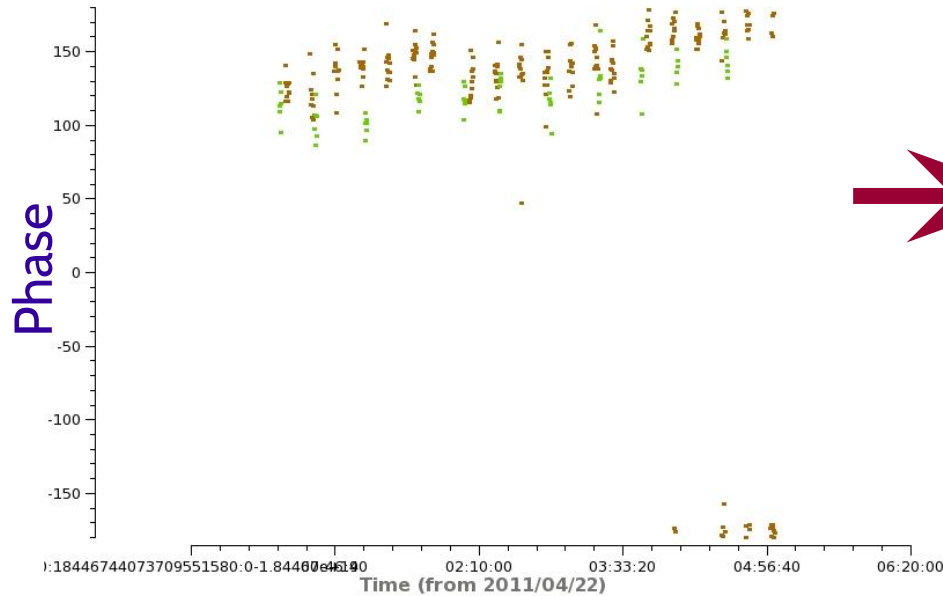
Water Vapor Correction on ALMA



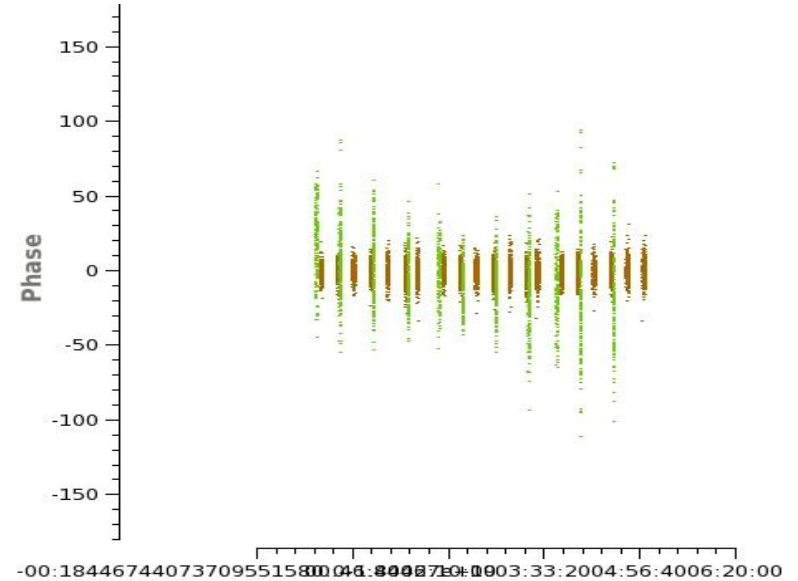
Phase vs. Time
One 600m Baseline
~600 GHz
Before WVR, After WVR

Phase Calibration

The phase calibrator must be a point source close to the science target and must be observed frequently. This provides a model of atmospheric phase change along the line of sight to the science target that can be compensated for in the data.



Time



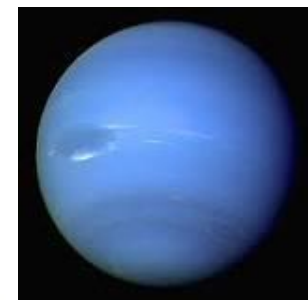
Corrected using point source model

Flux (or Amplitude) Calibration

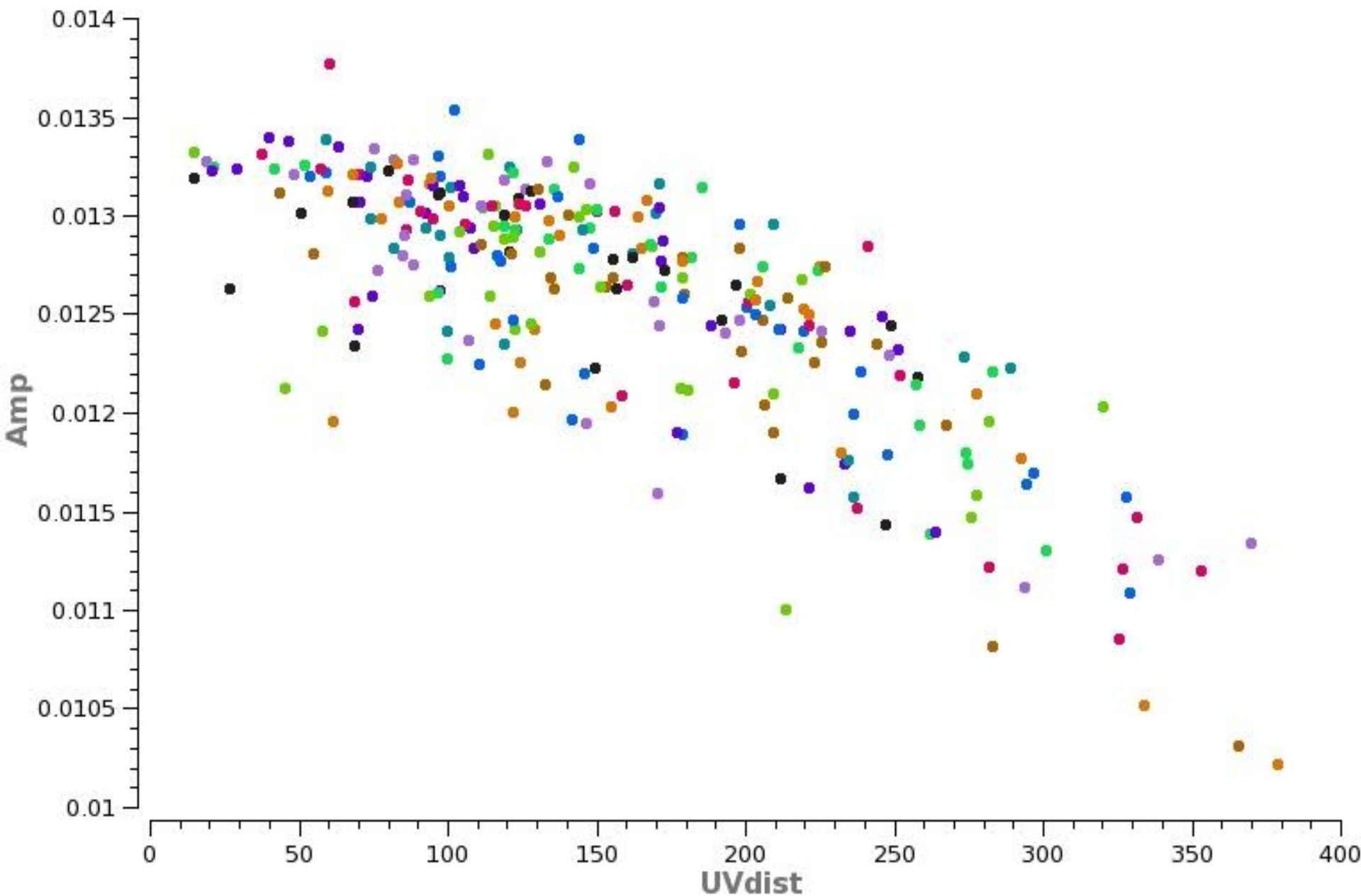
Two Steps:

1. Use calibration devices with known temperatures (hotload and ambient load) to measure System Temperature frequently.
2. Use a source of known flux to convert the signal measured at the antenna to common unit (Janskys). If the source is resolved, or has spectral lines, it must be modeled very well.

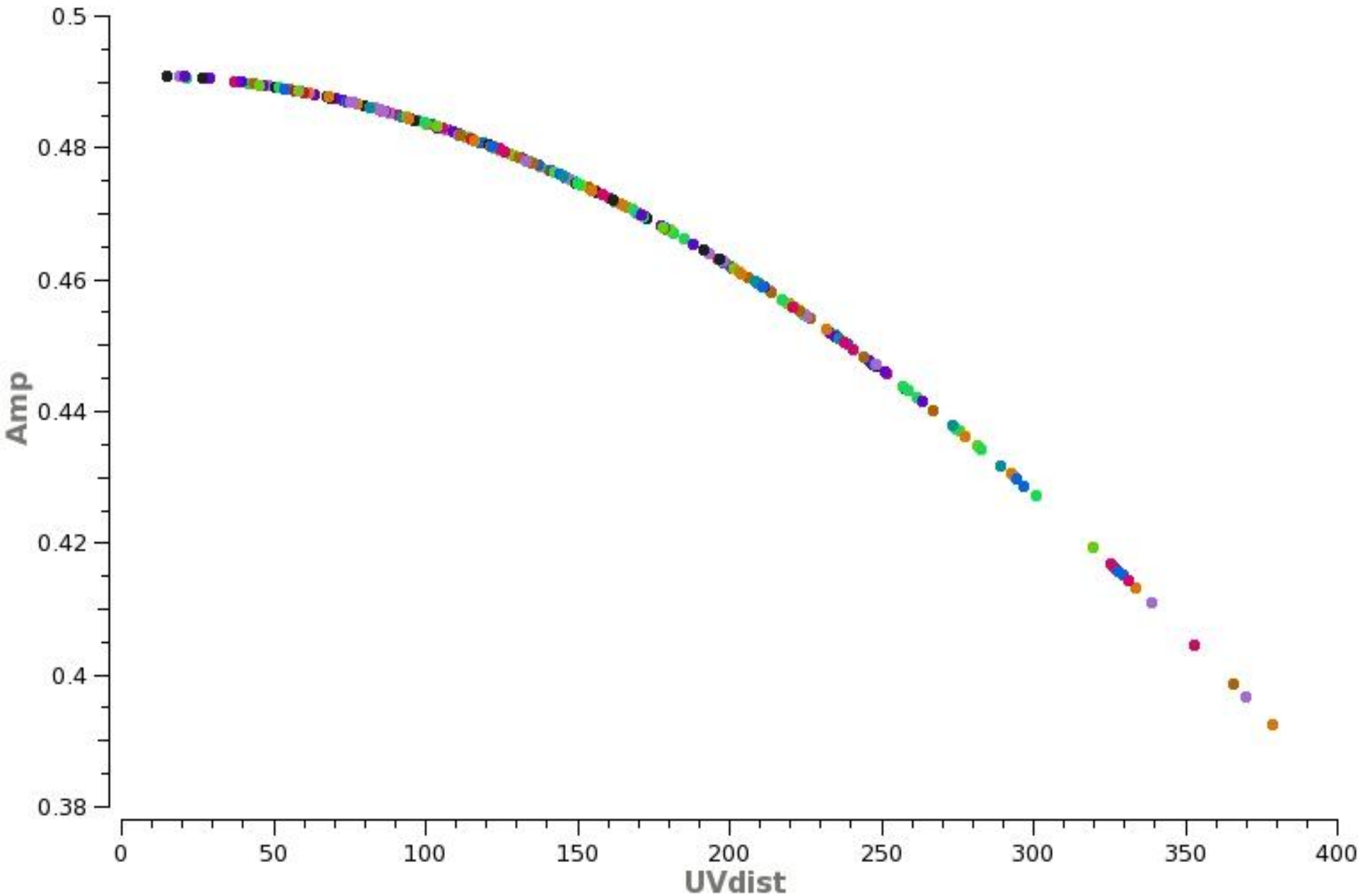
The derived amplitude vs. time corrections for the flux calibrator are then applied to the science target.



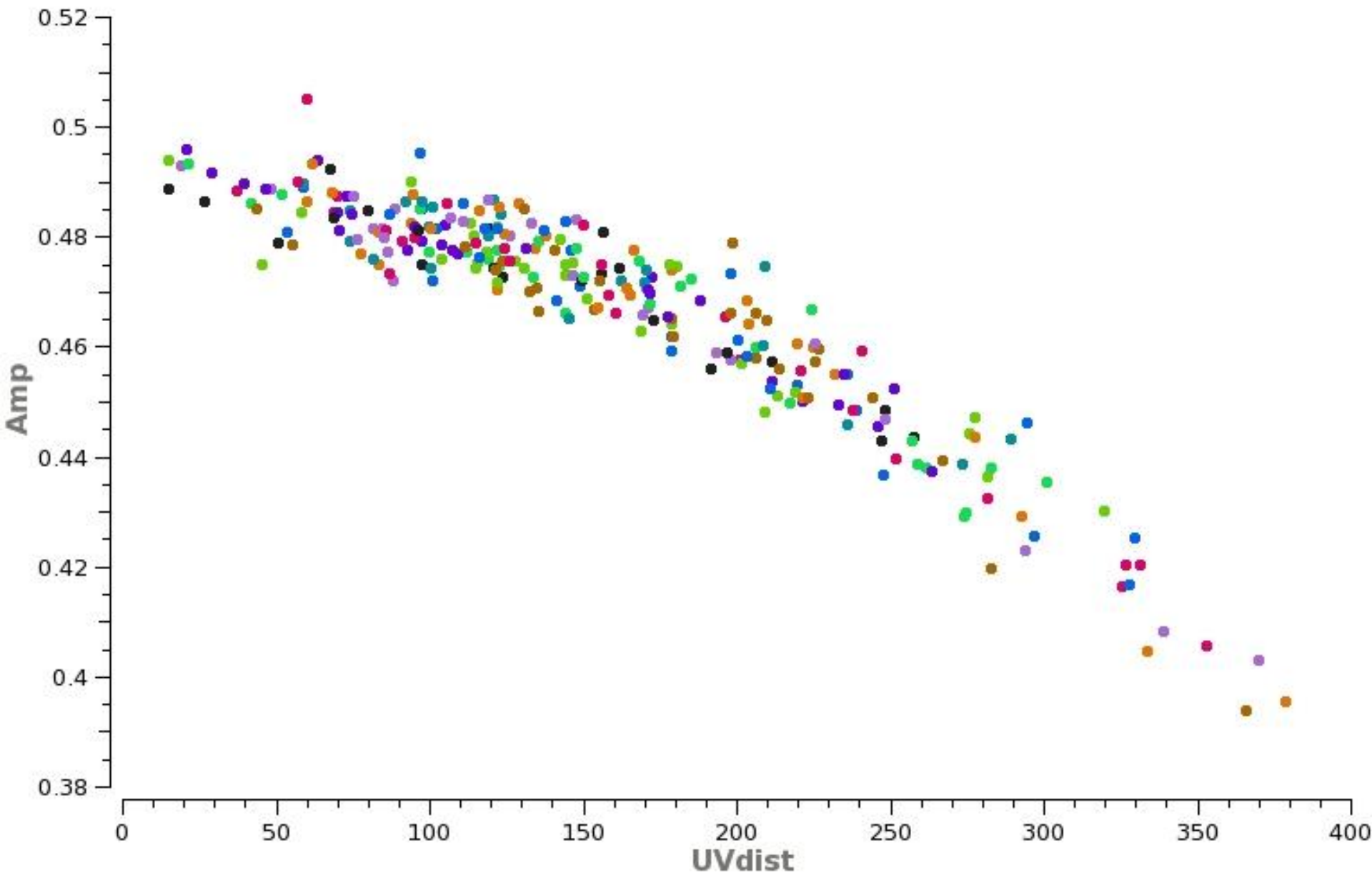
Amp-Calibrators Amp vs. uv-distance (Before)



Amp-Calibrators Amp vs. uv-distance (Model)

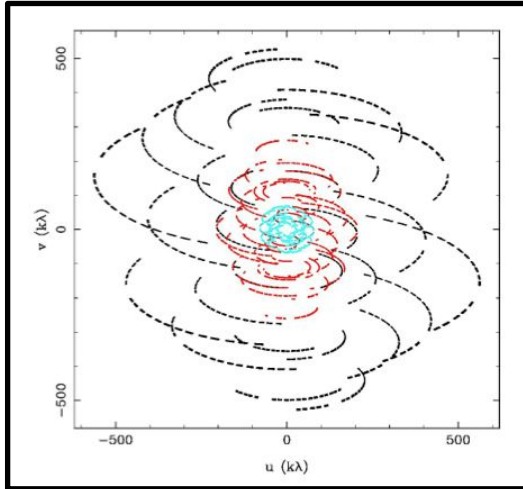


Amp-Calibrators Amp vs. uv-distance (After)



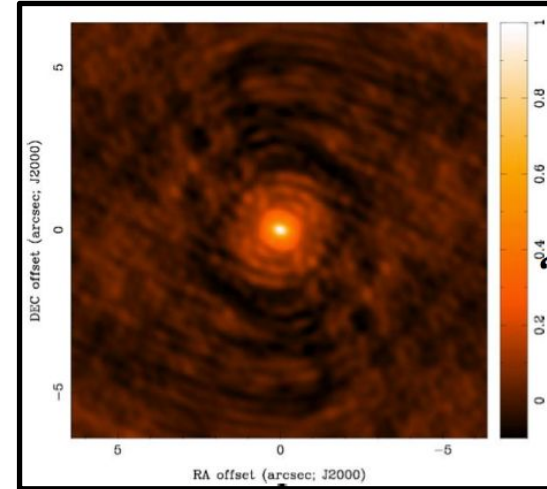
The Dirty Beam

$S(u,v)$

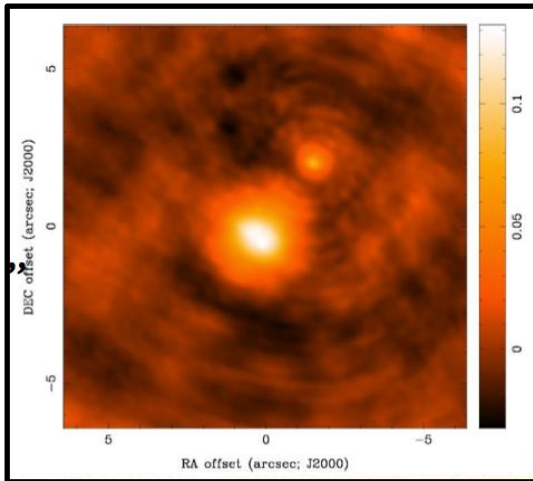


FT
→

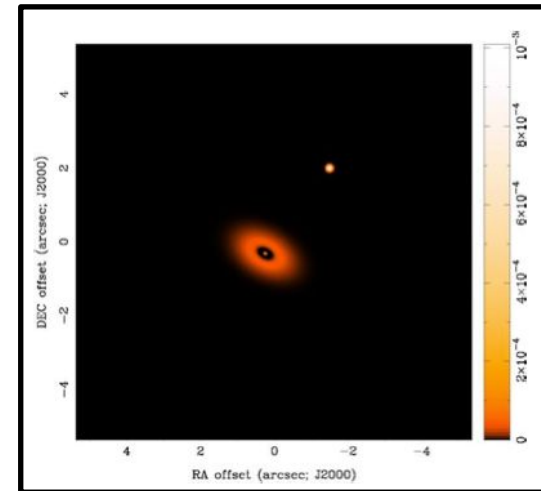
$s(x,y)$
“Dirty Beam”



* (Convolution)



←



$T_D(x,y)$ “Dirty Image”

$T(x,y)$



Deconvolution Philosophy

- use non-linear techniques to interpolate/extrapolate samples of $V(u,v)$ into unsampled regions of the (u,v) plane
(remove sidelobes of the dirty beam from the image)
- aim to find a sensible model of $T(l,m)$ compatible with data
- requires *a priori* assumptions about $T(l,m)$ to pick plausible “invisible” distributions to fill unsampled parts of (u,v) plane
- main assumption: real sky does not look like typical dirty beam
- “clean” deconvolution algorithm (and its variants) by far dominant in radio astronomy, though there are others in use
- a very active research area, e.g. compressed sensing



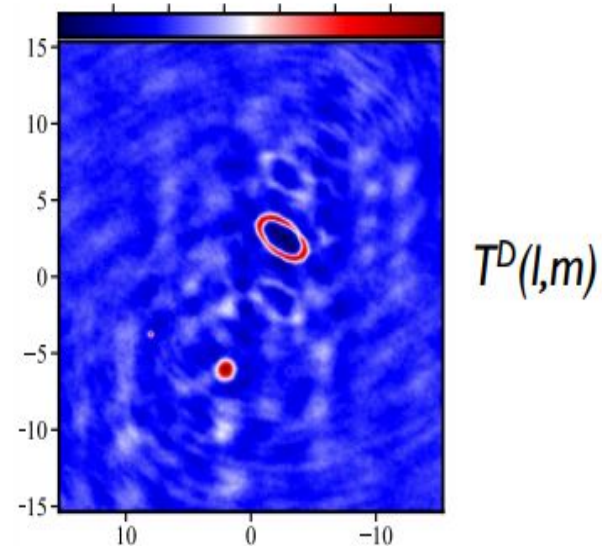
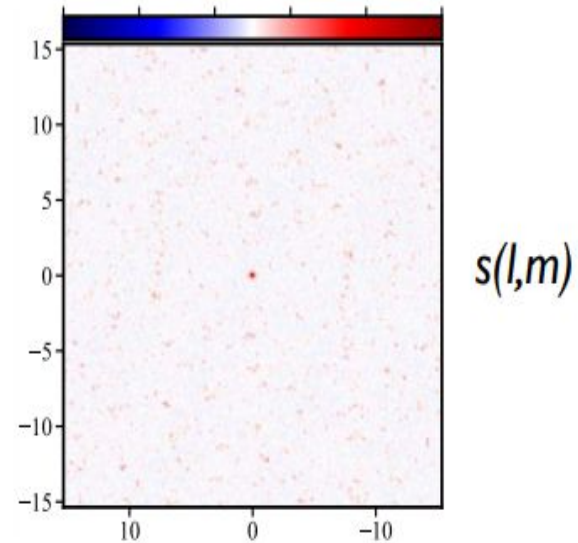
Classic Högbom (1974) clean Algorithm

- *a priori* assumption: $T(l,m)$ is a collection of point sources

initialize a *clean component* list

initialize a *residual image* = dirty image

1. identify the highest peak in the *residual image* as a point source
2. subtract a scaled dirty beam $s(l,m)$ x “loop gain” from this peak
3. add this point source location and amplitude to the *clean component* list
4. goto step 1 (an iteration) unless stopping criterion reached



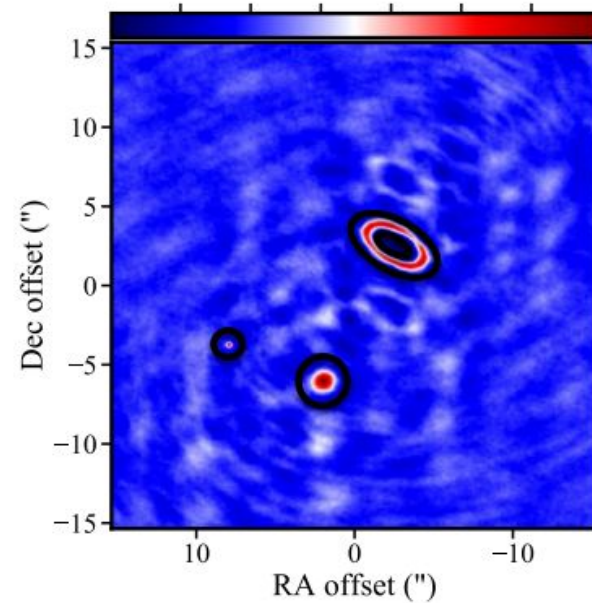
Classic Högbom (1974) clean Algorithm

- stopping criterion
 - *residual map* maximum < threshold = multiple of rms , e.g. 2 x rms (if noise limited)
 - *residual map* maximum < threshold = fraction of dirty map maximum (if dynamic range limited)
 - loop gain parameter
 - good results for $g=0.1$ (CASA `tclean` default)
 - lower values can work better for smooth and extended emission
 - don't "overclean" to artificially low noise level
 - generally a problem only when (u,v) coverage is sparse
-



Classic Högbom (1974) clean Algorithm

- finite support
 - easy to include *a priori* information about where in the dirty map to search for *clean components*
 - implemented as image masks or clean boxes; CASA `tclean` “mask”
 - very useful, often essential for best results, but potentially dangerous
 - use with care
 - can be an arduous manual process; automasking under development

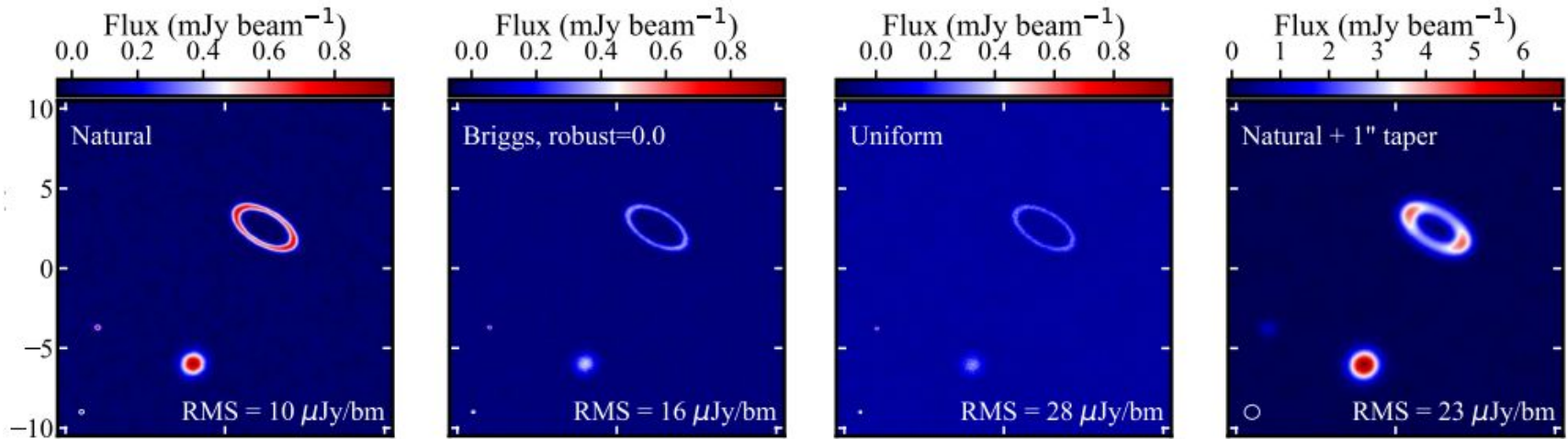


Classic Högbom (1974) clean Algorithm

- last step is to create a final “restored” image
 - make a model image with all point source *clean components*
 - convolve point source model image with a “clean beam”, an elliptical Gaussian fit to the main lobe of the dirty beam (avoids super-resolution of the point source component model)
 - add back *residual map* with noise and structure below the threshold
- restored image is an estimate of the true sky brightness $T(l,m)$
 - units of the restored image are (mostly) Jy per clean beam area = intensity, or brightness temperature



Results from Different Weighting Schemes



natural
0.29x0.25 p.a. -81

robust=0
0.19x0.17 p.a. -78

uniform
0.17x0.15 p.a. -87

natural + 1" taper
0.93x0.88 p.a. -86

Good Future References

Thompson, A.R., Moran, J.M., Swensen, G.W. 2017 “Interferometry and Synthesis in Radio Astronomy”, 3rd edition (Springer)

<http://www.springer.com/us/book/9783319444291>

Perley, R.A., Schwab, F.R., Bridle, A.H. eds. 1989 ASP Conf. Series 6 “Synthesis Imaging in Radio Astronomy” (San Francisco: ASP)

www.aoc.nrao.edu/events/synthesis

IRAM Interferometry School proceedings

www.iram.fr/IRAMFR/IS/IS2008/archive.html



Good Future References

NRAO Synthesis Imaging Workshop

<https://science.nrao.edu/science/meetings/2018/16th-synthesis-imaging-workshop/16th-synthesis-imaging-workshop-lectures>

Examples of UV coverage from Ian Czekala

<https://drive.google.com/file/d/1fy3edrjNATo175WopB49-3mZ7QeZPK5O/view>

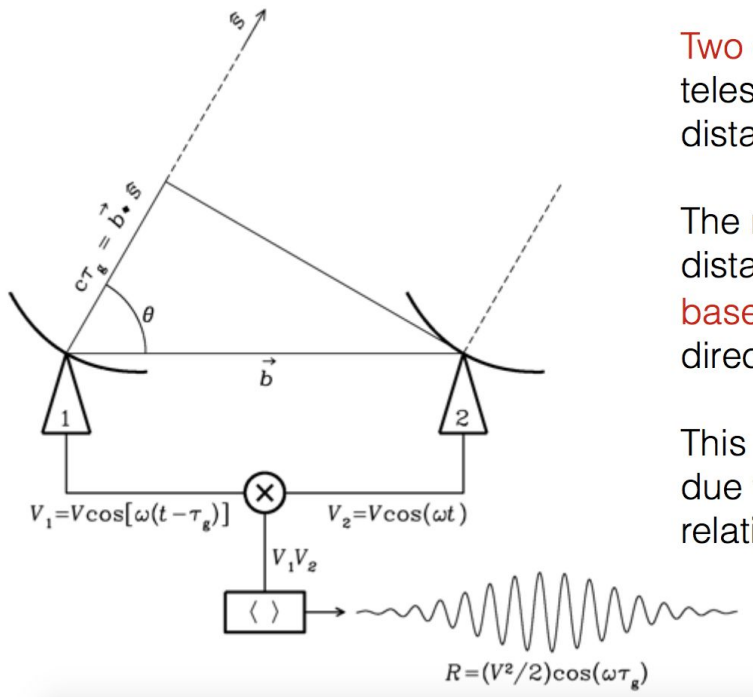




www.nrao.edu
science.nrao.edu

*The National Radio Astronomy Observatory is a facility of the National Science
Foundation
operated under cooperative agreement by Associated Universities, Inc.*





Two element interferometer: Two identical telescopes observe the electric field of some distant source (c.f. Young's double slit).

The radiation to antenna 1 travels an extra distance $\vec{b} \cdot \hat{s} = b \cos \theta$, where \vec{b} is the vector **baseline** length and \hat{s} a unit vector in the direction of the source.

This can be expressed as a **geometric delay** due to the projected position of the source, relative to the baseline of the antennas.

$$\tau_g = \vec{b} \cdot \hat{s} / c$$

For a **quasi-monochromatic** interferometer (responds to a narrow frequency range $\nu = 2\pi / \lambda$), the output voltages over time t from the two antennas are,

$$V_1 = V \cos[\omega(t - \tau_g)] \quad \text{and} \quad V_2 = V \cos(\omega t)$$

The **correlator** multiplies the voltages from the two antennas together to give,

$$V_1 V_2 = V^2 \cos[\omega(t - \tau_g)] \cos(\omega t) = \left(\frac{V^2}{2}\right) [\cos[2\omega t - \omega\tau_g] + \cos(\omega\tau_g)]$$

and then a time average $[\Delta t \gg (2\omega)^{-1}]$ to remove the high frequency component to give,

$$R = \langle V_1 V_2 \rangle = \left(\frac{V^2}{2}\right) \cos(\omega\tau_g)$$

Uncorrelated noise from gain variations within the receivers, the atmosphere and radio frequency interference does not correlate (advantage over single dish measurements).

The output voltage R varies sinusoidally with the change of the source direction in the interferometer frame, i.e. the delay changes. These sinusoids are called **fringes**, and we can define the **fringe phase** as,

$$\phi = \omega\tau_g = \frac{\omega}{c} b \cos \theta \quad \text{and} \quad \frac{d\phi}{d\theta} = \frac{\omega}{c} b \sin \theta = 2\pi \left(\frac{b \sin \theta}{\lambda}\right)$$

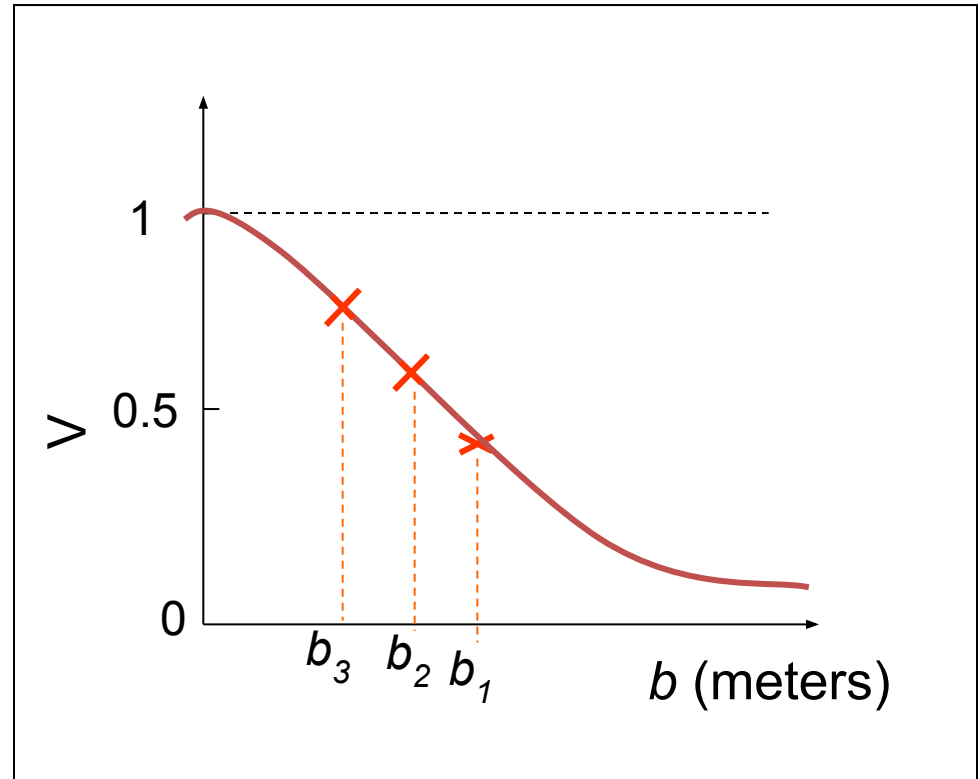
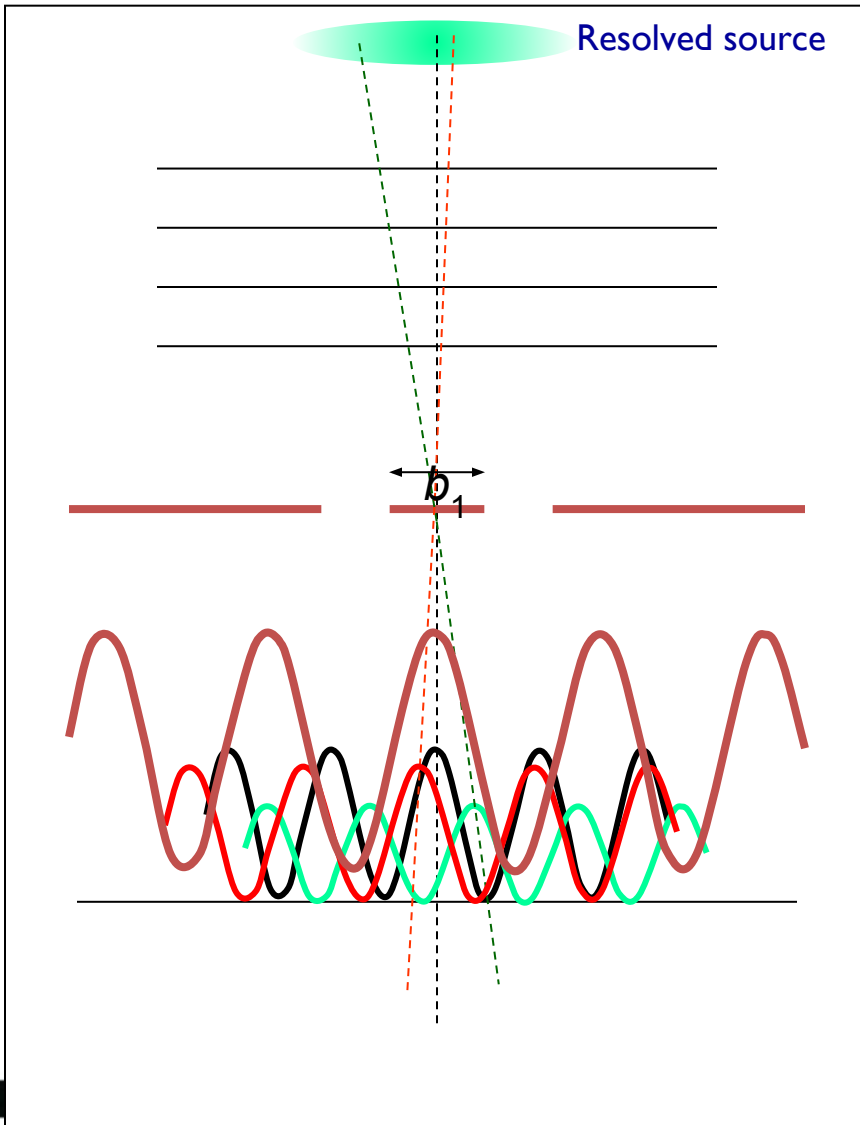
The fringe period ($\Delta\phi = 2\pi$) corresponds to an angular change of $\Delta\theta = \lambda / (b \sin \theta)$, and so, for large b , interferometers can measure very accurate positions of sources (typically $\sigma_\theta \sim 10^{-3}$ arcsec).

As the source(s) moves across the sky, the response of the interferometer changes because the geometric delay changes. The maximum in the fringe pattern occurs when $\tau_g c$ is an integral number of wavelengths (similar to the Young's double slit).



Visibility and Sky Brightness

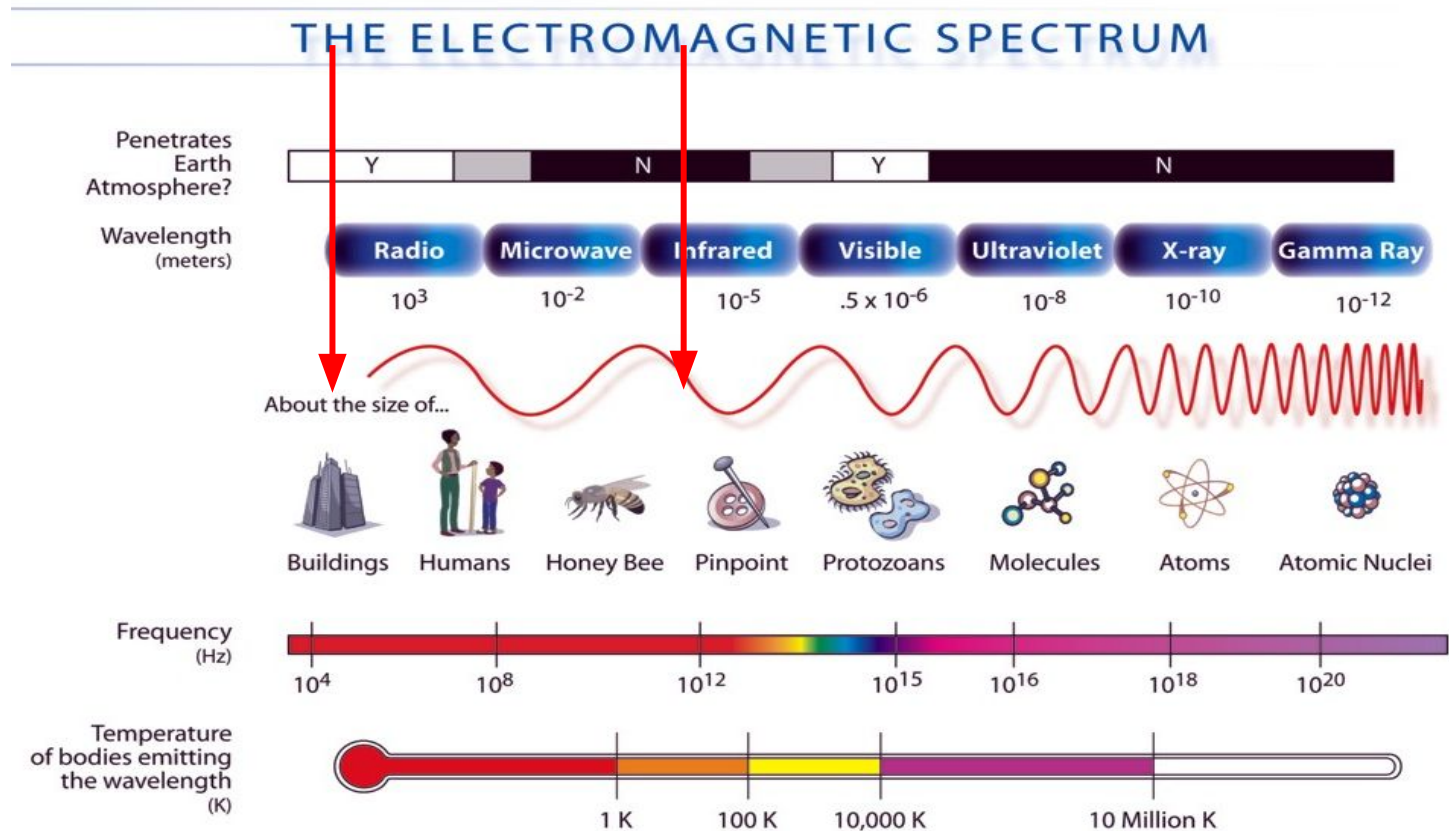
Graphic courtesy Andrea Isella



$$|V| = \frac{I_{\max} - I_{\min}}{I_{\max} + I_{\min}} = \frac{\text{Fringe Amplitude}}{\text{Average Intensity}}$$

Radio Astronomy

Now used to refer to most telescopes using heterodyne technology



What is heterodyne?

In a heterodyne receiver, observed sky frequencies are converted to lower frequency signals by mixing with a signal artificially created by a Local Oscillator. The output can then be amplified and analyzed more easily while retaining the original phase and amplitude information.

**Synoptic diagram of heterodyne receivers
(basic building blocks)**

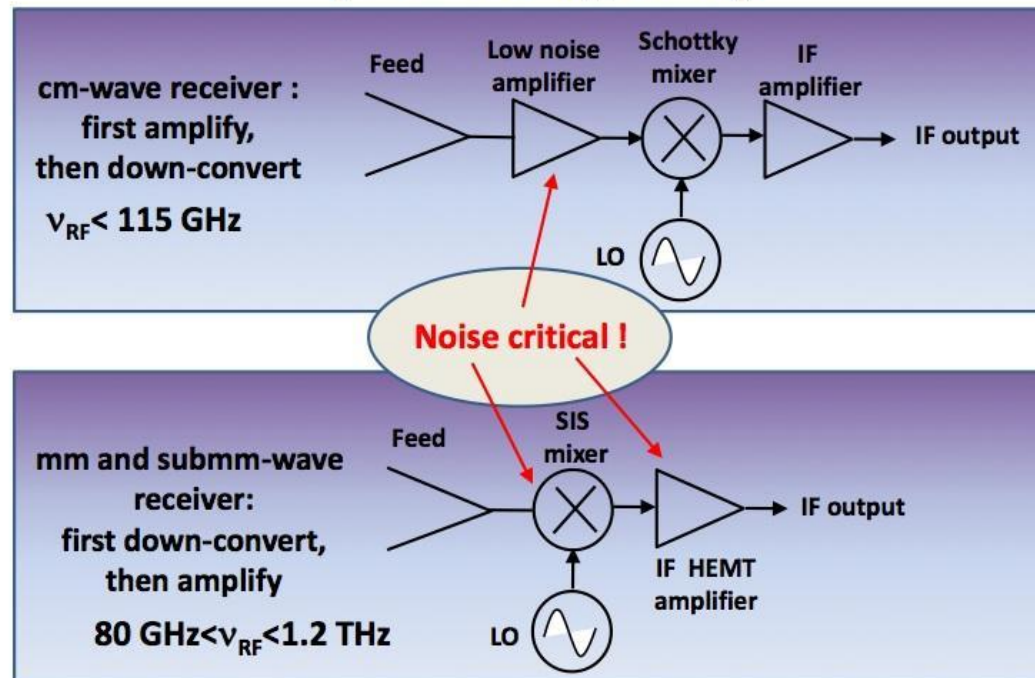
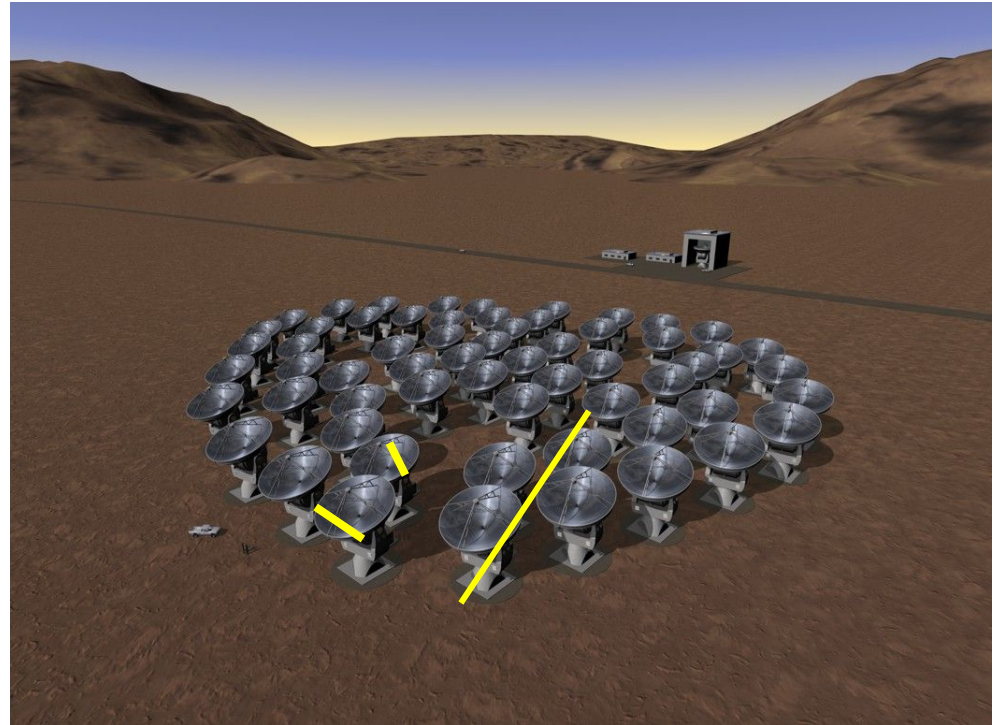
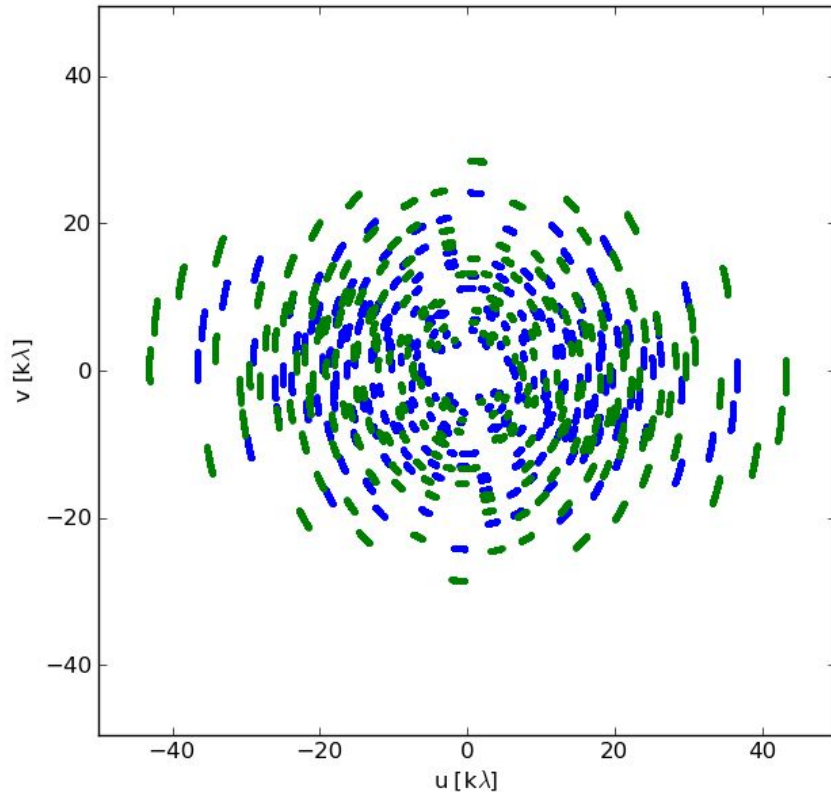


Image from Alessandro Navarrini (IRAM)

Sampling Function

Each antenna pair samples only one spot; the array cannot sample the entire Fourier/uv domain resulting in an **imperfect image**



Small uv-distance: short baselines (measure extended emission)
Long uv-distance: long baselines (measure small scale emission)
Orientation of baseline also determines orientation in the uv-plane



uv coverage: why the central hole?

- The central hole in the sampling of the uv plane arises due to **short baselines**.
- The largest angular scale that an interferometer is sensitive to is given by the shortest distance between 2 antennas.
- The field of view is given by the beam of a single antenna.
- A single antenna diameter will always be $<$ the shortest distance between two antennas.
- So the field of view is always $>$ the largest angular scale
- If your source is extended, you will always have some flux at short spacings (i.e. extended emission) that is not recovered.
- **Solutions:** We can extrapolate to these shorter spacings after our observations are taken or we can fill in the information with 7m observations or ultimately single dish data.



A Brief Word on Calibration

Calibration requirements (Handled by ALMA):

Gain calibrator

Bright quasar near science target
Solves for atmospheric and
instrumental variations with time

Bandpass calibrator

Bright quasar
Fixes instrumental effects and
variations vs frequency

Absolute flux calibrator

Solar system object or quasar
Used to scale relative amplitudes
to absolute value

