

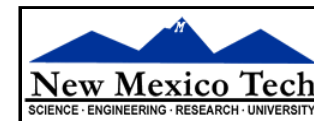
Wide Bandwidth Imaging



14th NRAO Synthesis Imaging Workshop

13 – 20 May, 2014, Socorro, NM

Urvashi Rau
National Radio Astronomy Observatory



Why do we need wide bandwidths ?

Broad-band receivers => Increased 'instantaneous' imaging sensitivity

Continuum sensitivity : σ_{cont} (at field-center) $= \frac{\sigma_{chan}}{\sqrt{N_{chan}}} \propto \frac{T_{sys}}{\sqrt{N_{ant}(N_{ant}-1)} \delta\tau \delta\nu}$

50 MHz \rightarrow 2 GHz => Theoretical improvement : $\sqrt{\frac{2\text{GHz}}{50\text{MHz}}} \approx 6$ times.

In practice, effective broadband sensitivity for imaging depends on bandpass shape, data weights, and regions of the spectrum flagged due to RFI. For VLA L-band, we typically use 70% of the band.

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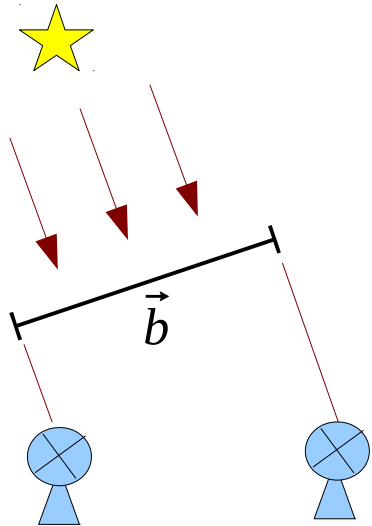
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Some bandwidth jargon.....

Frequency Range :	ν_{min}, ν_{max}	(1 - 2 GHz)	(4 - 8 GHz)	(8 - 12 GHz)
Bandwidth :	$\nu_{max} - \nu_{min}$	1 GHz	4 GHz	4 GHz
Bandwidth Ratio :	$\nu_{max} : \nu_{min}$	2 : 1	2 : 1	1.5 : 1
Fractional Bandwidth :	$(\nu_{max} - \nu_{min}) / \nu_{mid}$	66%	66%	40%

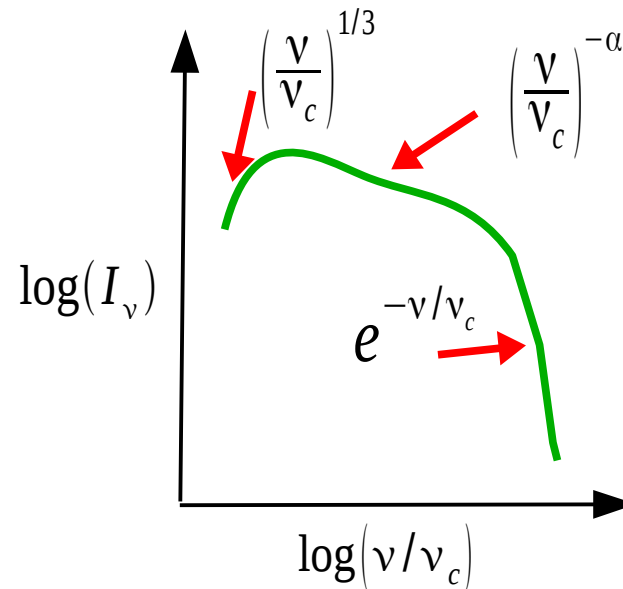
The instrument and the sky change with frequency...

UV-coverage



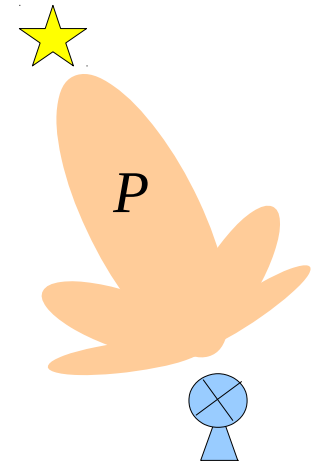
$$S(u, v)_\nu = \frac{\vec{b}}{\lambda} = \frac{\vec{b} \nu}{c}$$

Sky Brightness



$$I(\nu)$$

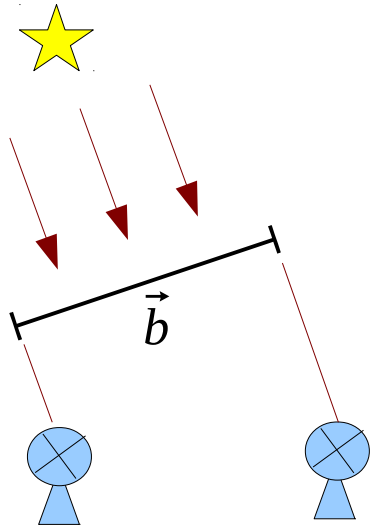
Primary Beam



$$HPBW_\nu = \frac{\lambda}{D} = \frac{c}{\nu D}$$

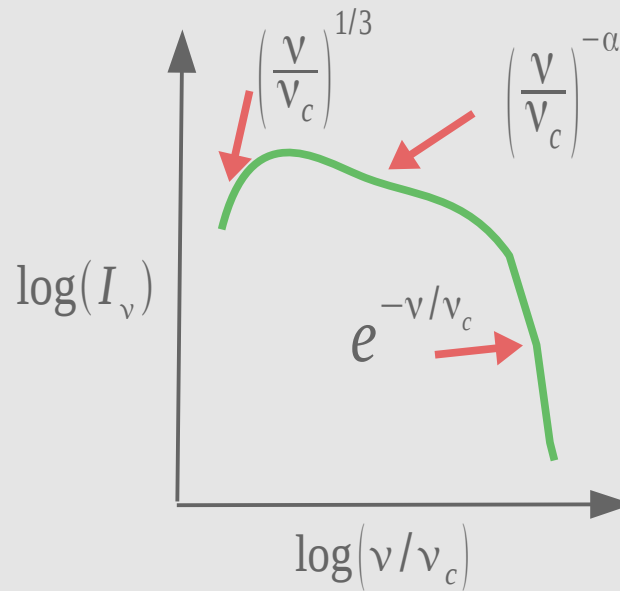
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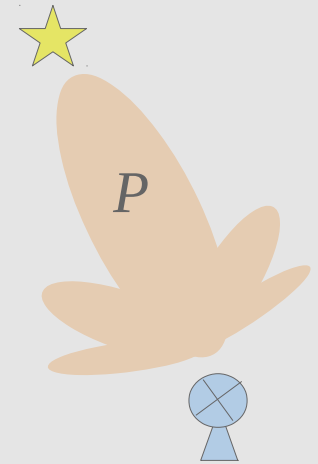
$$S(u, v)_\nu = \frac{\vec{b}}{\lambda} = \frac{\vec{b} \nu}{c}$$

Sky Brightness



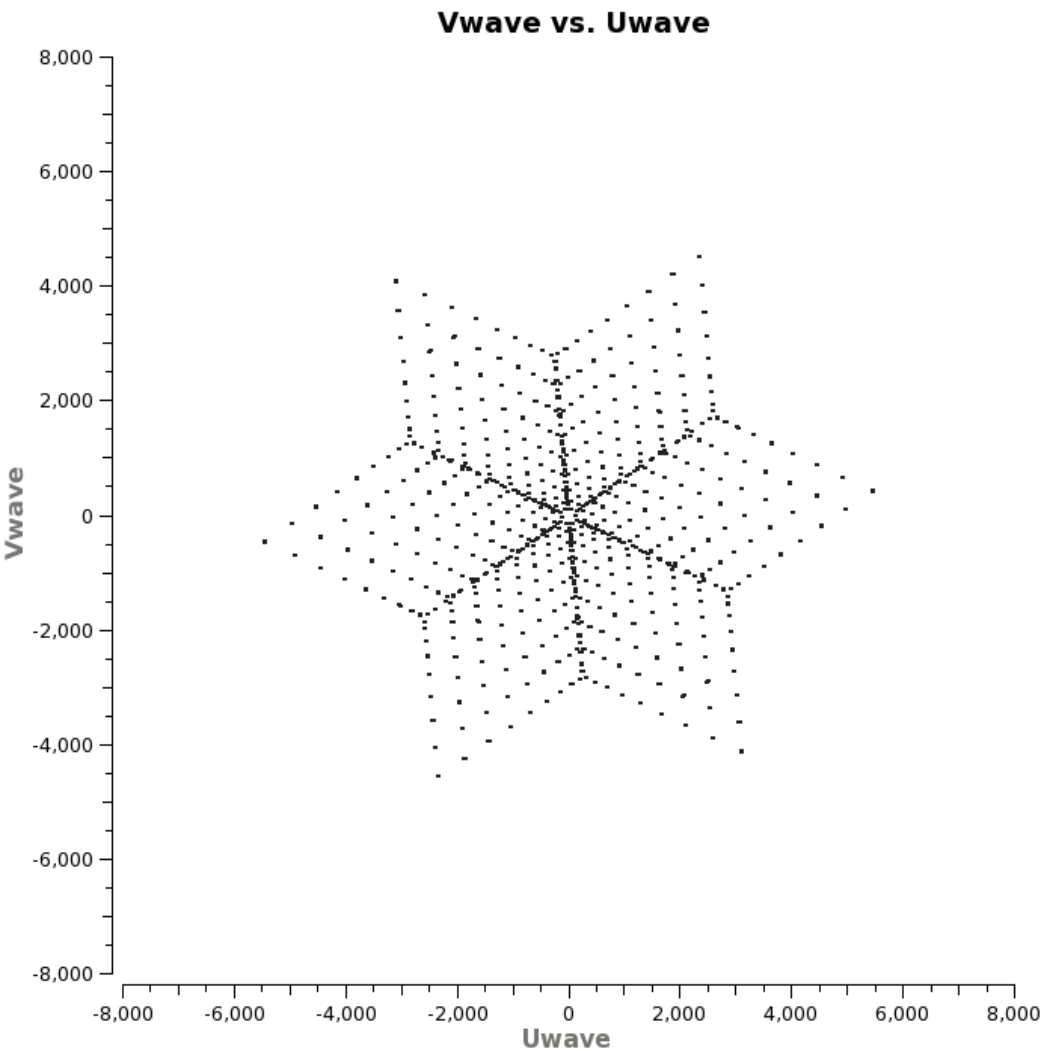
$$I(\nu)$$

Primary Beam

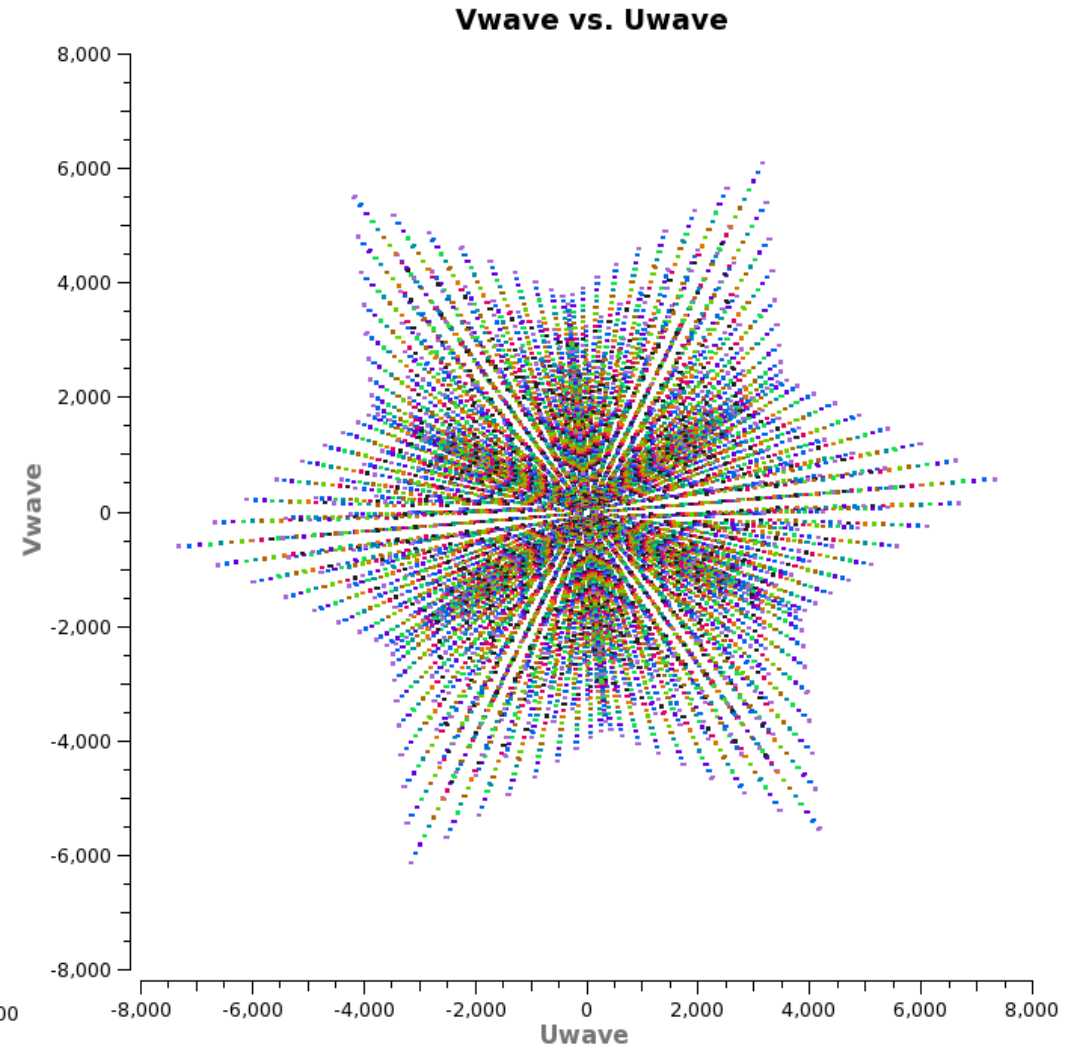


$$HPBW_\nu = \frac{\lambda}{D} = \frac{c}{\nu D}$$

Multi-Frequency-Synthesis – UV coverage

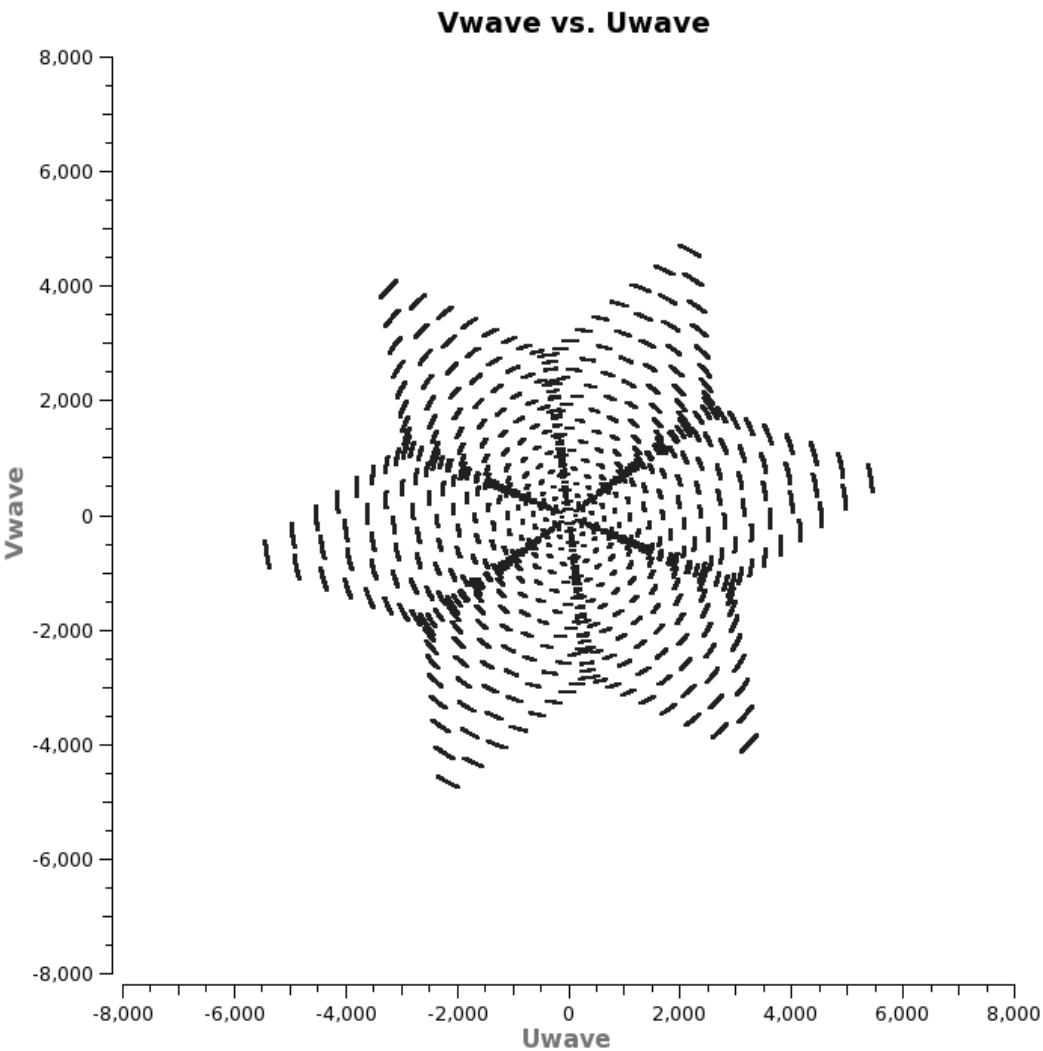


1.5 GHz

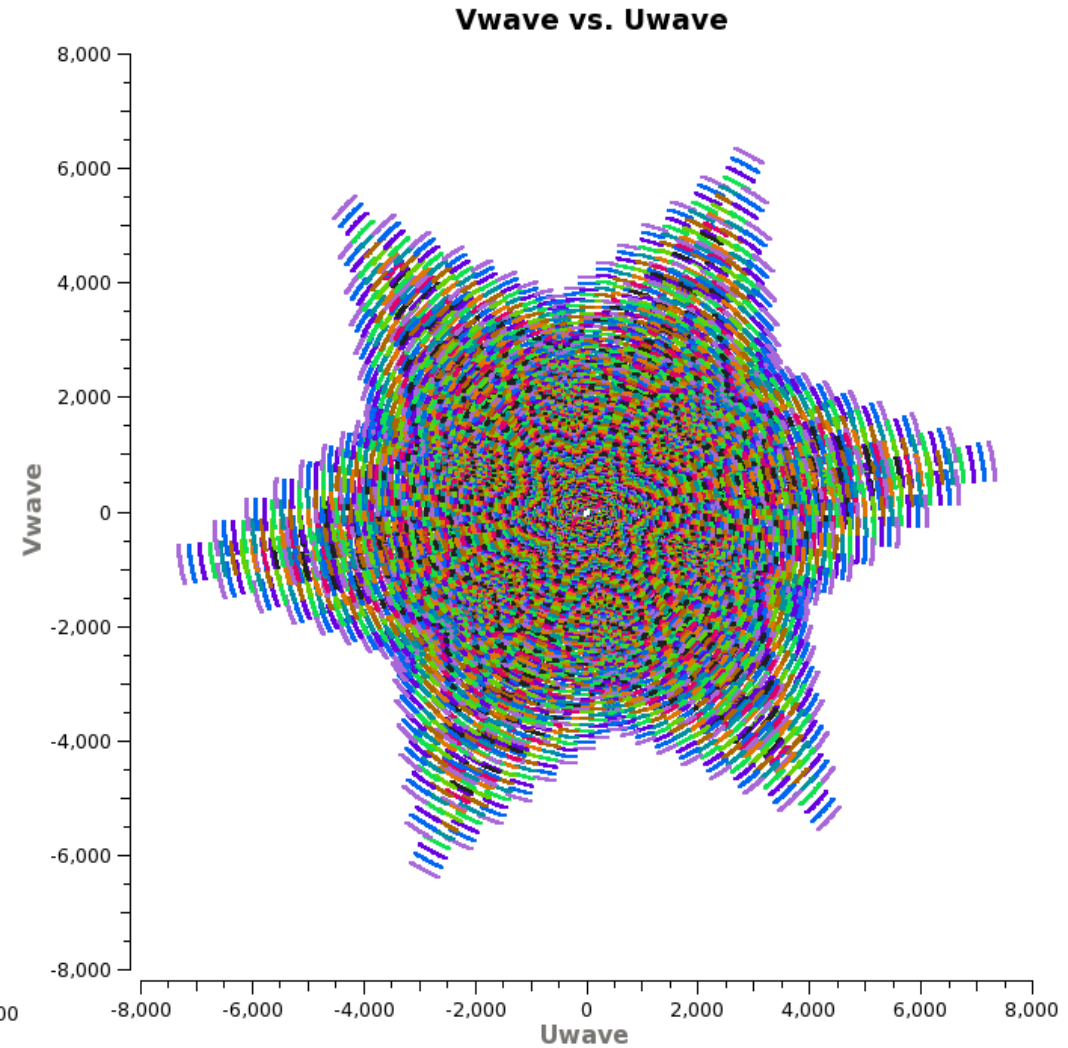


1 – 2 GHz

Multi-Frequency-Synthesis – UV coverage

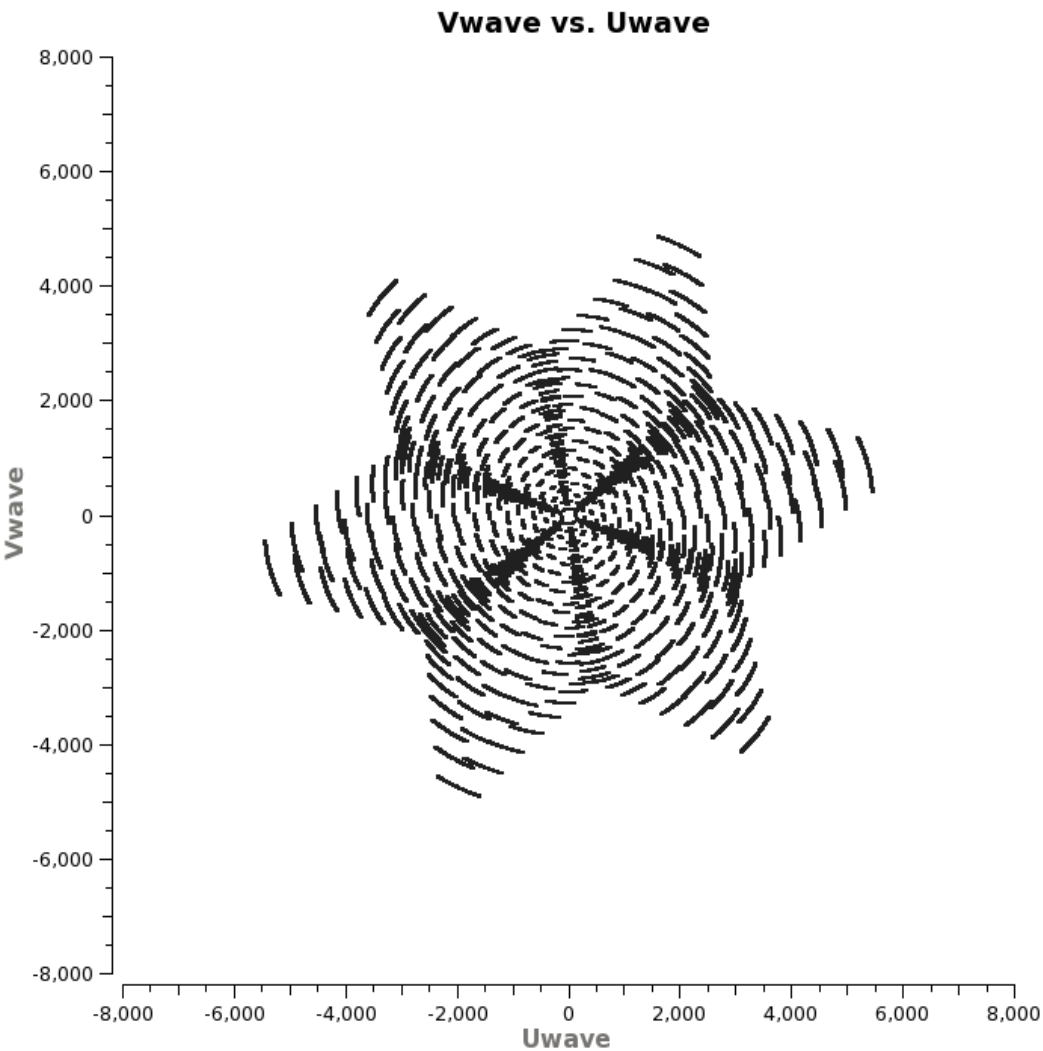


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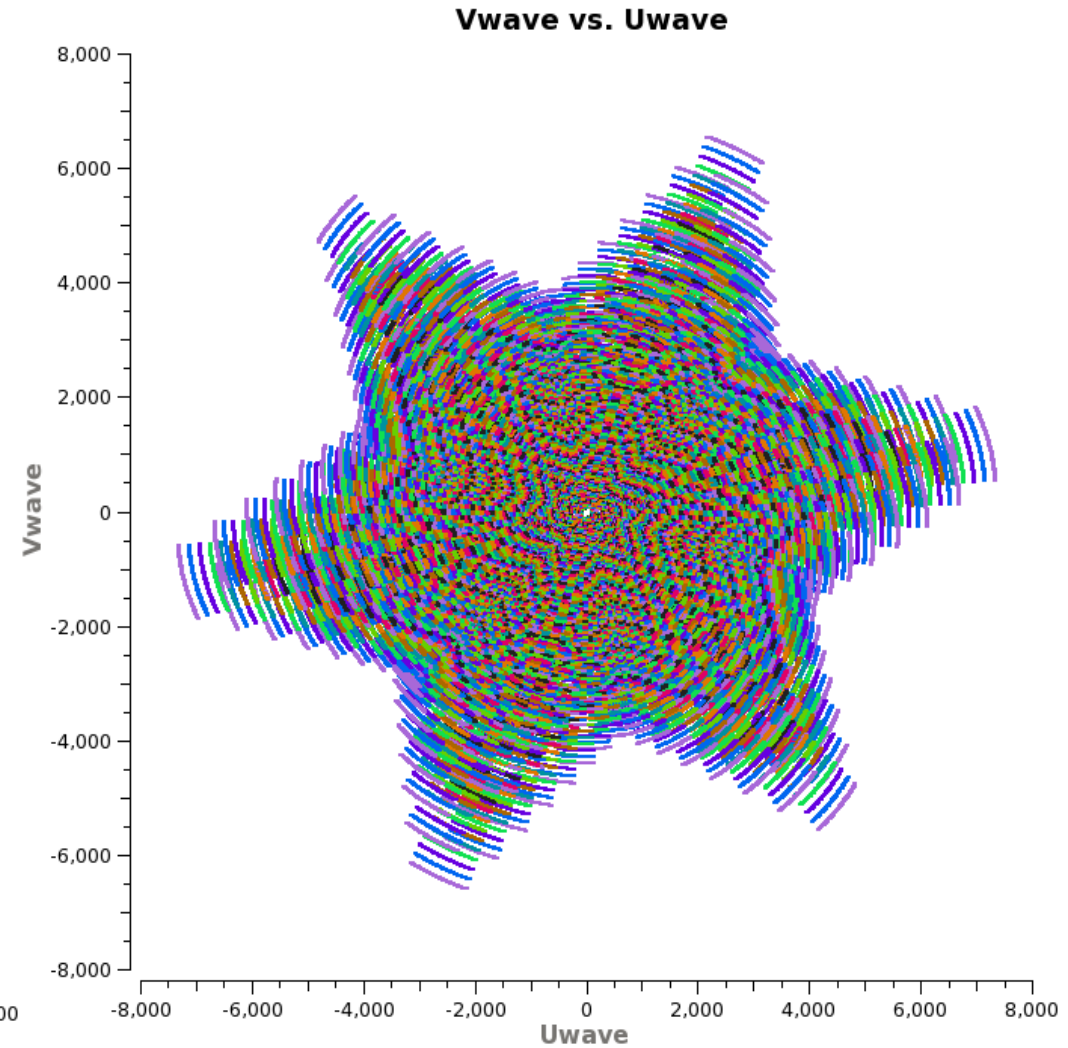


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Multi-Frequency Synthesis – UV coverage

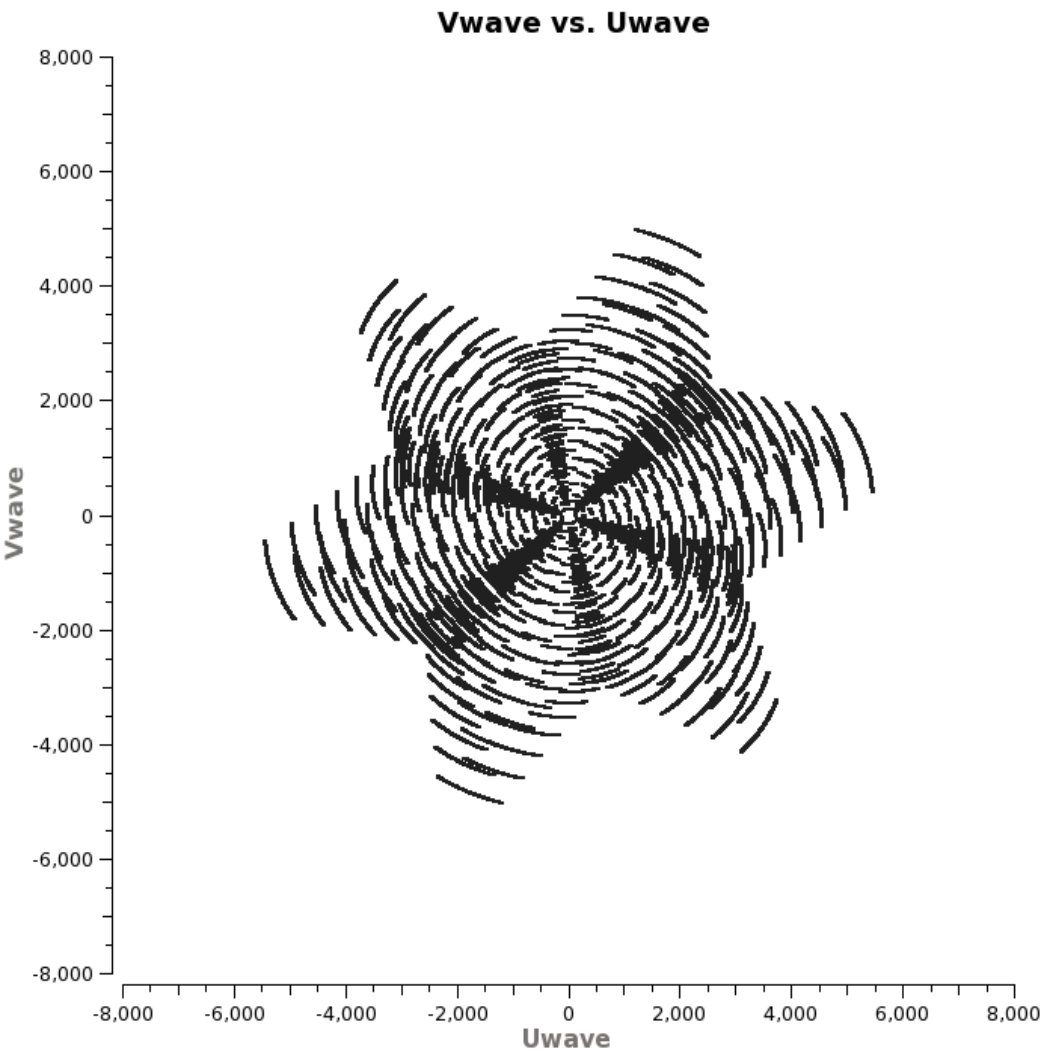


1.5 GHz

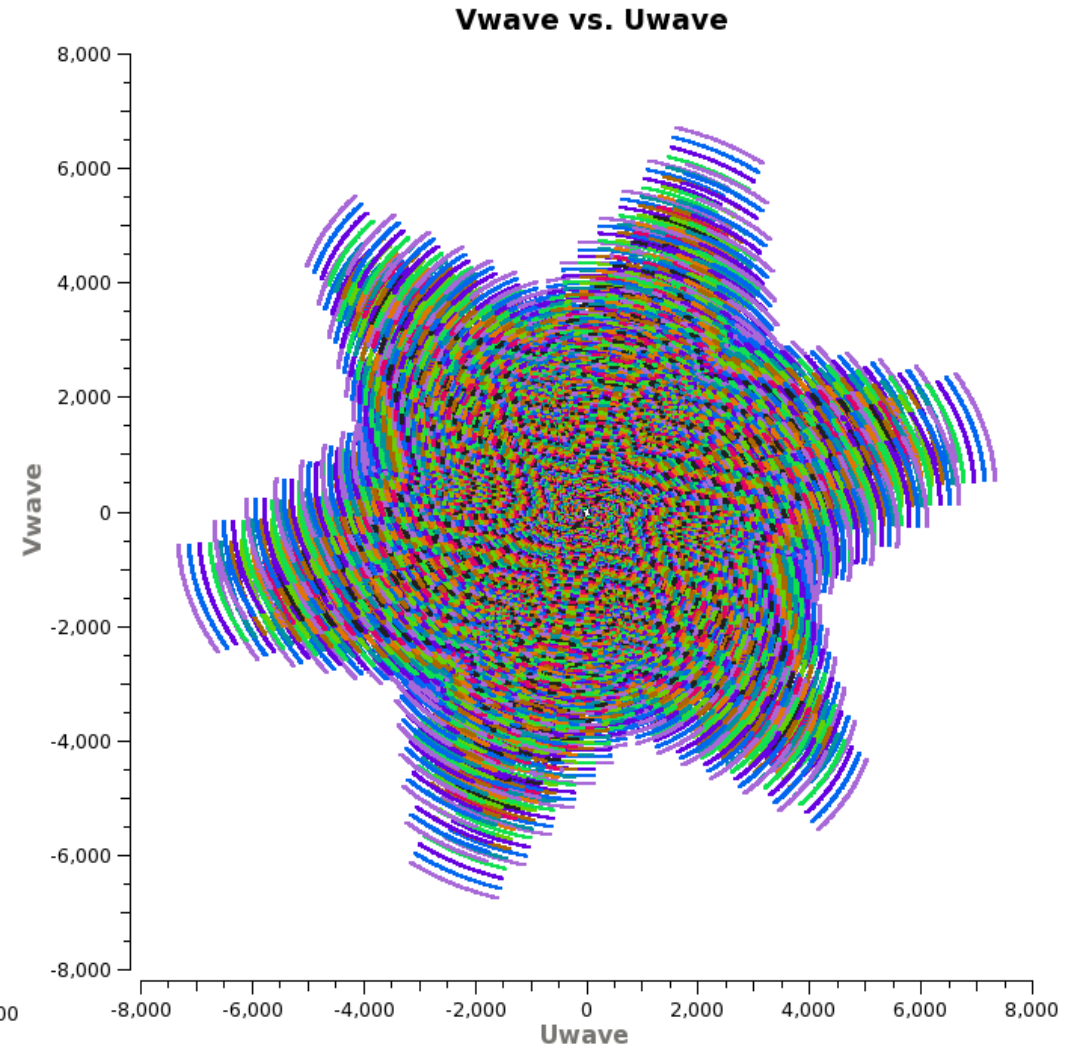


1 – 2 GHz

Multi-Frequency Synthesis – UV coverage

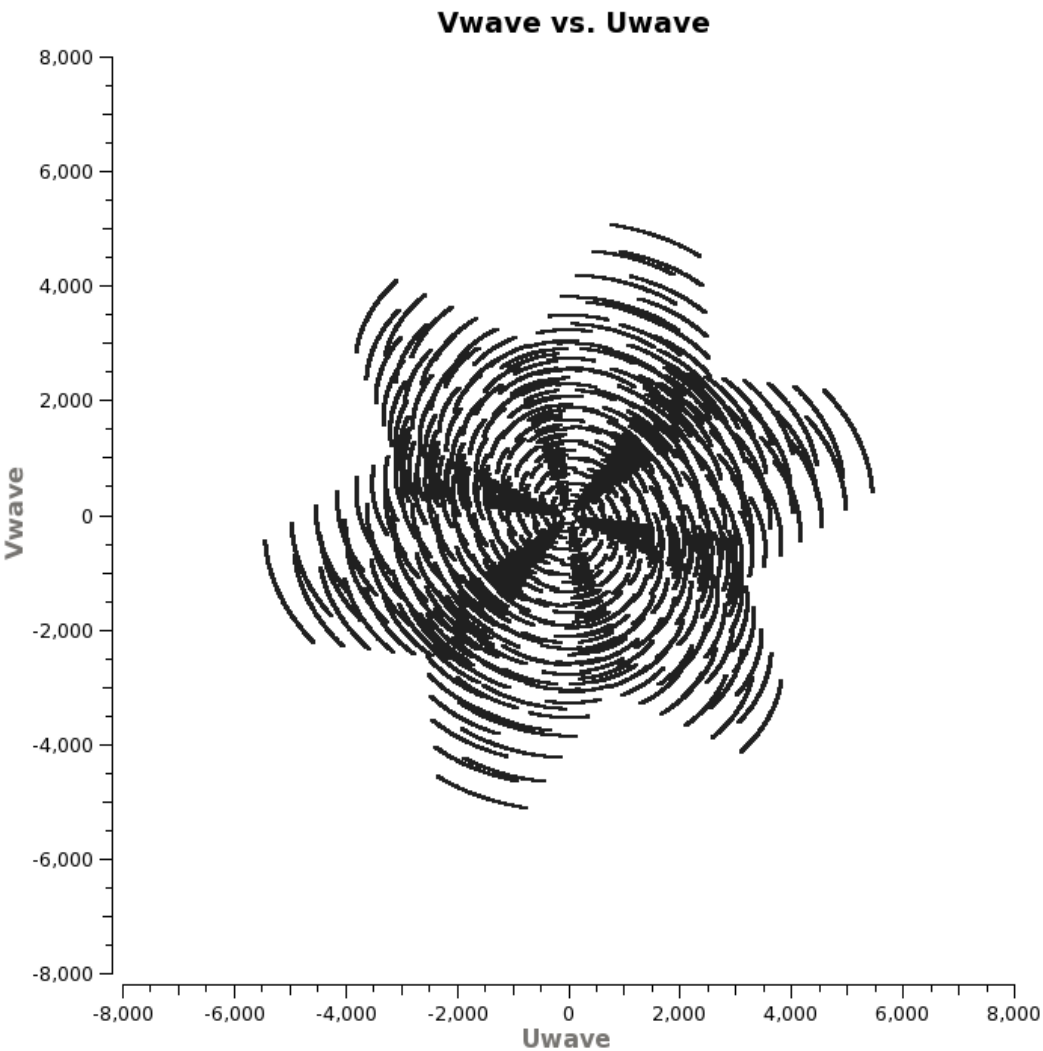


1.5 GHz

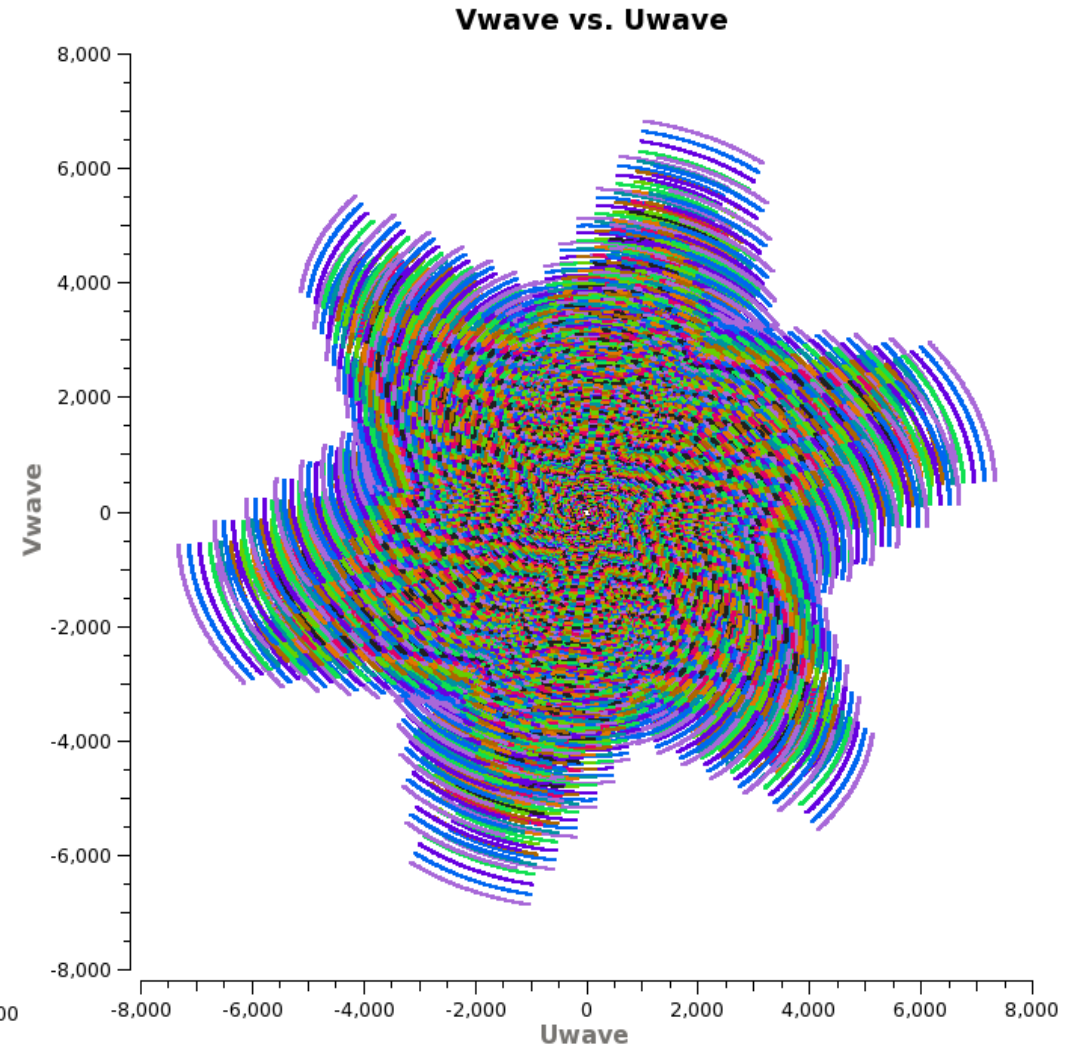


1 – 2 GHz

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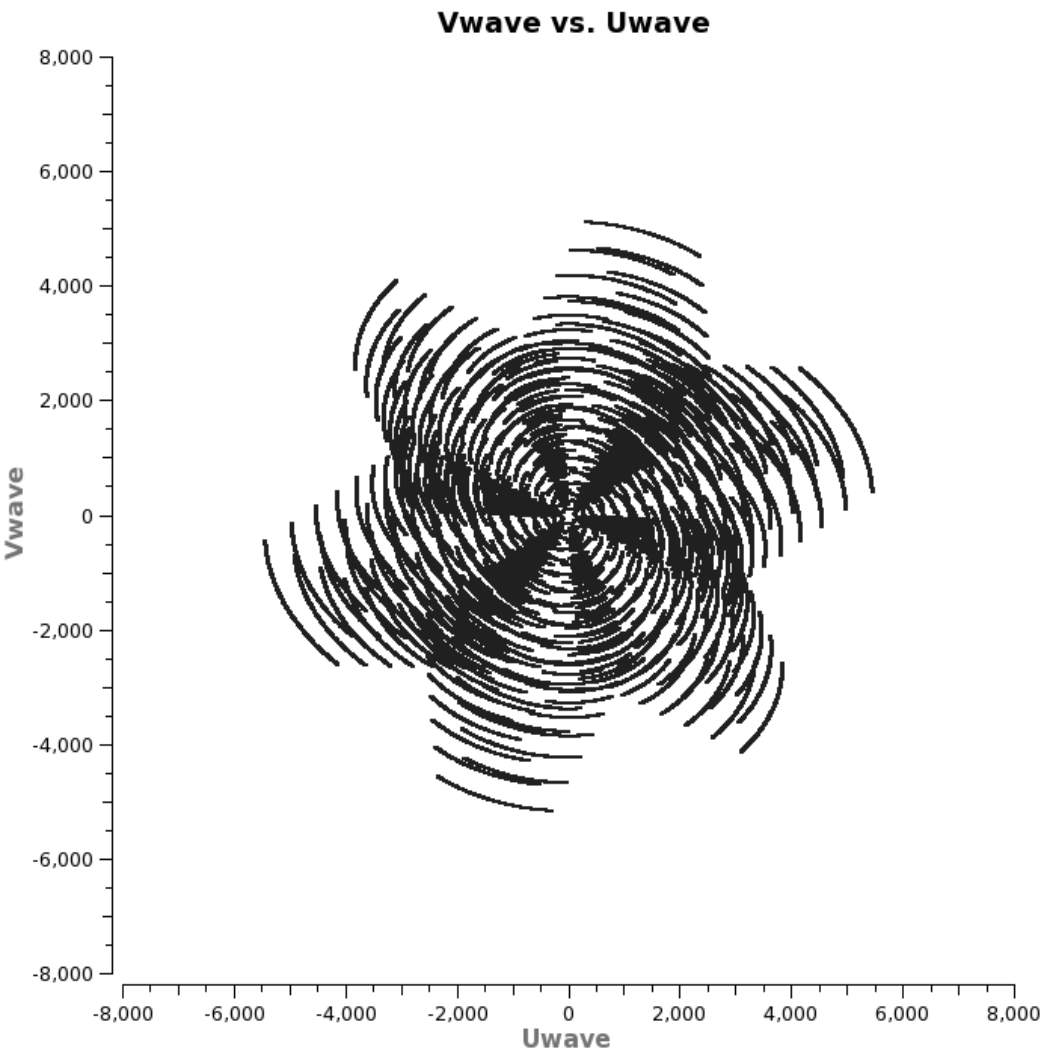


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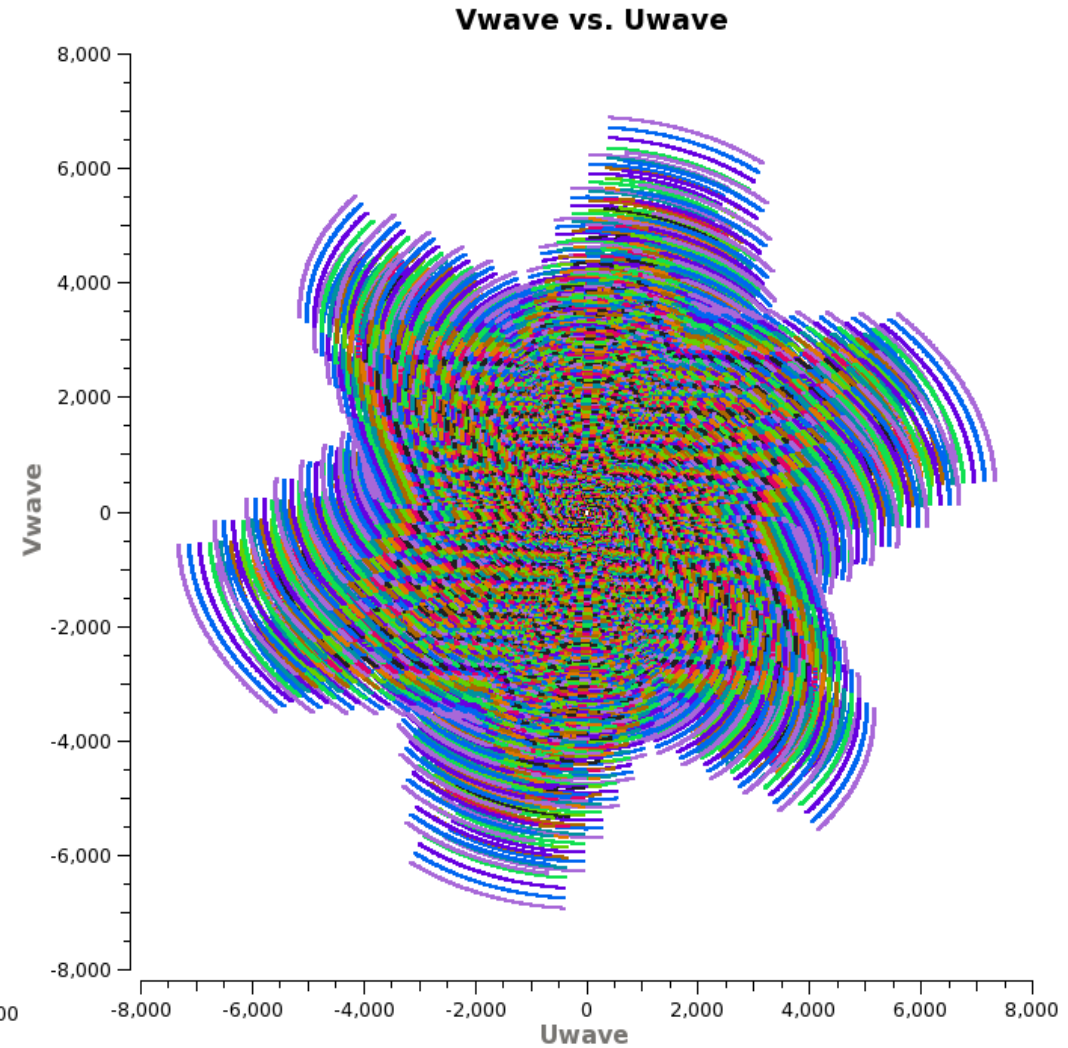


1 – 2 GHz

Multi-Frequency Synthesis – UV coverage

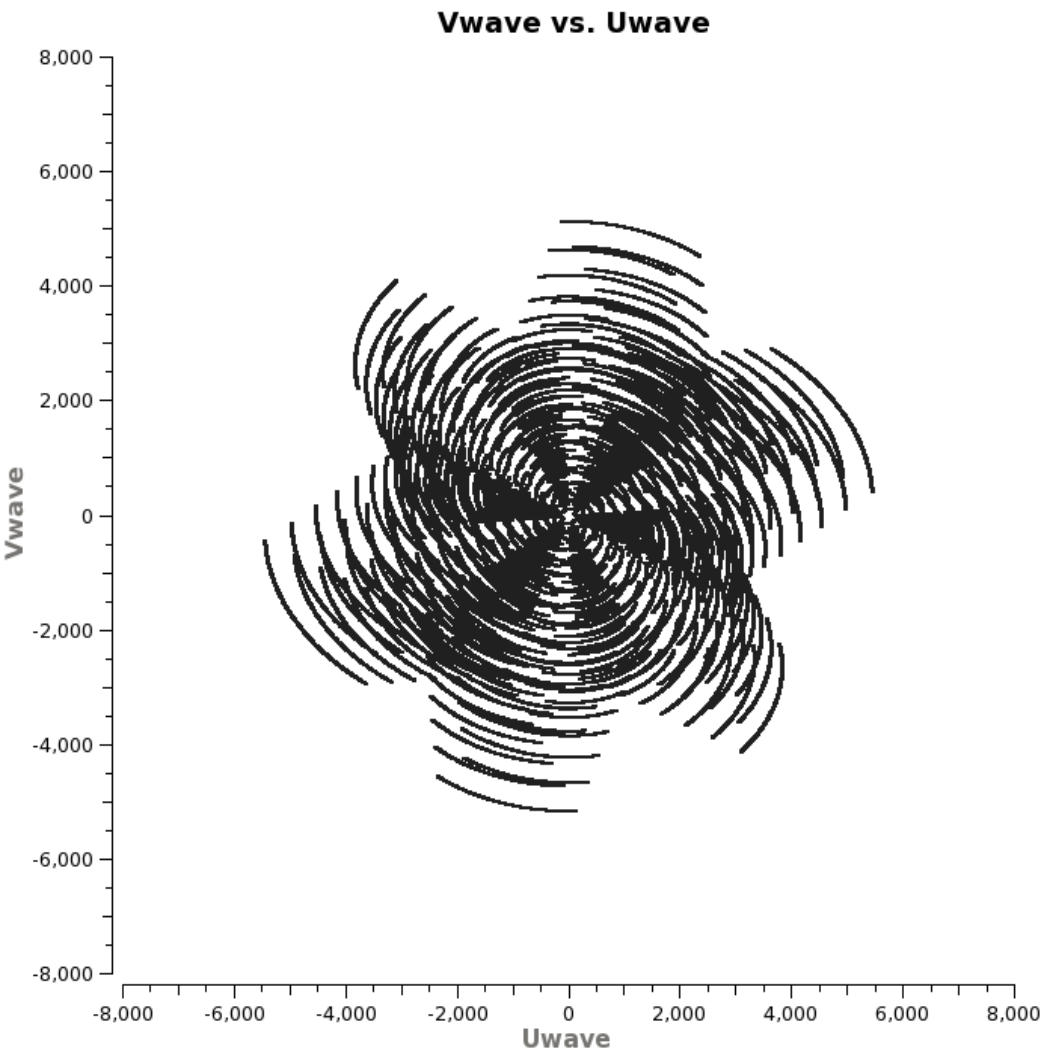


1.5 GHz

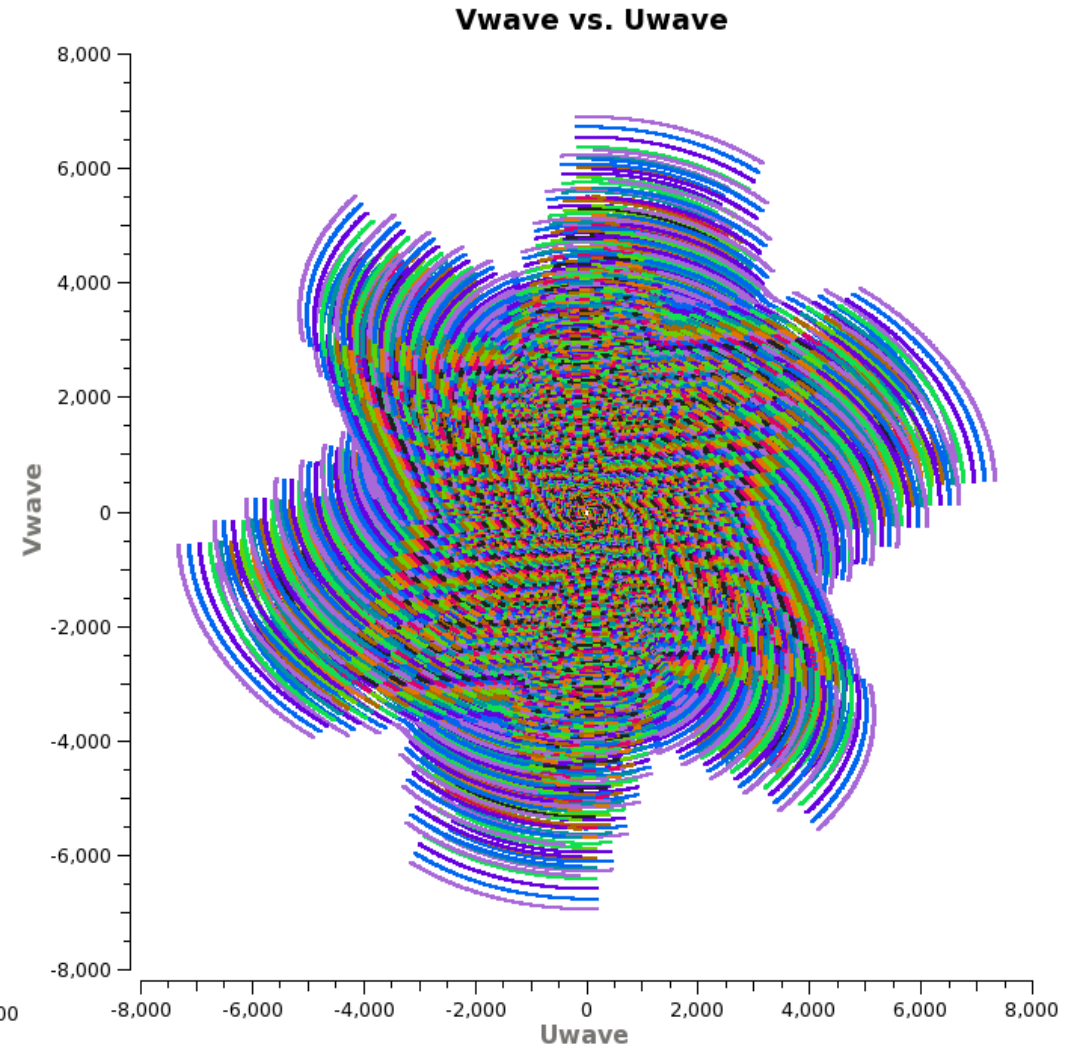


1 - 2 GHz

Multi-Frequency Synthesis – UV coverage

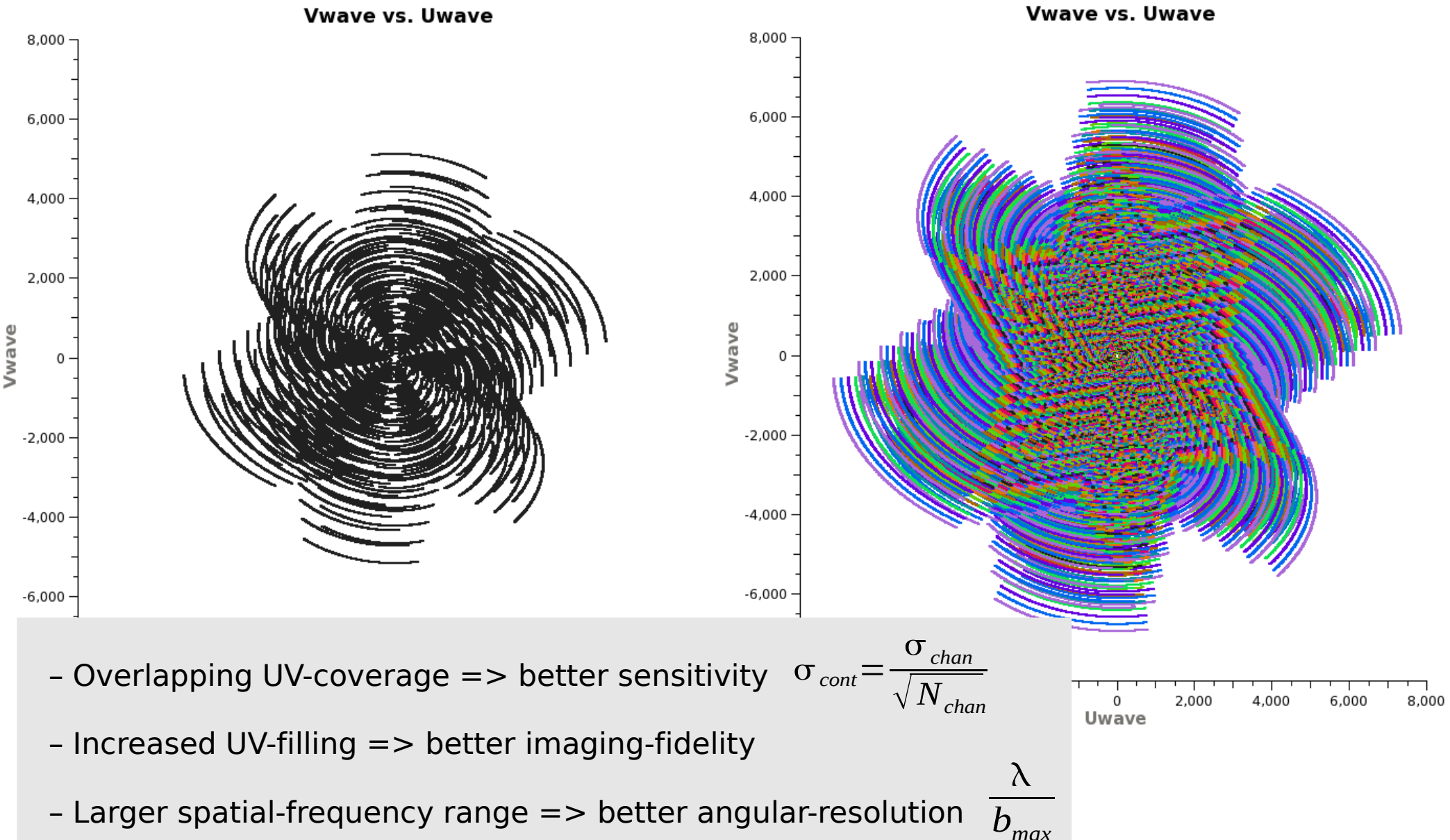


1.5 GHz



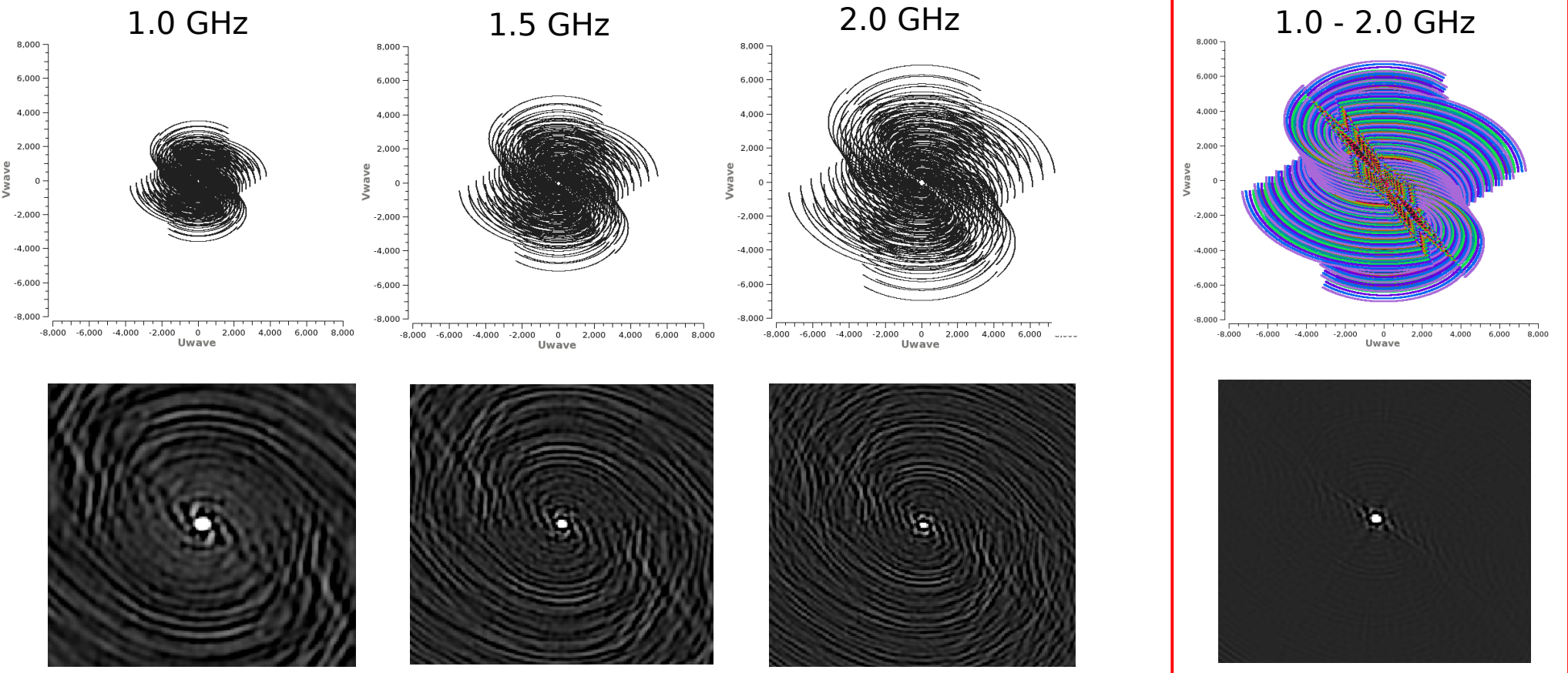
1 - 2 GHz

Multi-Frequency Synthesis – UV coverage



Imaging Properties change with frequency

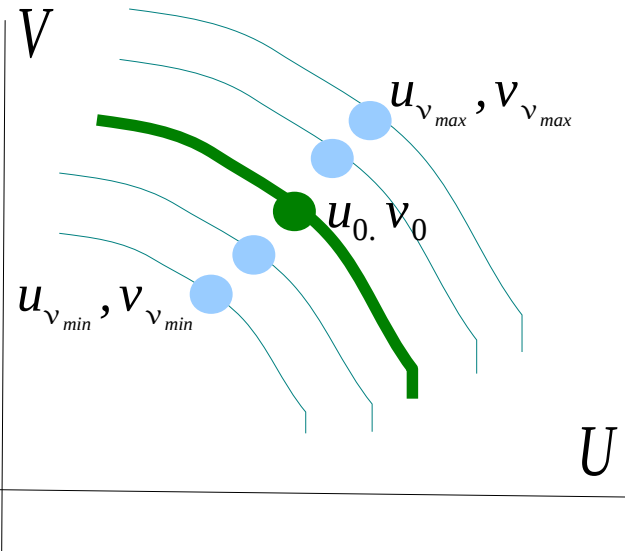
- Angular-resolution increases at higher frequencies
- Sensitivity to large scales decreases at higher frequencies
- Wideband UV-coverage has fewer gaps => lower Psf sidelobe levels



Measure visibilities in frequency 'channels' and place them at their correct locations on the UV-plane.

Bandwidth smearing (chromatic aberration)

Suppose the entire receiver bandwidth was measured in one channel ν_0



$V(u_\nu)$ is mistakenly mapped to $\frac{\nu_0}{\nu} u_\nu$

Similarity theorem of Fourier-transforms :

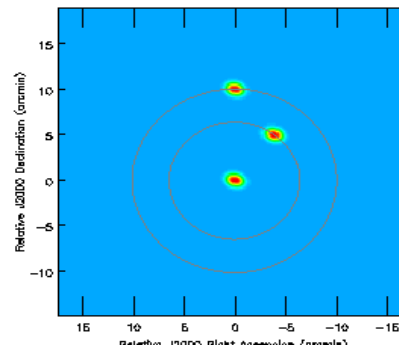
Radial shift in source position with frequency.
=> Radial smearing of the sky brightness

Excessive channel averaging during post-processing has a similar effect.

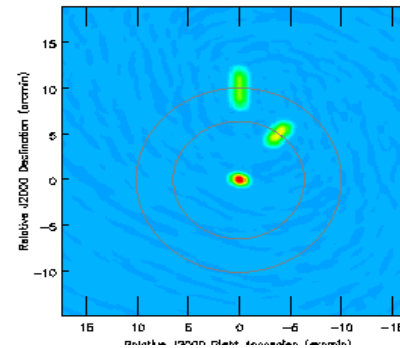
Bandwidth smearing limit for HPBW field-of-view :

$$\delta \nu < \frac{\nu_0 D}{b_{max}}$$

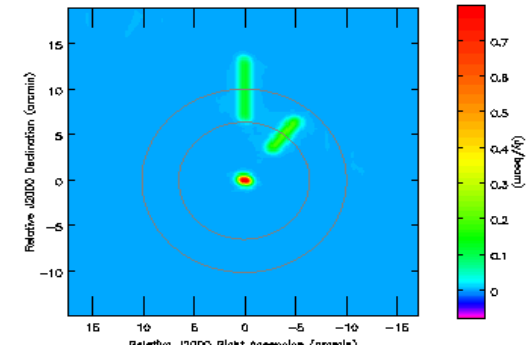
2 MHz



200 MHz



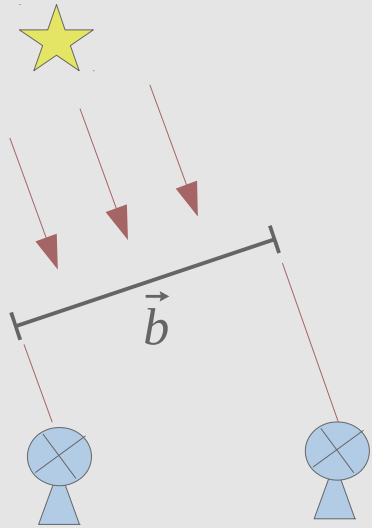
1.0 GHz



Bandwidth Smearing limits at L-Band (1.4 GHz),
33 MHz (VLA D-config), 10 MHz (VLA C-config),
3 MHz (VLA B-config), 1 MHz (VLA A-config)

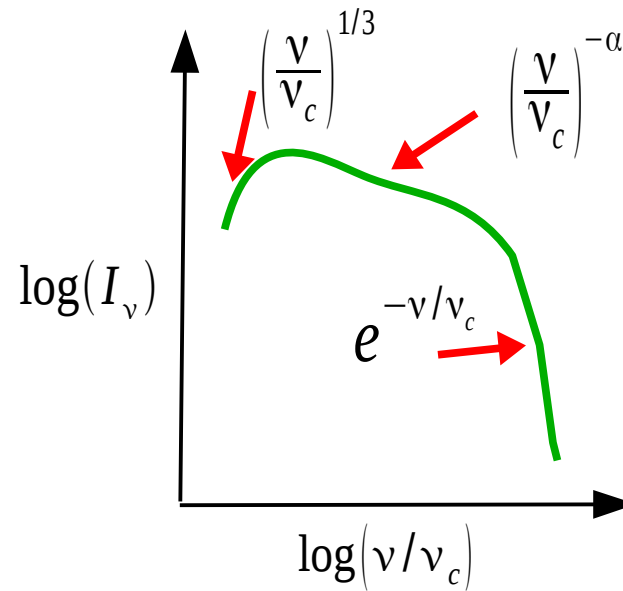
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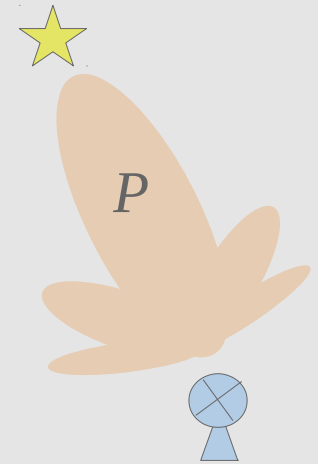
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Sky Brightness



$$I(\nu)$$

Primary Beam



$$HPBW_\nu = \frac{\lambda}{D} = \frac{c}{\nu D}$$

Imaging Equations

Narrow Band / Flat spectrum sky

$$I^{obs} = I^{sky} * PSF$$

$$I_{wb}^{obs} \approx I^{sky} * \left[\sum_v PSF_v \right]$$

Image reconstruction

= deconvolution : remove the effect of the instrument's response to a flat spectrum point source.

= non-linear fitting of a narrow-band model of the sky to the data

(Ref : Imaging and Deconvolution lecture)

Wide Band Sky with spectral structure

$$I_{wb}^{obs} = \sum_v \left[I_v^{sky} * PSF_v \right]$$

Wideband Image reconstruction

= Treat each frequency separately
(Ref : Spectral Line Analysis lecture)

(or)

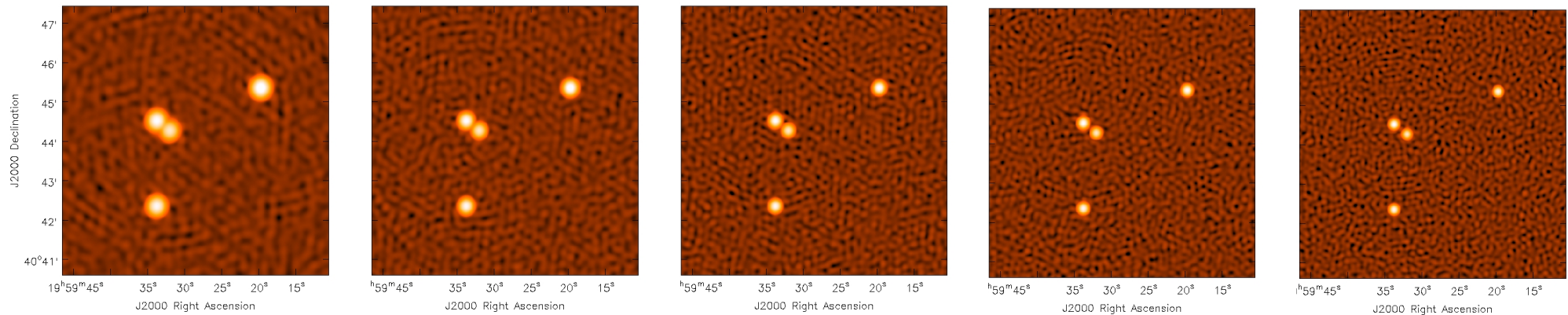
= joint deconvolution : remove the effect of the instruments response to a point source with spectral features

= non-linear fitting of a wide-band model of the sky to the data

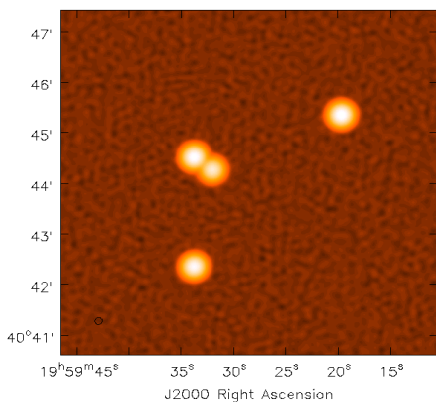
Single-channel vs MFS imaging – Angular Resolution

3 flat-spectrum sources + 1 steep-spectrum source (1-2 GHz)

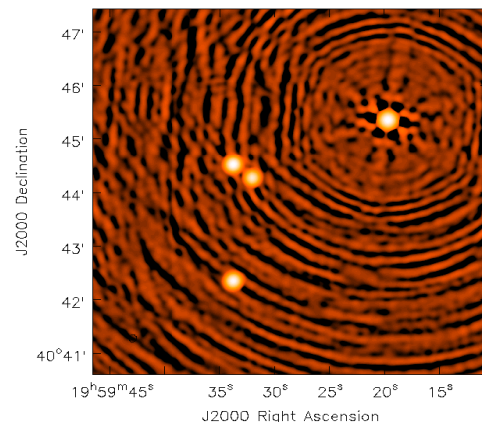
Images made at multiple frequencies (Spectral Cube / Image Cube)



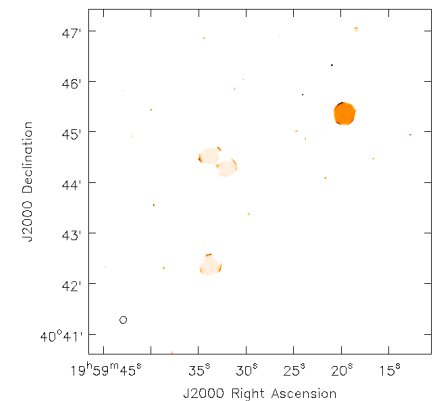
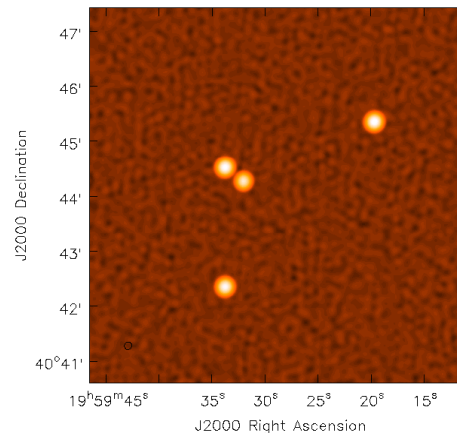
Combine
single-frequency
images (after
smoothing)



Do MFS using all
data, but ignore
spectra



Do MFS using all data
+ Model and fit for spectra too
= Intensity and Spectral-Index



Algorithm : Multi-Term MFS (with multi-scale)

Sky Model : Collection of multi-scale flux components whose amplitudes follow a Taylor polynomial in frequency

Reconstruction Algorithm : Linear least squares + deconvolution

Data Products : Taylor-Coefficient images $I_0^m, I_1^m, I_2^m, \dots$

that represent the sky spectrum $I_\nu^{sky} = \sum_t I_t \left(\frac{\nu - \nu_0}{\nu_0} \right)^t$

Interpretation :

- As a power-law (spectral index and curvature)

$$I_\nu = I_{\nu_0} \left(\frac{\nu}{\nu_0} \right)^{\alpha + \beta \log(\nu/\nu_0)} \quad \longleftrightarrow \quad I_0^m = I_{\nu_0} \quad I_1^m = I_{\nu_0} \alpha \quad I_2^m = I_{\nu_0} \left(\frac{\alpha(\alpha-1)}{2} + \beta \right)$$

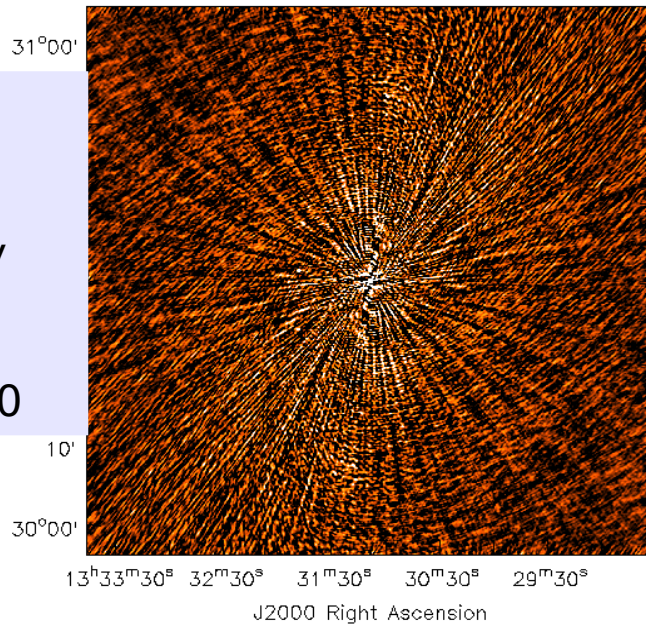
*Sault & Wieringa, 1994
Rau & Cornwell, 2011*

Dynamic-range with MS-MFS : 3C286 example : $N_t=1,2,3,4$

NTERMS = 1

Rms :
9 mJy -- 1 mJy

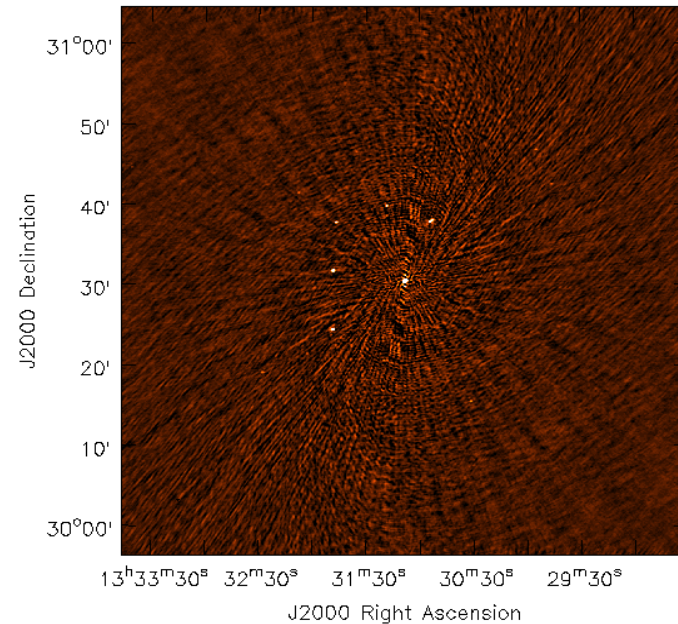
DR :
1600 - 13000



NTERMS = 2

Rms :
1 mJy -- 0.2 mJy

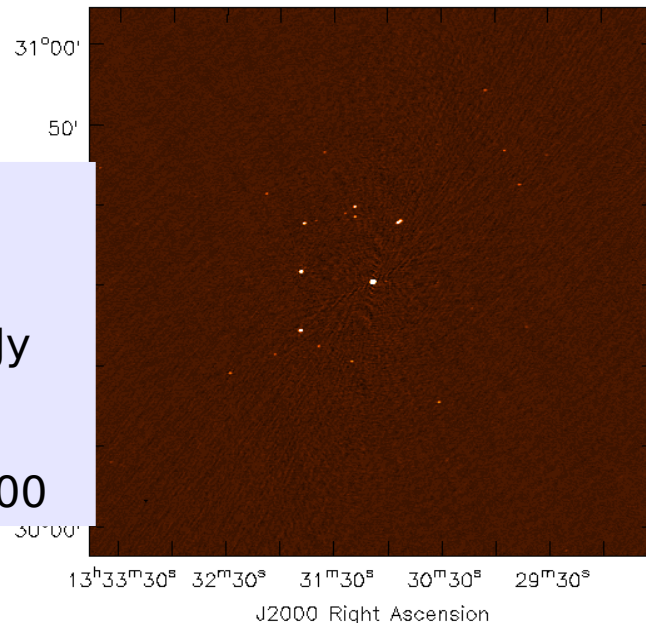
DR :
10,000 - 17,000



NTERMS = 3

Rms :
0.2 mJy -- 85 μ Jy

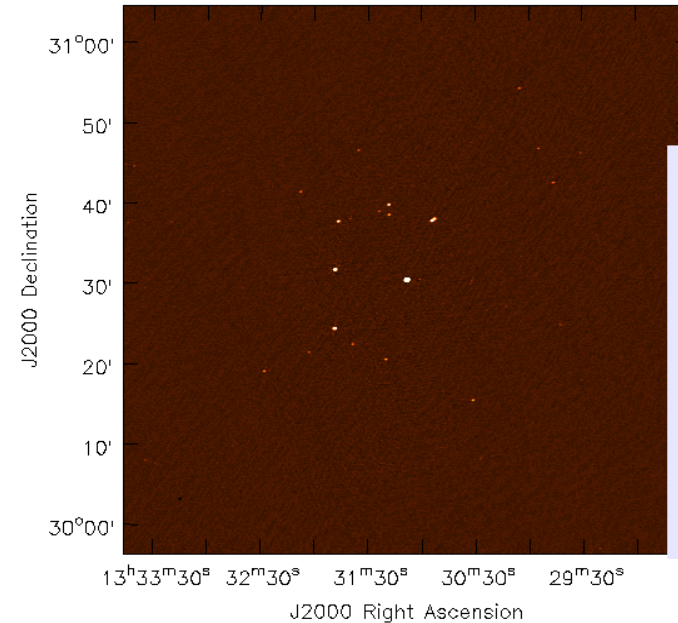
DR :
65,000 - 170,000



NTERMS = 4

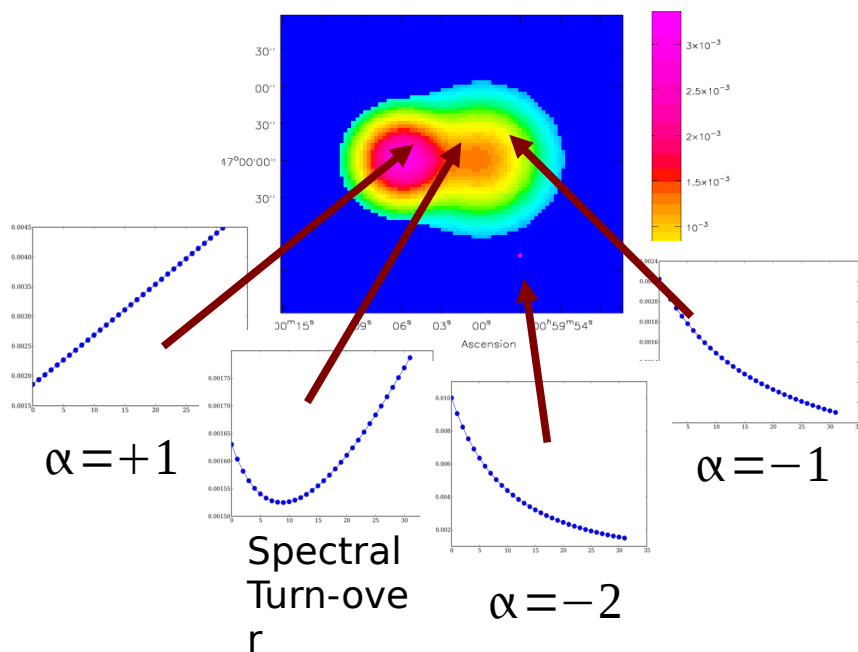
Rms
0.14 mJy -- 80 μ Jy

DR :
>110,000
- 180,000

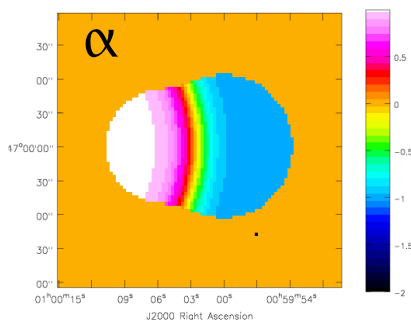


Example of wideband-imaging on extended-emission

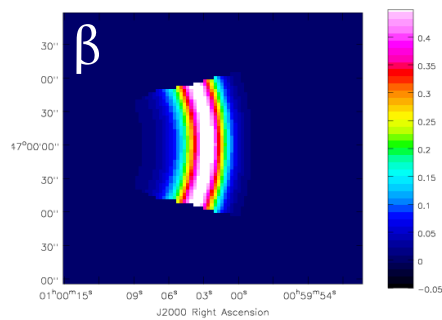
Intensity Image



Average Spectral Index

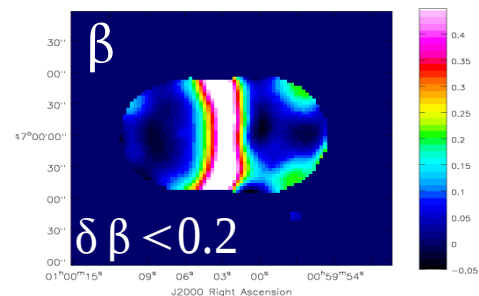
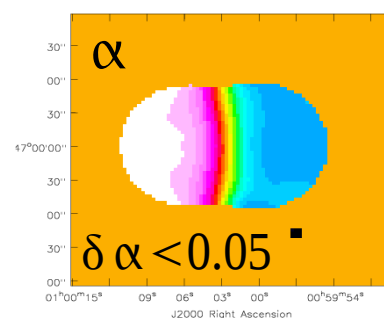
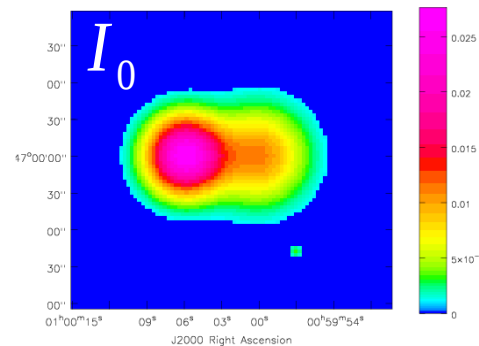


Gradient in Spectral Index

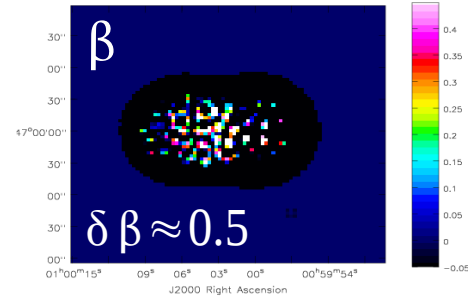
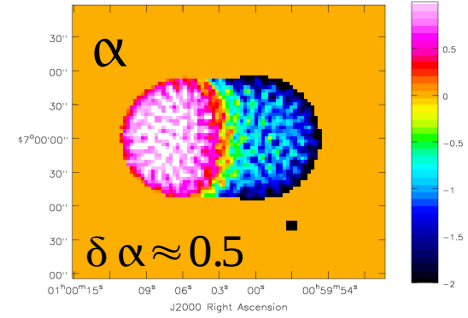
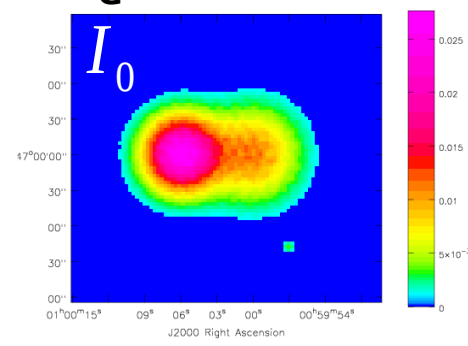


MFS

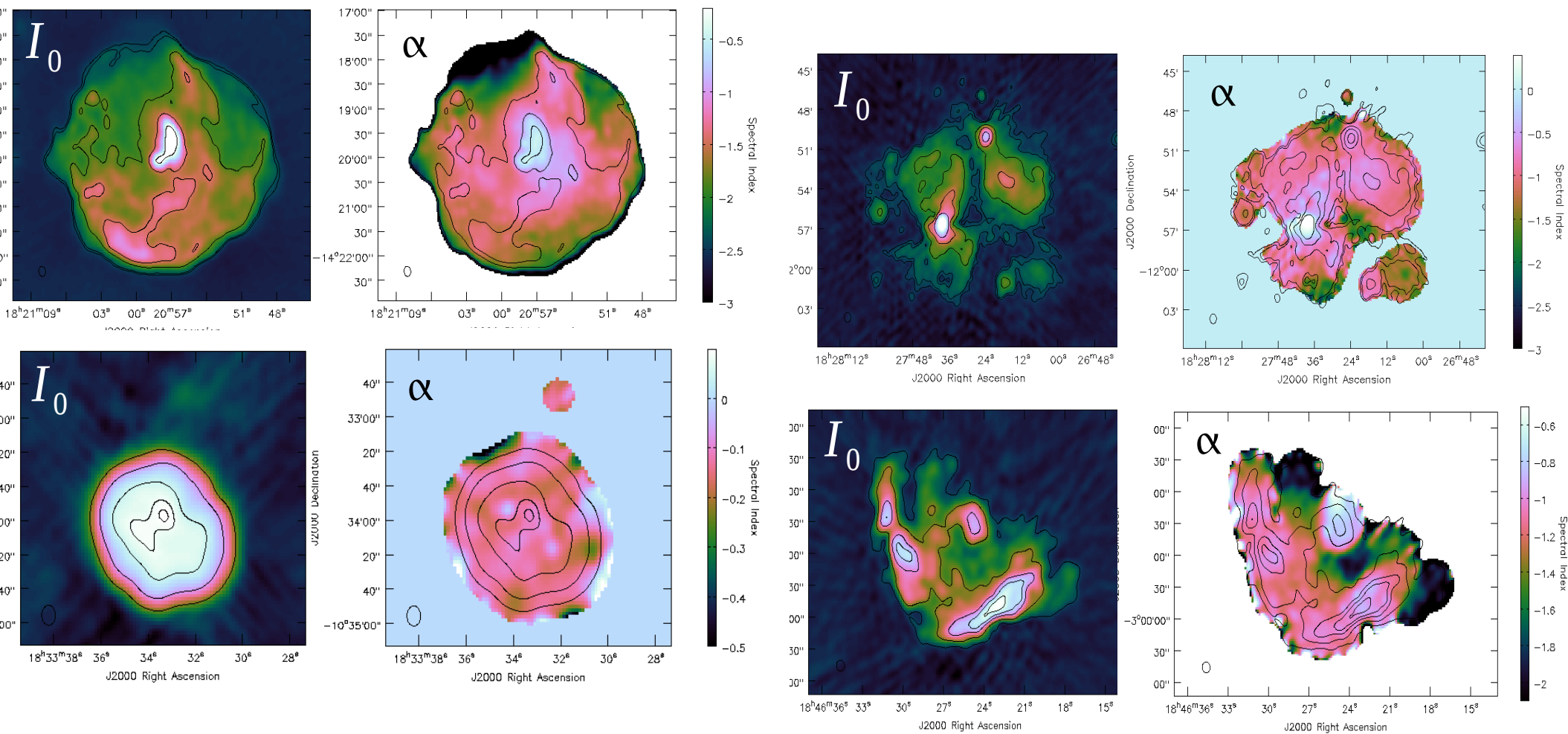
multi-scale



point-source



=> Spectral-index error is dominated by 'division between noisy images'
 - a multi-scale model gives better spectral index and curvature maps



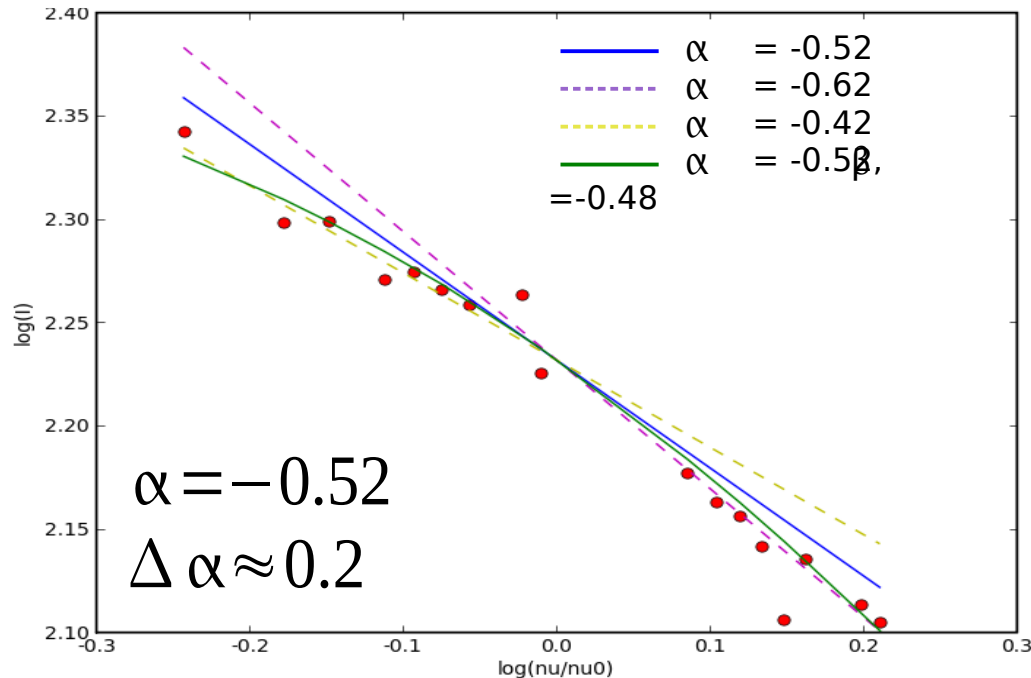
These examples used $n_{\text{terms}}=2$, and about 5 scales.

=> Within 1-2 GHz and 4-8 GHz, spectral-index error is < 0.2 for $\text{SNR} > 100$.

=> Dynamic-range limit of few $\times 1000$ ---> residuals are artifact-dominated

Spectral Curvature

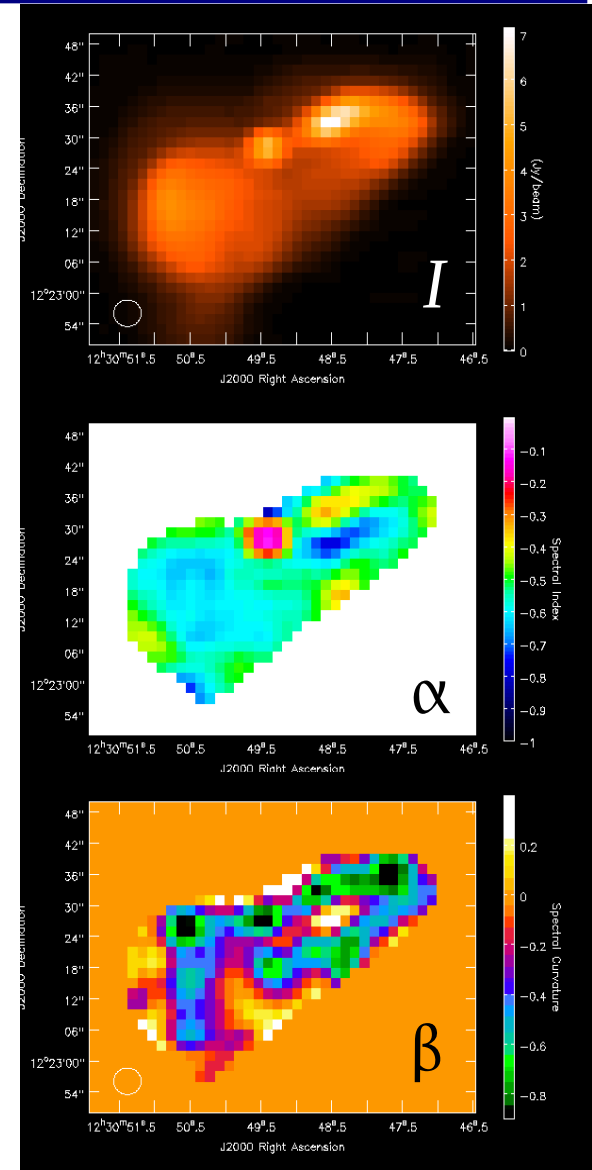
Data : 10 VLA snapshots at 16 frequencies (1.2 – 2.1 GHz)



From existing P-band (327 MHz), L-band(1.42 GHz) and C-band (5.0 GHz) images of the core/jet

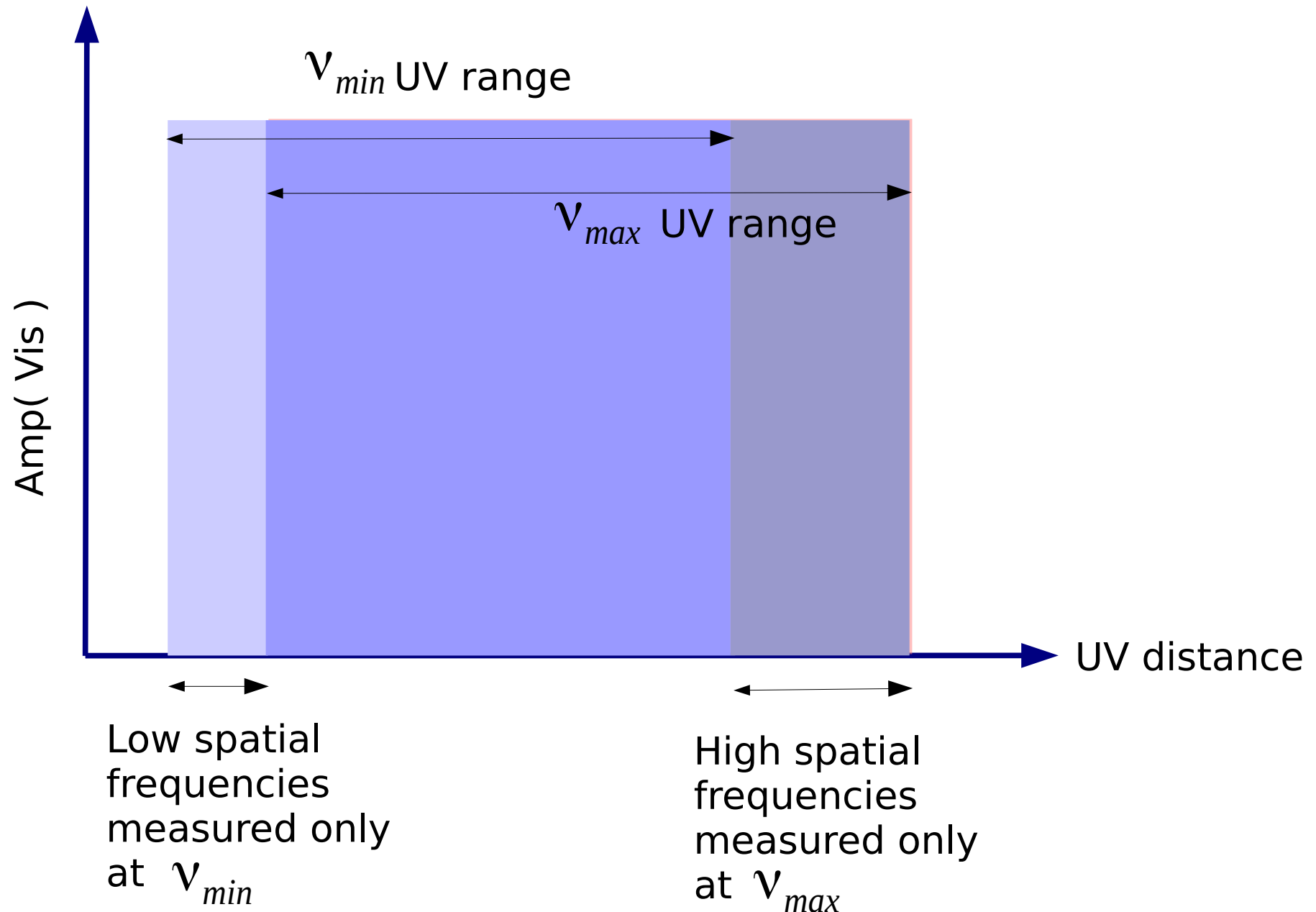
P-L spectral index : $-0.36 \sim -0.45$

L-C spectral index : $-0.5 \sim -0.7$

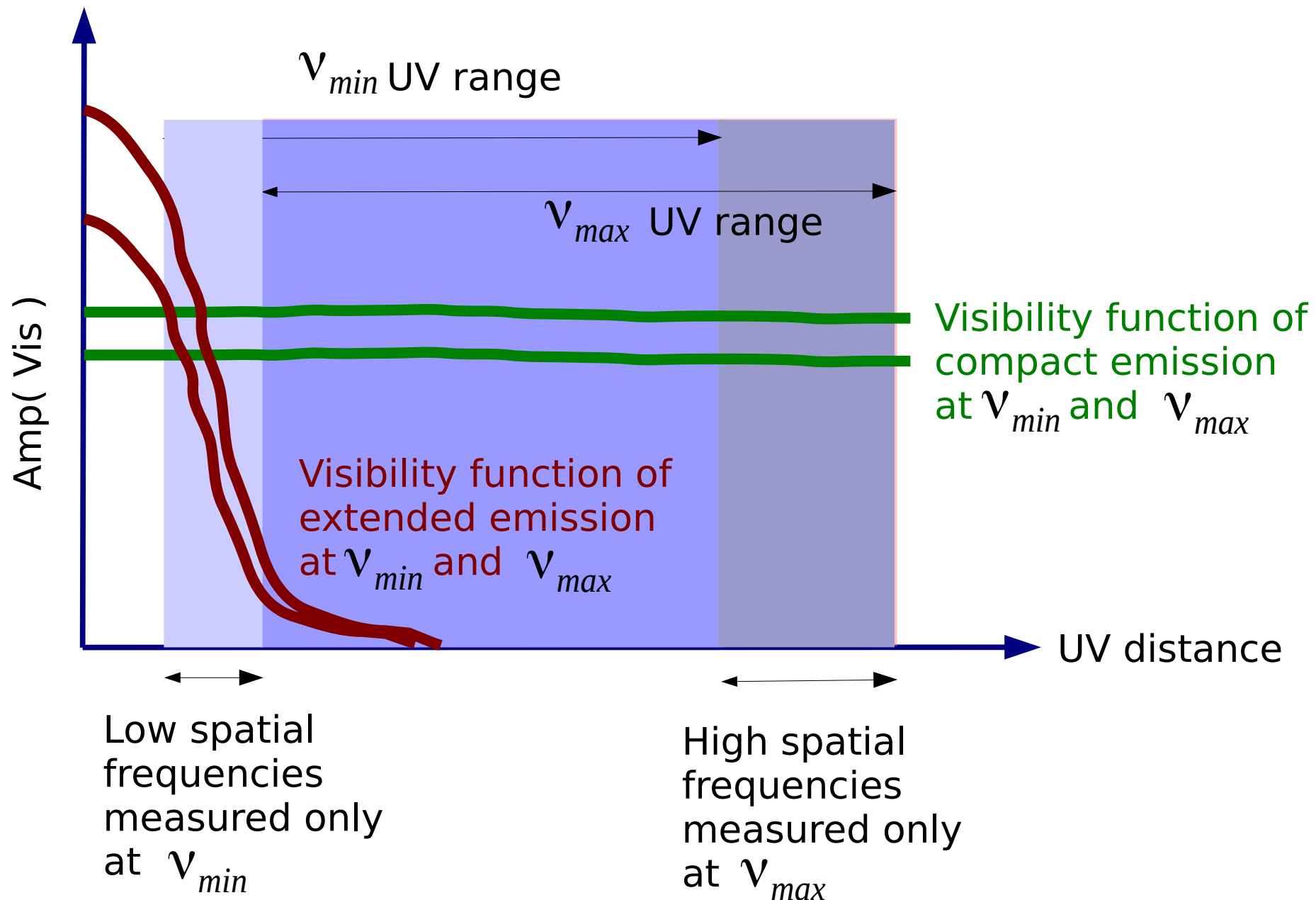


\Rightarrow Need SNR > 100 to fit spectral index variation ~ 0.2 (at the 1-sigma level ...)
 \Rightarrow Be very careful about interpreting β

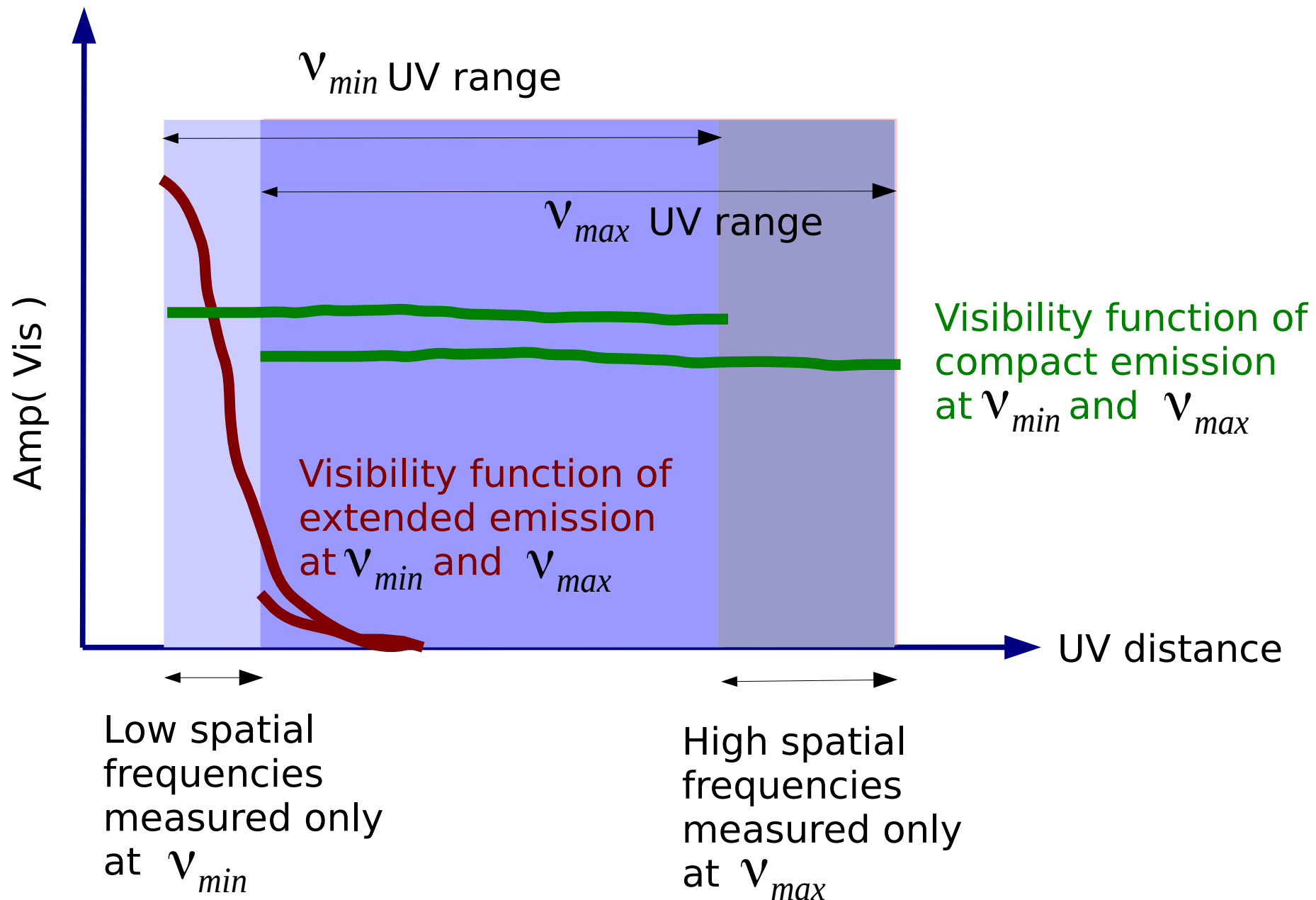
For which scales can we reconstruct the spectrum ?



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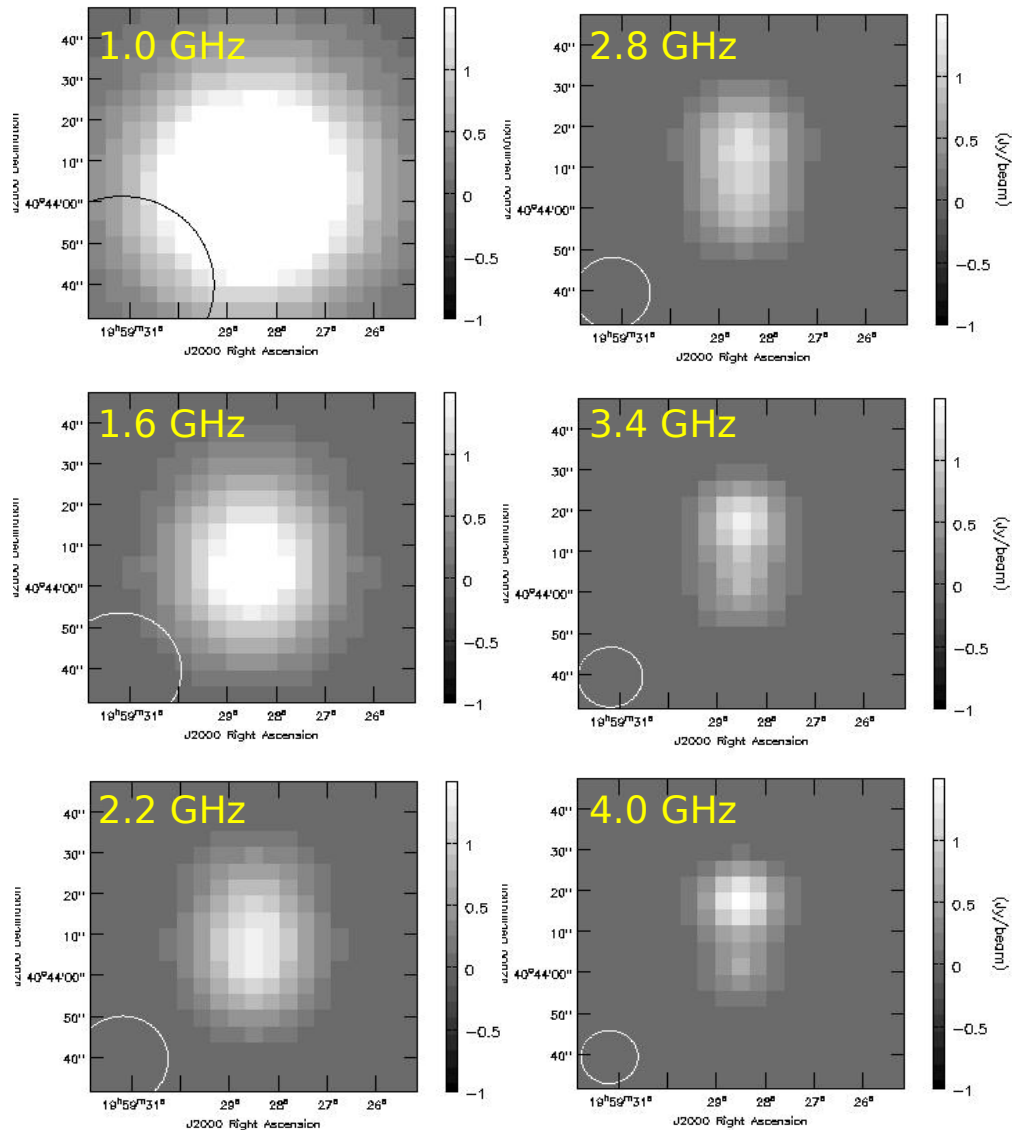


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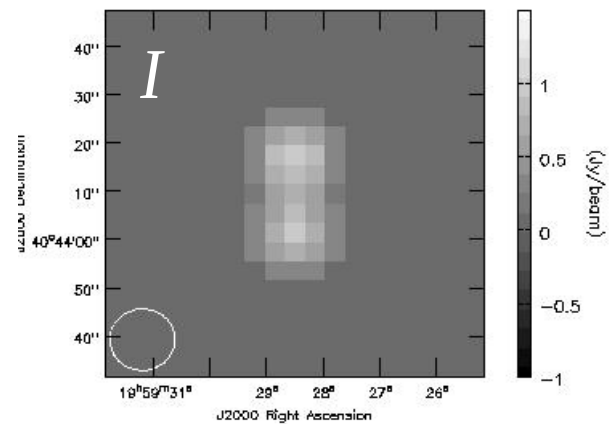


Moderately Resolved Sources + High SNR

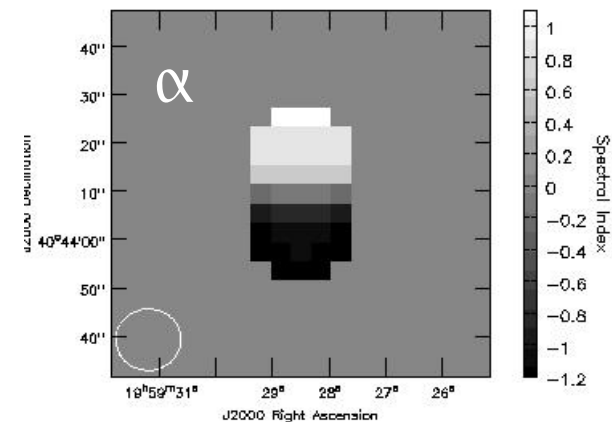
Can reconstruct the spectrum at the angular resolution of the highest frequency (only high SNR)



Restored Intensity image

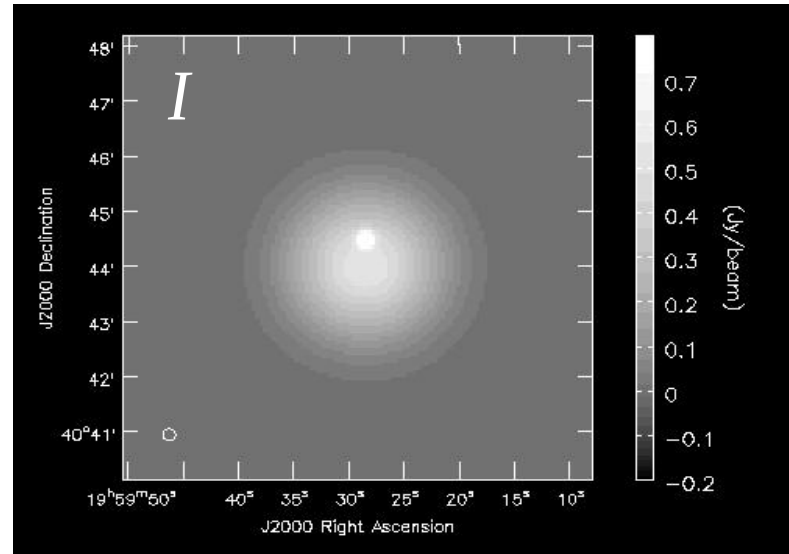
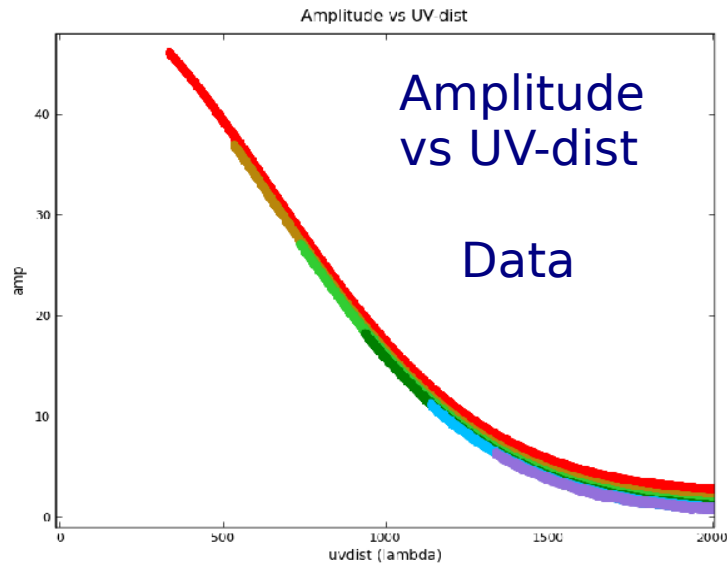


Spectral Index map

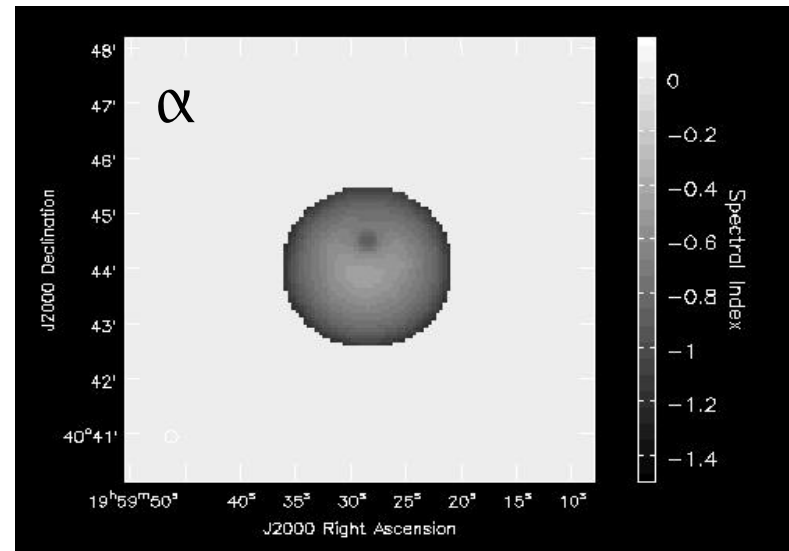
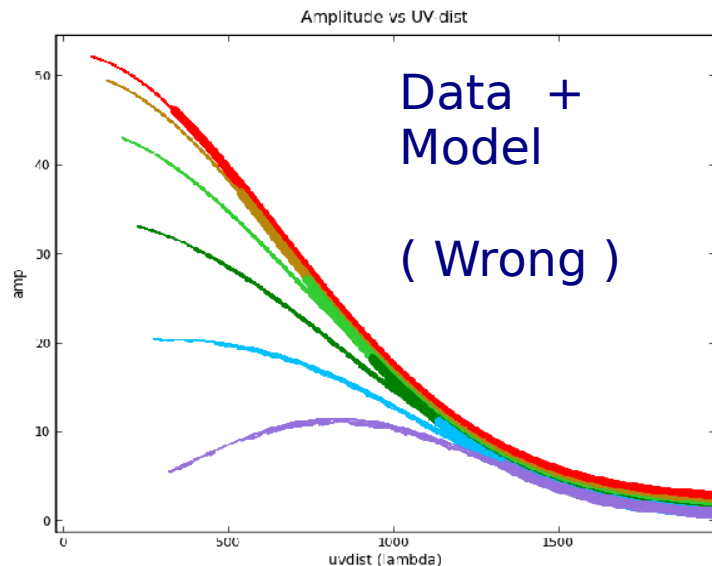


Very large spatial scales – Unconstrained spectrum

The spectrum at the largest spatial scales is NOT constrained by the data



True sky has one steep spectrum point, and a flat-spectrum extended emission

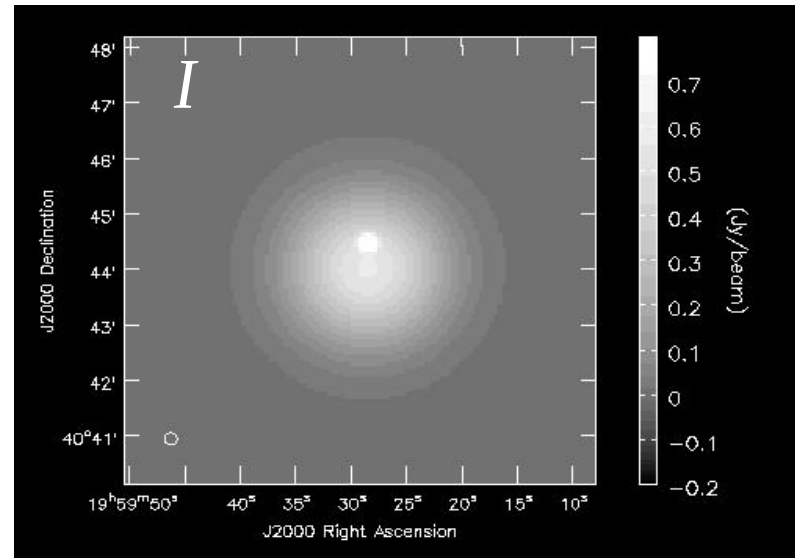
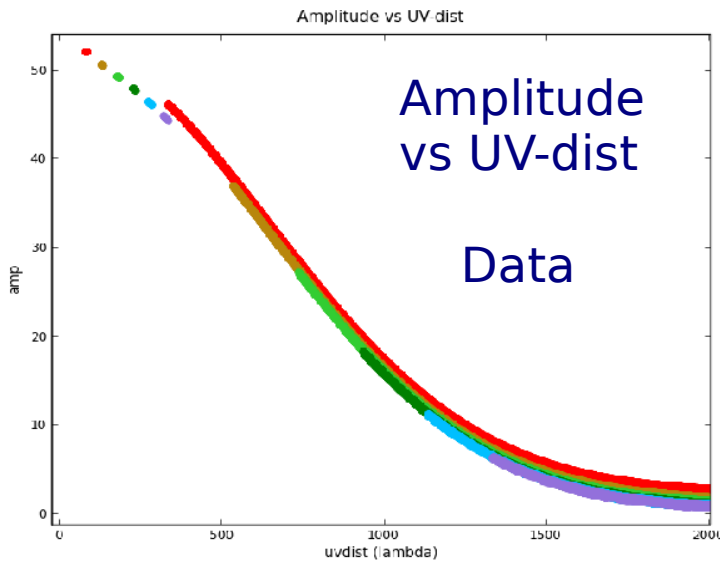


No short spacings to constrain the spectra

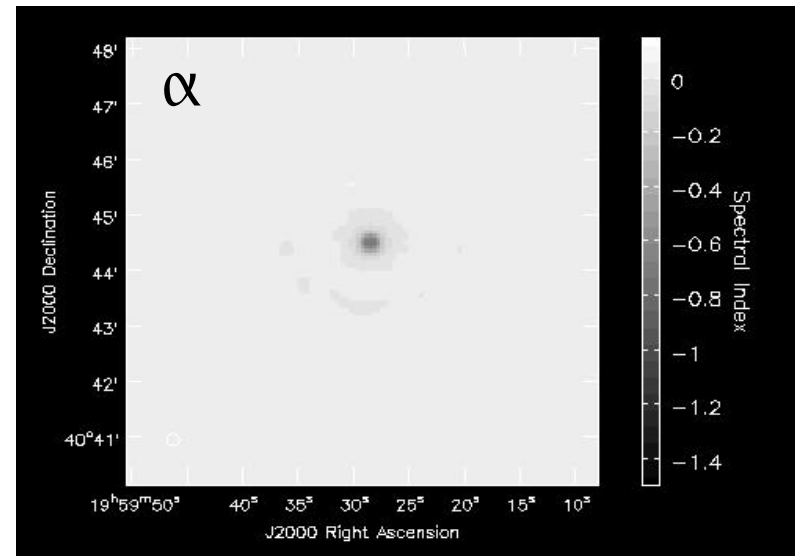
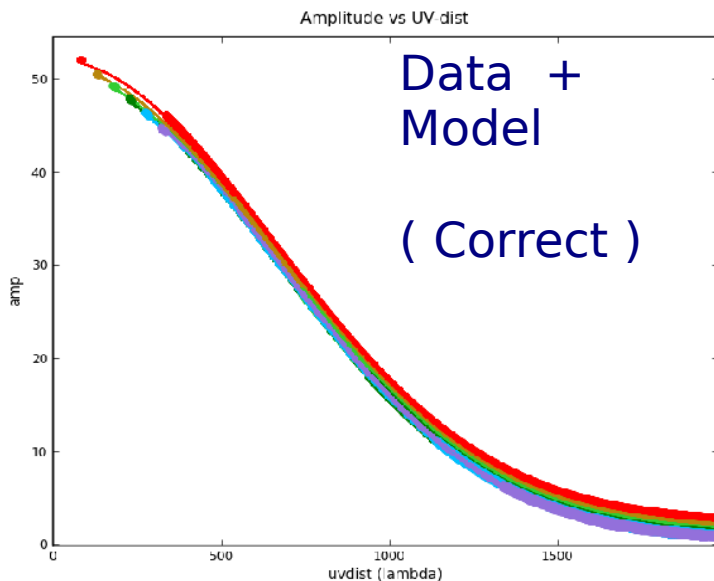
=> False steep spectrum reconstruction

Very large spatial scales – Need additional information

External short-spacing constraints (visibility data, or starting image model)



True sky has one steep spectrum point, and a flat-spectrum extended emission

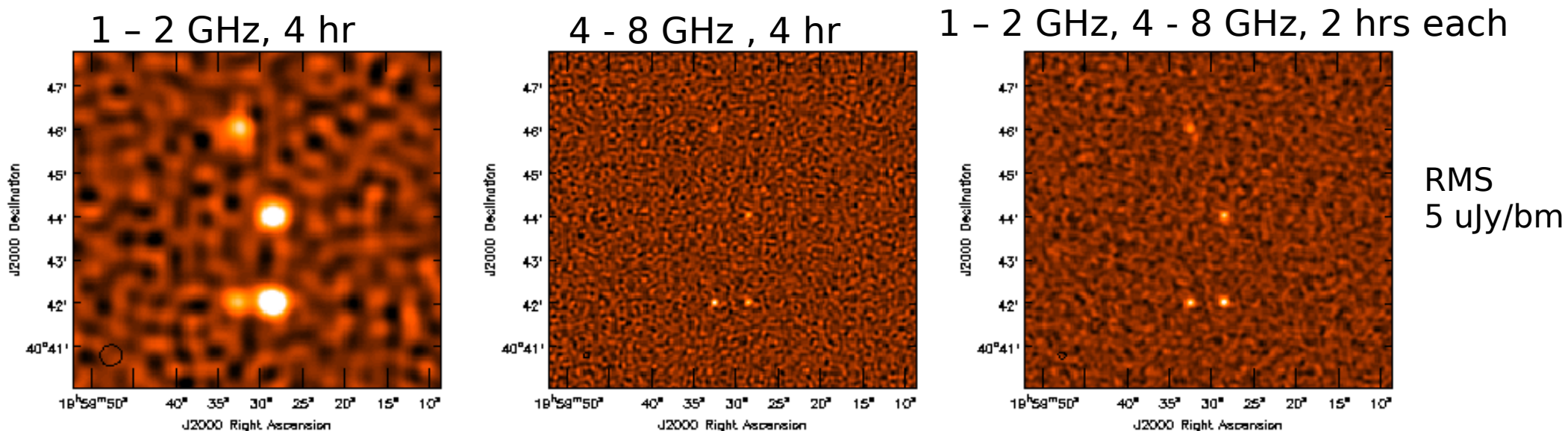


With short spacing info,

Correct reconstruction of a flat spectrum

Spectral Index Accuracy (for low signal-to-noise)

Accuracy of the spectral-fit increases with larger bandwidth-ratio

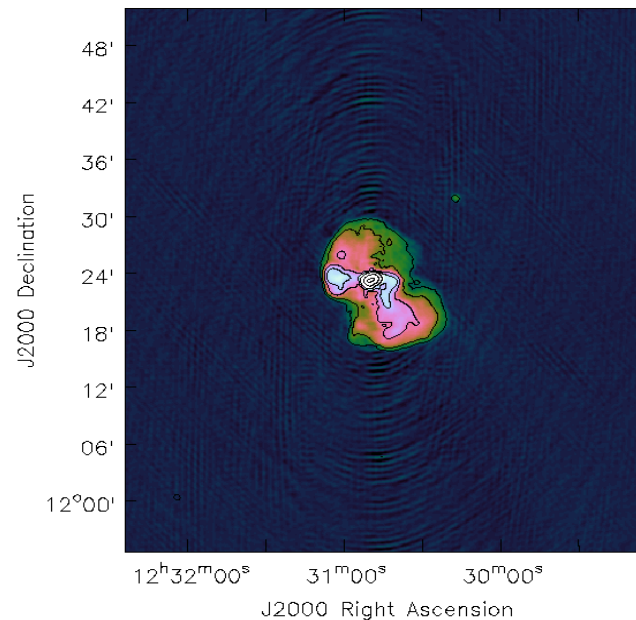
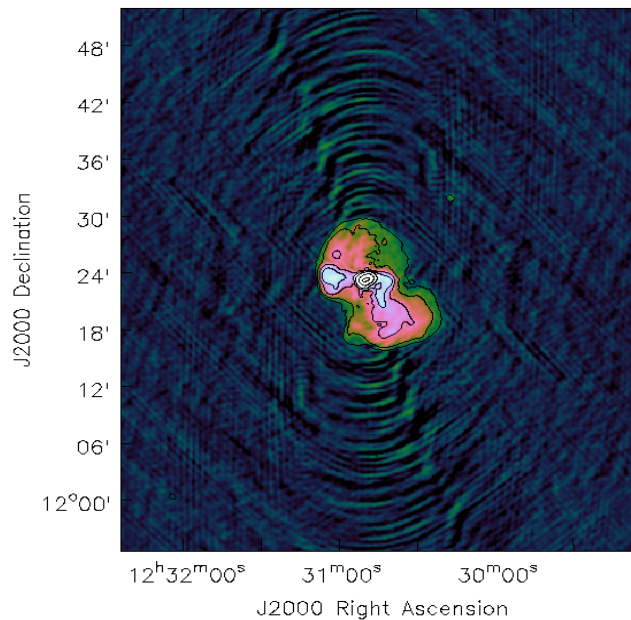


Source	Peak Flux	SNR	L alpha	C alpha	LC alpha	True
Bottom right	100 μ Jy	20	-0.89	-1.18	-0.75	-0.7
Bottom left	100 μ Jy	20	+0.11	+0.06	+0.34	+0.3
Mid	75 μ Jy	15	-0.86	-1.48	-0.75	-0.7
Top	50 μ Jy	10	-1.1	0	-0.82	-0.7

To trust spectral-index values, need SNR > 50 (within one band – 2:1)
For SNR < 50 need larger bandwidth-ratio.

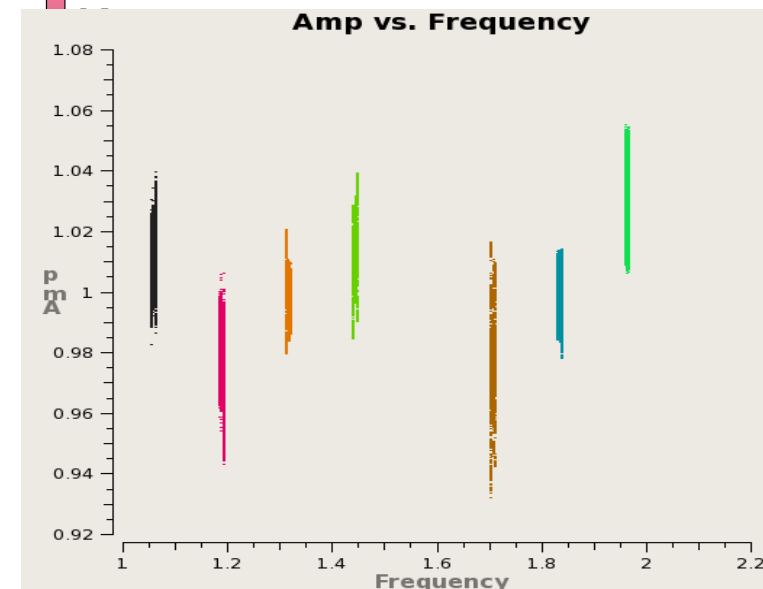
Wide-band Self-Calibration (for HDR imaging)

- First, get a wide-band sky model.
- Follow with 'bandpass' calibration
- Check amplitude solutions carefully before applying them.
(easy to impose an artificial spectrum on your data)



Dynamic range improved from ~2000 to ~4000.

Amplitudes of bandpass gain solutions
(< 5% from 1.0)

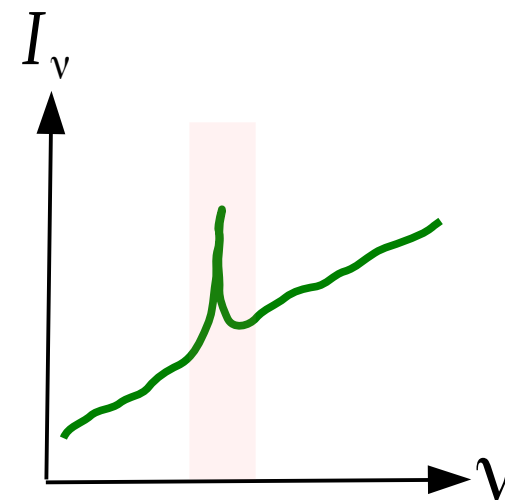


In these VLA data (of M87), each SPW had been calibrated, imaged, and phase self-cal'd separately, prior to joint MFS imaging and **wide-band self-cal to smooth out the spectrum.**

Using Wide-Band Models for other processing....

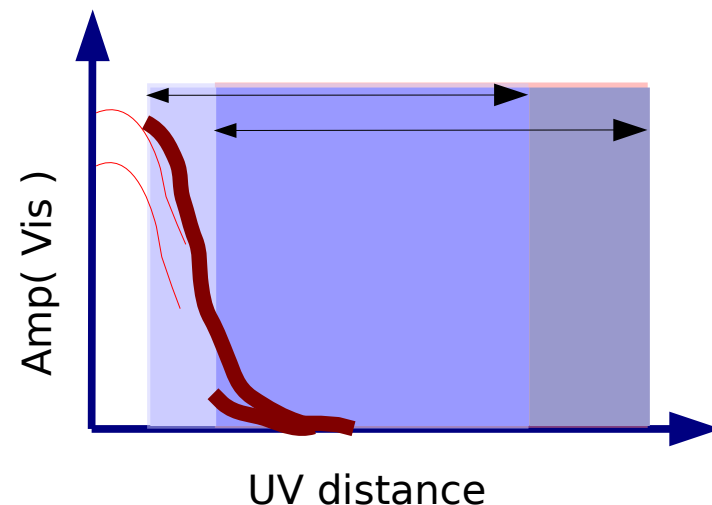
(1) Continuum Subtraction

- De-select frequency channels with spectral-lines
- Make a wide-band image model
- Predict model-visibilitys over **all** channels
- Subtract these model visibilities from the data



(2) Combining with single-dish data

- Make Taylor-coefficient maps from multi-frequency single-dish images
- Use as a starting model in the MT-MFS interferometric reconstruction



Stokes Q,U,V can also change with frequency

- If the expected variation $< \sim 1\%$ of the peak, MFS (nt=1) will suffice
- If not, it is safest to make a Cube (as the spectra may not smooth)

Faraday Rotation-Measure Synthesis

Images of polarized surface-brightness at various Faraday-depths : $F(\phi)$

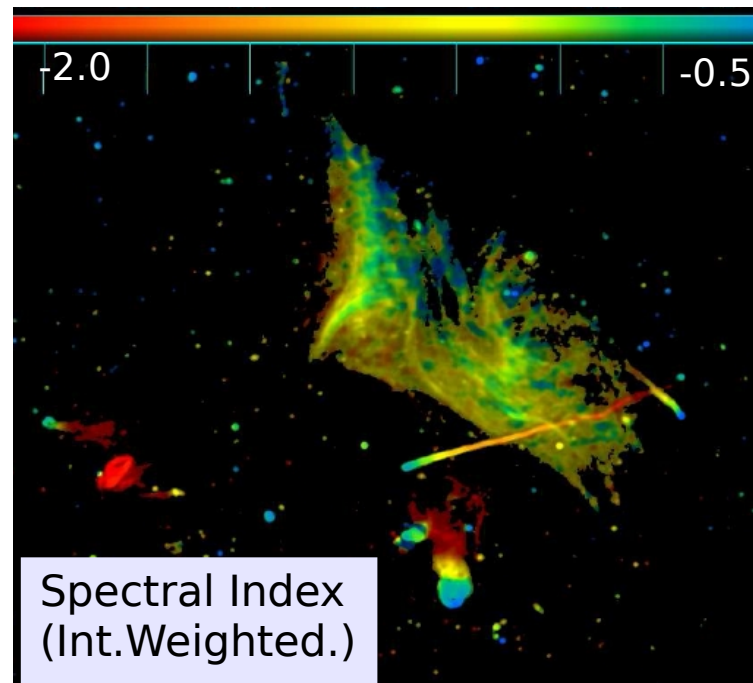
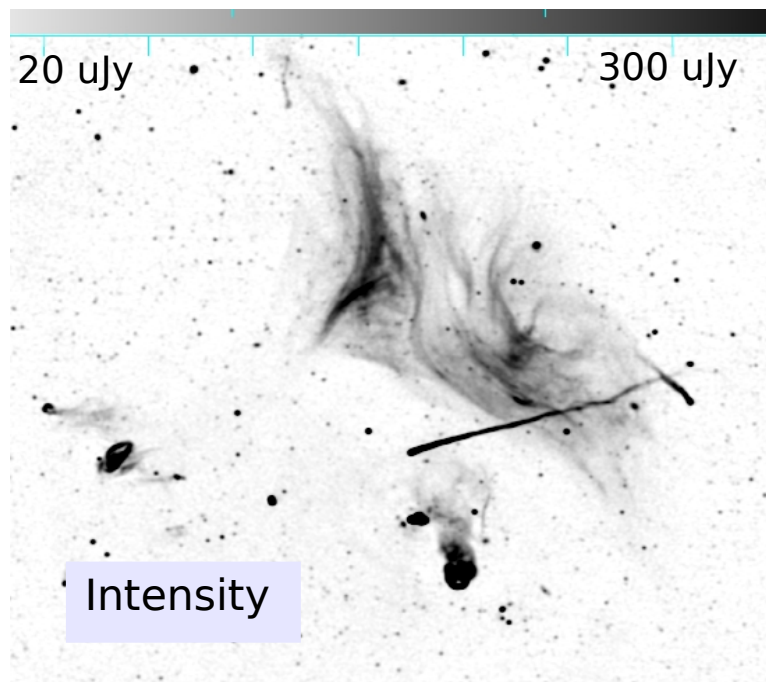
- $P = Q + i U$: Make spectral cubes for Q and U separately, and calculate P
- For each pixel in the P-cube, solve $P(\lambda^2) = \int F(\phi) e^{2\pi i \phi \lambda^2} d\phi$ for $F(\phi)$

Brentjens, 2008, Bell et al, 2013

This calculation is currently done post-deconvolution, but it could be folded into the image reconstruction framework.

(Ref : Polarization in Interferometry" lecture)

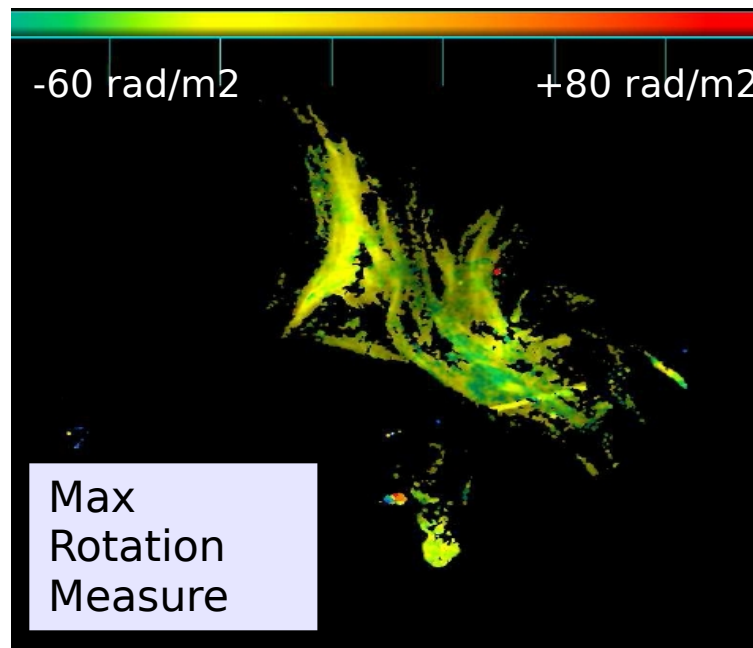
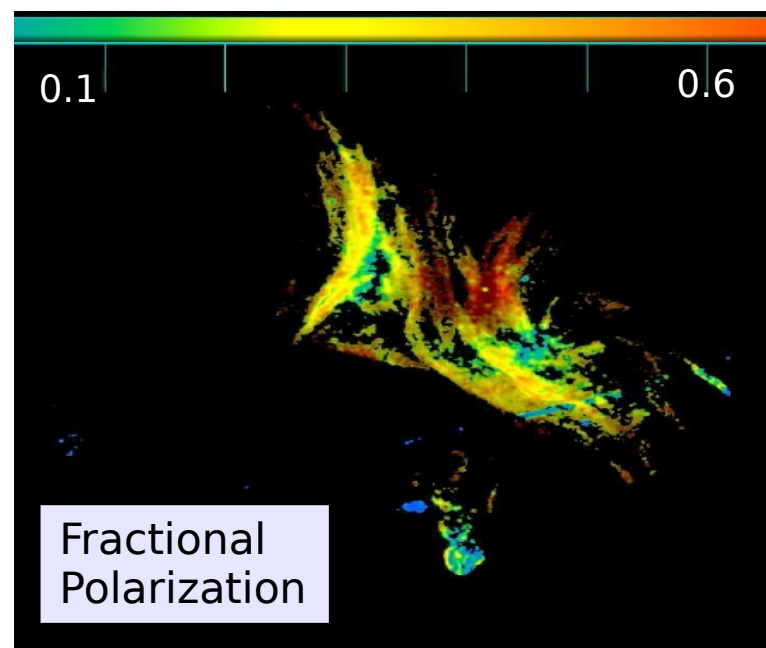
Wideband VLA imaging of Abell 2256 [Owen et al, 2014]



VLA A,B,C,D at
L-Band (1-2 GHz)

VLA A, at S&C
bands(2-4, 4-6,
6-8 GHz)

Calibration and
Auto-flagging in
AIPS.

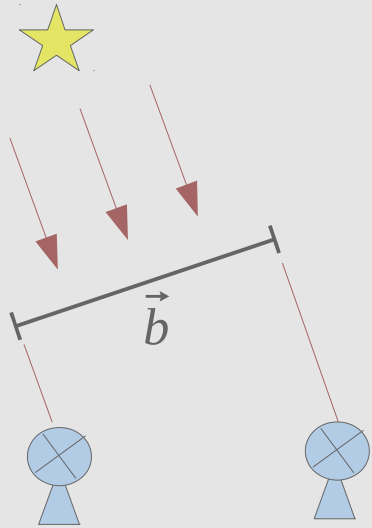


Intensity and
Spectral index
Imaging in CASA.
(with Pbcor only
post-deconv.)

Polarization and
Rotation Measure
Imaging in AIPS.

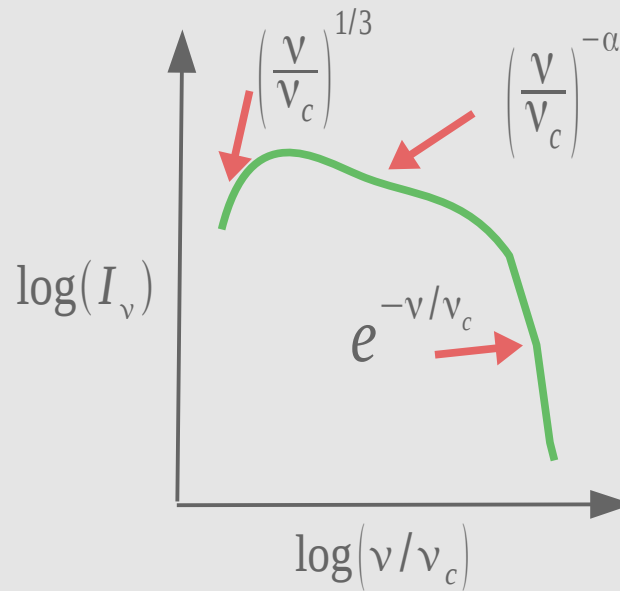
The instrument and the sky change with frequency...

UV-coverage



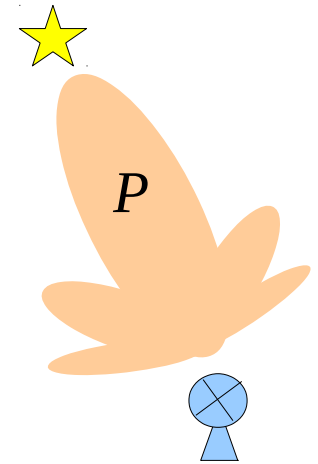
$$S(u, v)_\nu = \frac{\vec{b}}{\lambda} = \frac{\vec{b} \nu}{c}$$

Sky Brightness



$$I(\nu)$$

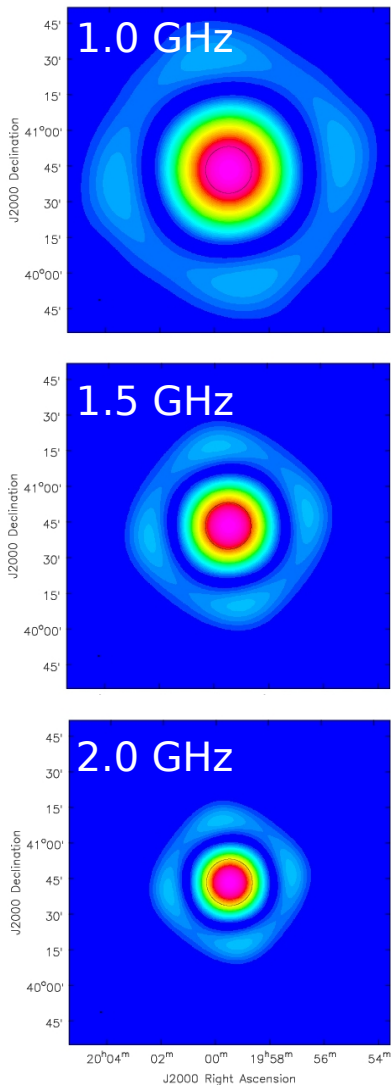
Primary Beam



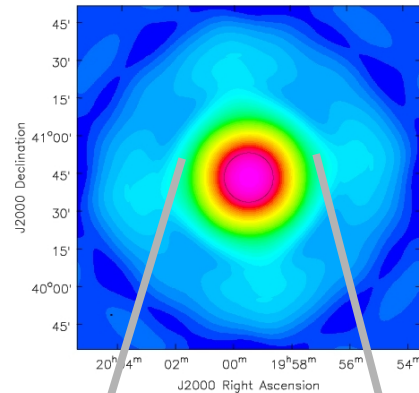
$$HPBW_\nu = \frac{\lambda}{D} = \frac{c}{\nu D}$$

Wide-Band Wide-Field Imaging : Primary Beams

VLA PBs



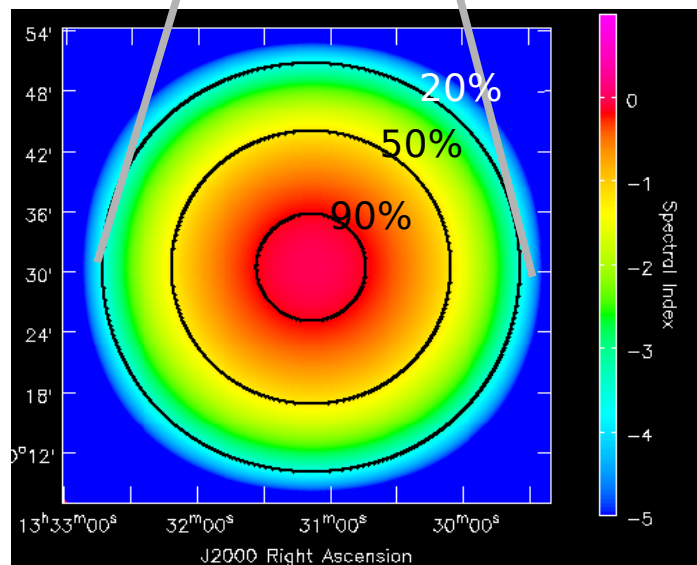
Average Primary Beam



MFS : artificial 'spectral index' away from the center

For VLA L-Band (1-2 GHz)

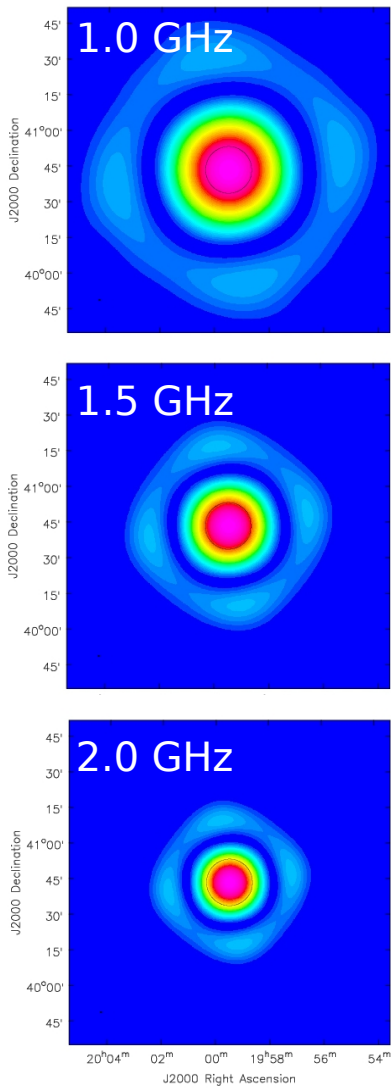
- About -0.4 at the PB=0.8 (6 arcmin from the center)
- About -1.4 at the HPBW (15 arcmin from the center)



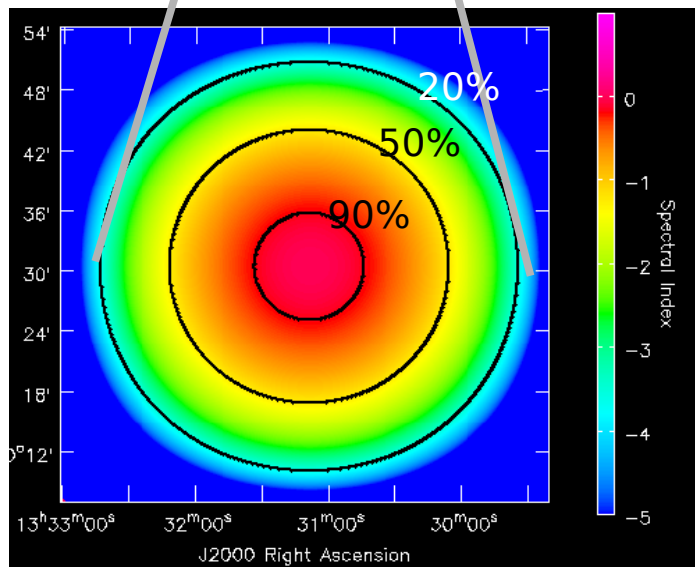
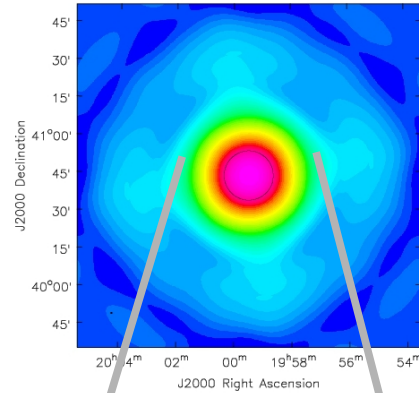
Spectral Index of PB

Wide-Band Wide-Field Imaging : Primary Beams

VLA PBs



Average Primary Beam



Spectral Index of PB

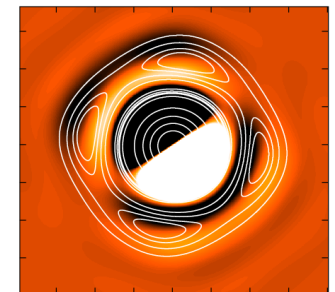
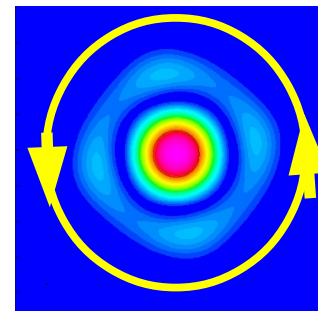
MFS : artificial 'spectral index' away from the center

For VLA L-Band (1-2 GHz)

- About -0.4 at the PB=0.8 (6 arcmin from the center)
- About -1.4 at the HPBW (15 arcmin from the center)

Primary beams also

- rotate with time
- have polarization structure (beam squint, etc...)



(Ref: Wide-Field Imaging – Full Beams lecture)

Wide-Band Primary Beam Correction

Cube Imaging

- Sky model represents $I(\nu)P(\nu)$
- Divide the output image at each frequency by $P(\nu)$

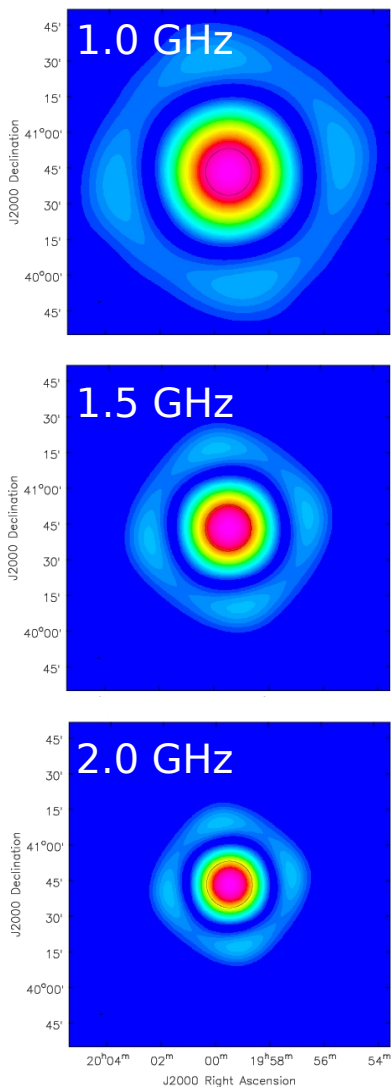
Multi-Term MFS Imaging

- Taylor coefficients represent $I(\nu)P(\nu)$
- Polynomial division by PB Taylor coefficients

$$\frac{(I_0^m, I_1^m, I_2^m, \dots)}{(P_0, P_1, P_2, \dots)} = (I_0^{sky}, I_1^{sky}, I_2^{sky}, \dots)$$

Wideband A-Projection

- Remove $P(\nu)$ during gridding (before model fitting)
- Also handles PB rotation/squint
- Output spectral index image represents only the sky



Imaging Options : MT-MFS [y/n], A-Projection [y/n]

MT-MFS

Multi-term MFS (wideband) Imaging
+
Absorb PB spectrum into sky model
+
Post-deconvolution Wideband PBcor
for intensity and alpha

Sault & Wieringa 1994, Rau & Cornwell, 2011

MT-MFS + WB-A-Projection

Multi-term MFS with wideband A-Projection
to remove PB spectrum during gridding
+
Minor cycle sees only sky spectrum
+
Post-deconvolution PBcor of intensity only.

Bhatnagar, Rau, Golap, 2013

Cube

Per channel Hogbom/Clark/CS Clean
+
Per channel post-deconvolution Pbcor
+
Smooth to lowest resolution
+
Fit spectrum per pixel, collapse chans

*Hogbom 1974, Clark 1980, Schwab & Cotton 1983,
Schwarz, 1978*

Cube + A-Projection

Same as Cube,
- with narrow-band A-Projection
per channel

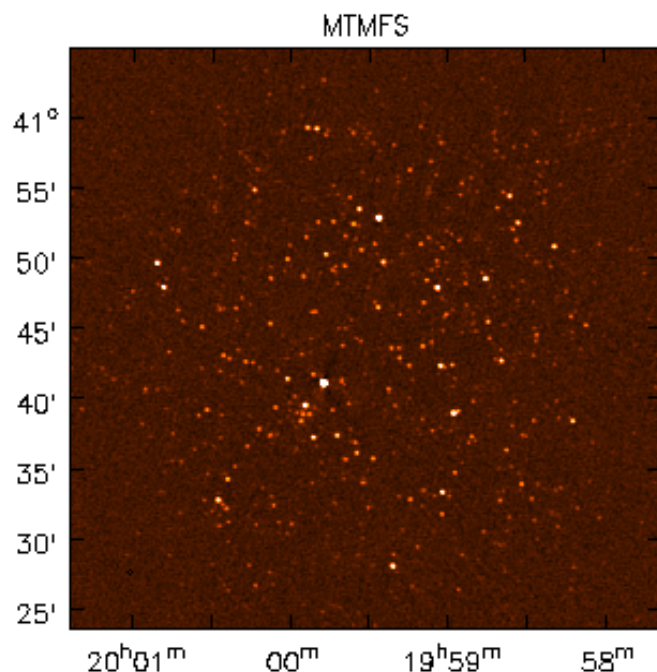
(A-Projection : Construct gridding
convolution operators from antenna
aperture illumination models. Removes
beam squint and accounts for aperture
rotation)

Bhatnagar, Cornwell, Golap, Uson, 2004

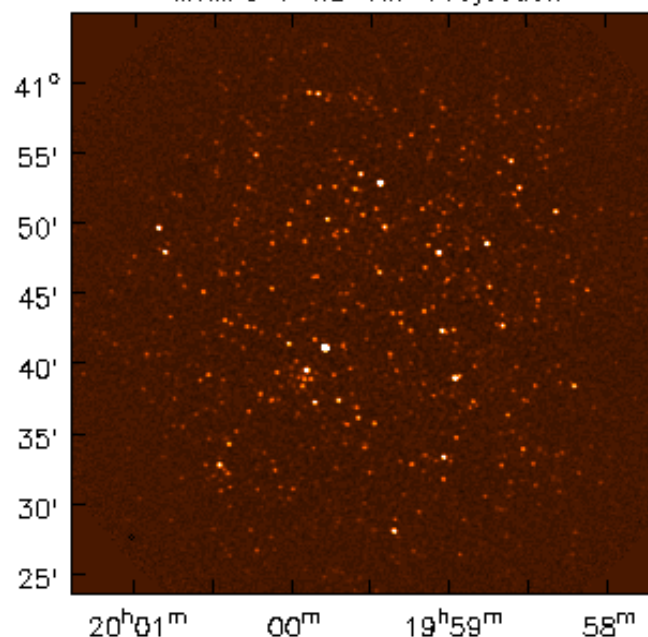
Low dynamic range test ($< 10^4$) – compare four methods

MT-MFS

2 μ Jy rms



MTMFS + WB-AW-Projection



MT-MFS
+
WB-AWP

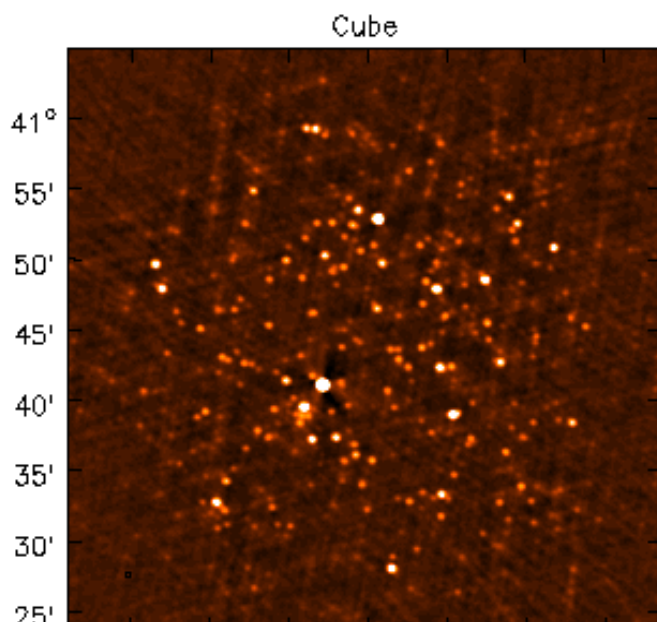
2 μ Jy rms

Brightest
Source :
7 mJy

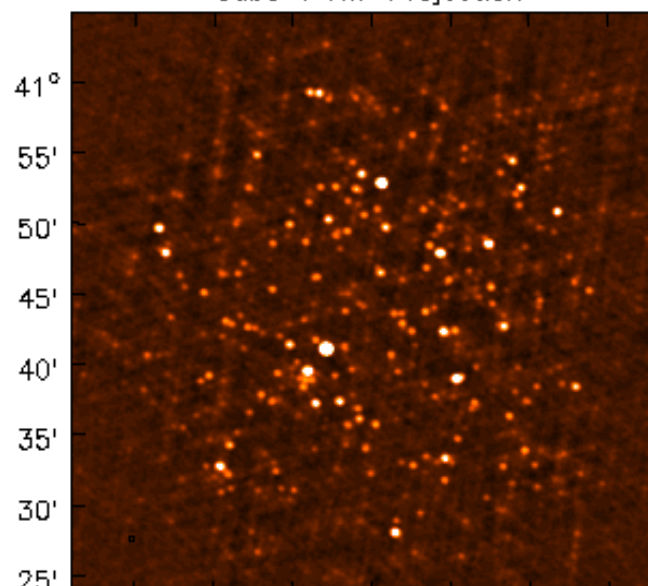
Cube

3 μ Jy rms

peak res :
9 μ Jy



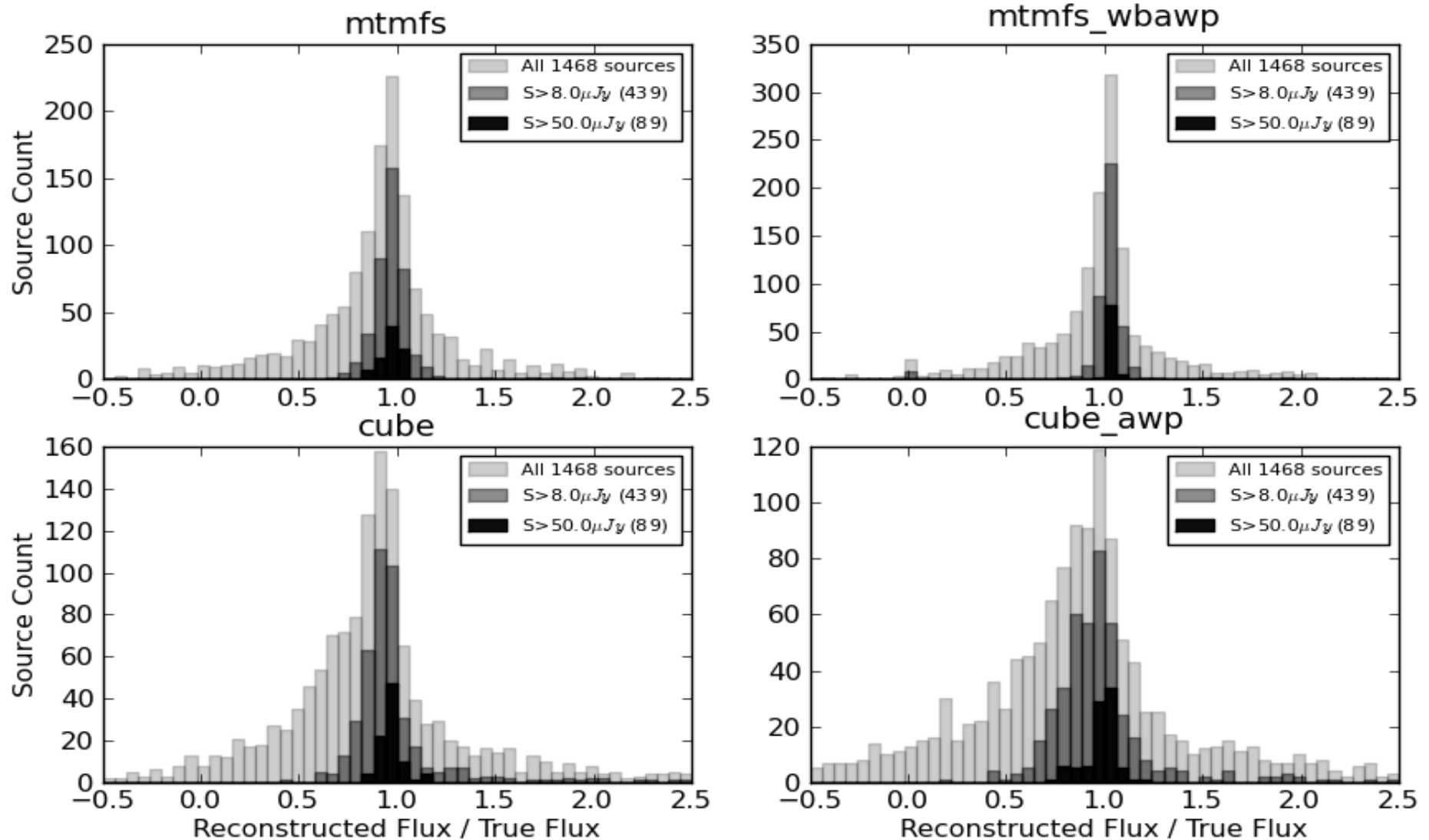
Cube + AW-Projection



Cube
+
AWP

3 μ Jy rms

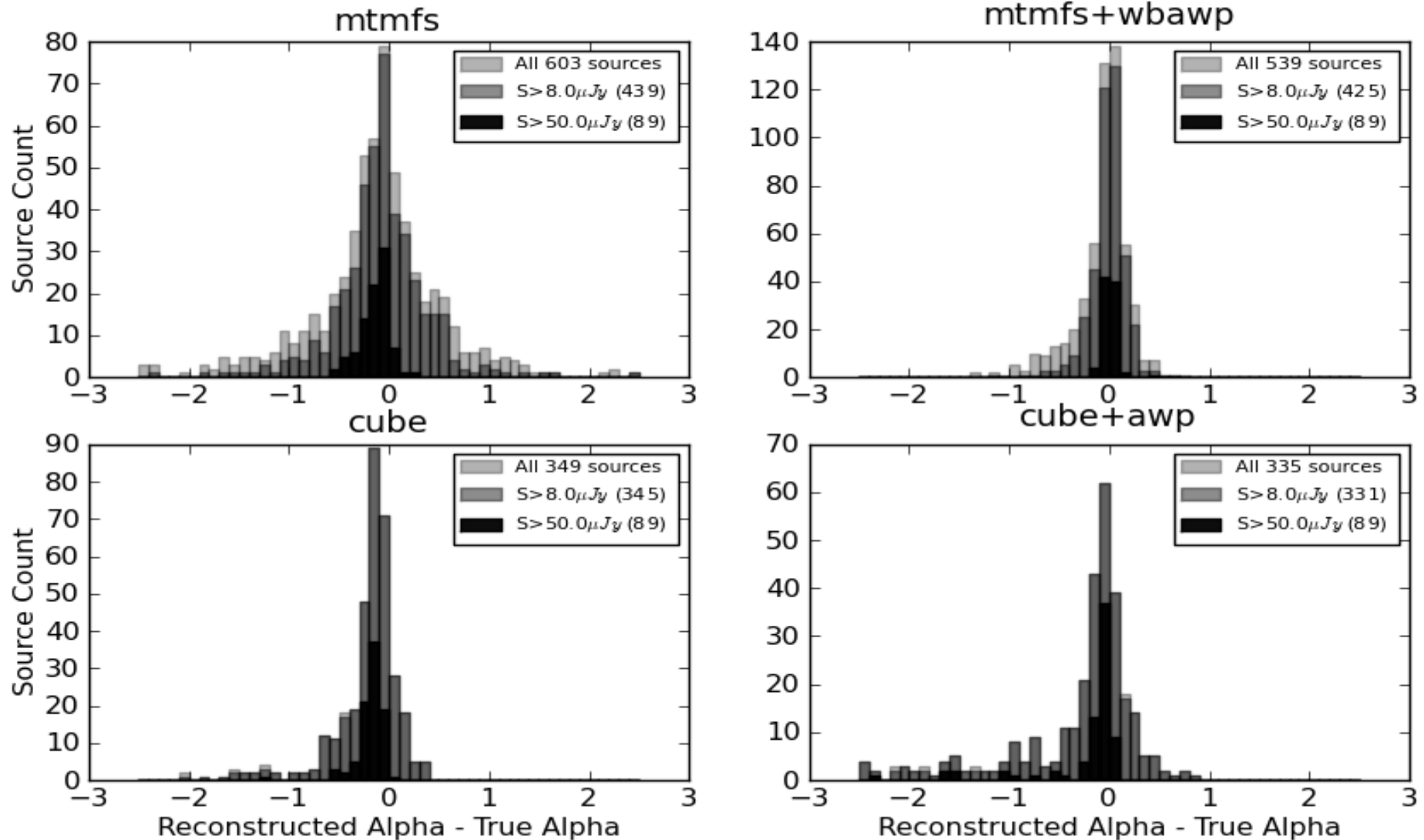
Histogram of Reconstructed / True Intensity



=> Brighter sources and MFS methods are more accurate

(Different shades in the plots indicate different source intensity ranges)

Histogram of Reconstructed – True Spectral Index



=> Spectral index accuracy degrades faster than intensity...

(Different algorithms produced different #s of usable spectral indices)

High dynamic range test ($>10^4$) - compare four methods

MT-MFS

6 μ Jy rms*

peak res :
15 μ Jy

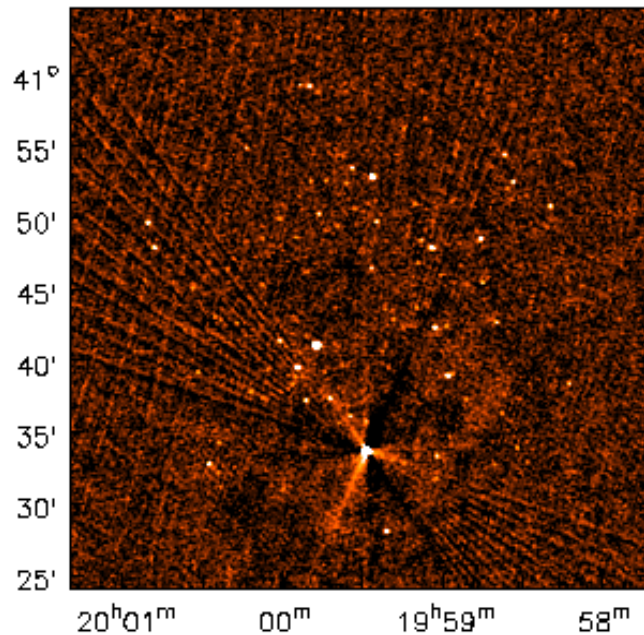
Brightest
Source :
100 mJy

Cube

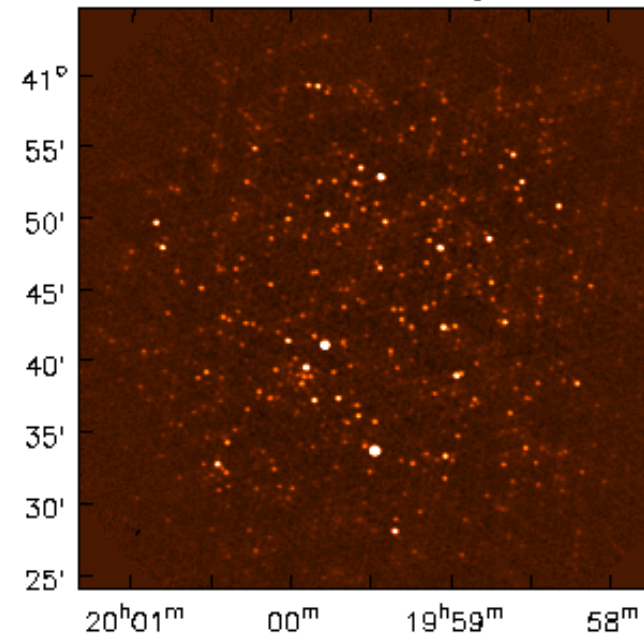
4 μ Jy rms

peak res :
20 μ Jy

MTMFS



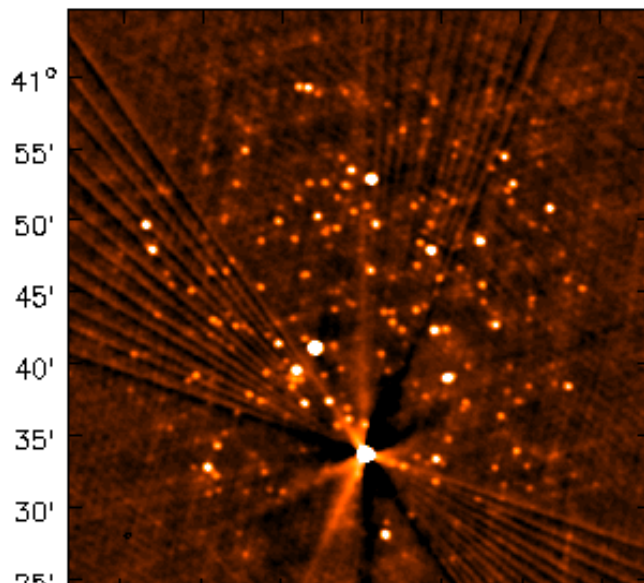
MTMFS + WB-AW-Projection



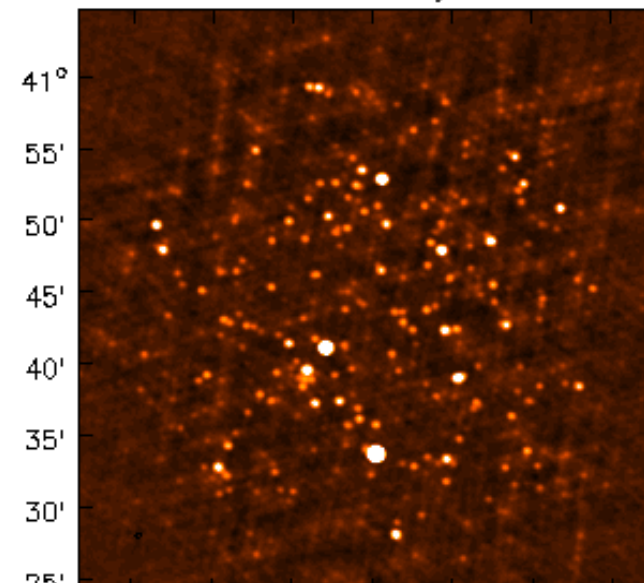
MT-MFS
+
WB-AWP

2 μ Jy rms

Cube



Cube + AW-Projection



Cube
+
AW-Proj

3 μ Jy rms

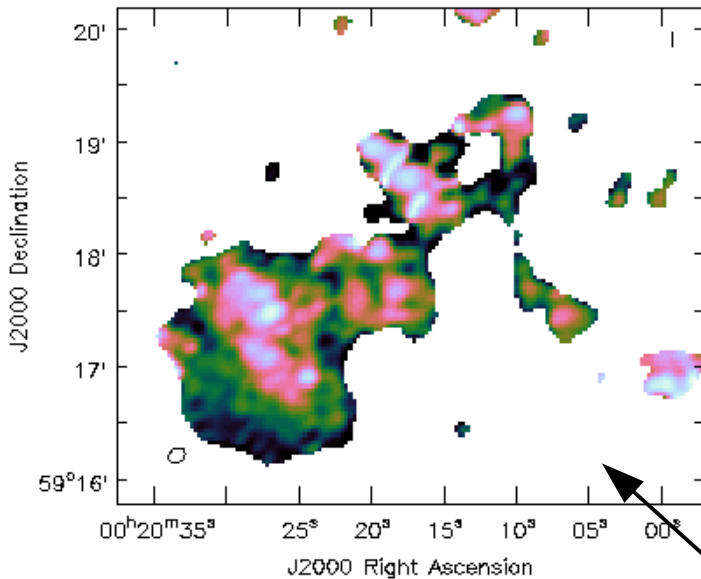
Wideband VLA imaging of IC10 Dwarf Galaxy [Heesen et al, 2011]

IC10 Dwarf Galaxy :

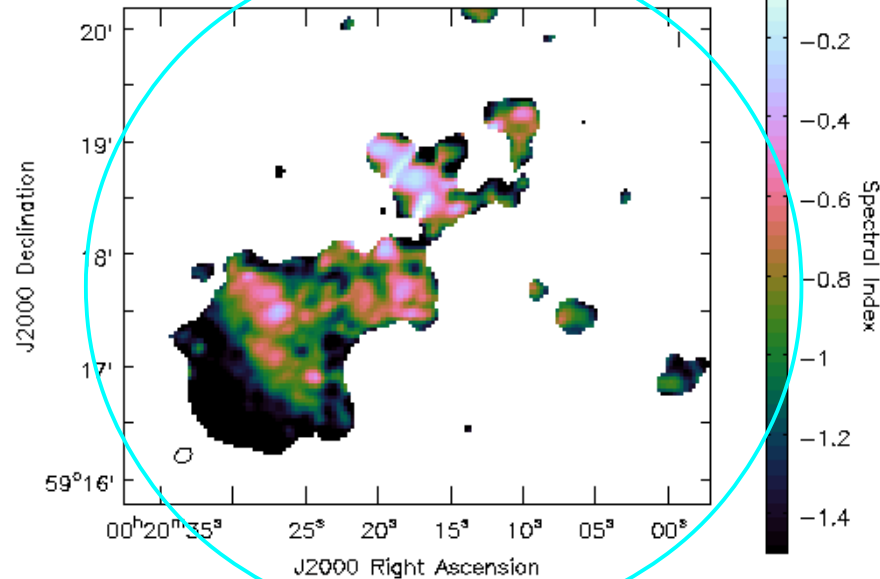
Spectral Index across C-Band.

Dynamic-range ~ 2000

After PB-correction



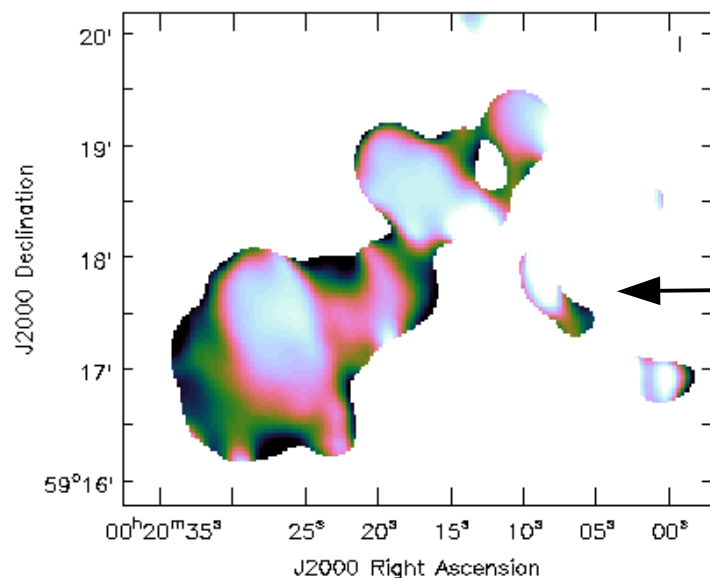
Before PB-correction



50% of PB

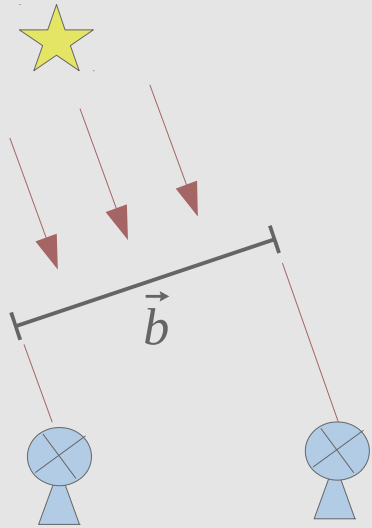
MT-MFS : Wide-band PB-correction after multi-term multi-scale MFS.

Cube : Spectral-index map made by cube imaging, smoothing to lowest resolution, and spectral fitting.



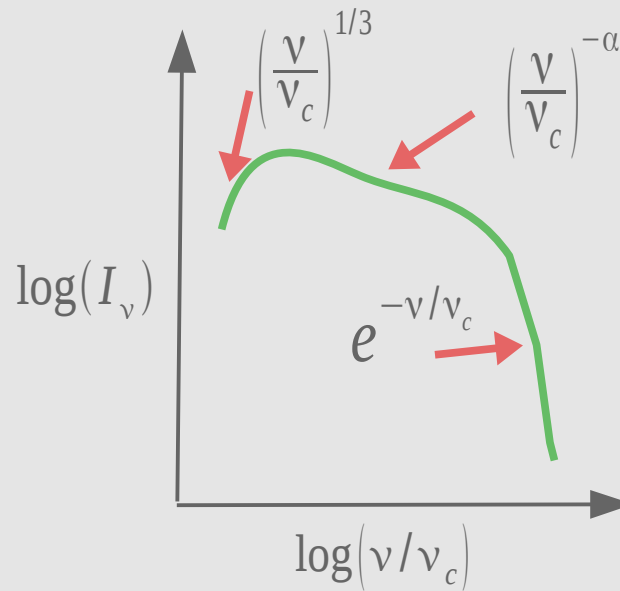
The instrument and the sky change with frequency...

UV-coverage



$$S(u, v)_\nu = \frac{\vec{b}}{\lambda} = \frac{\vec{b} \nu}{c}$$

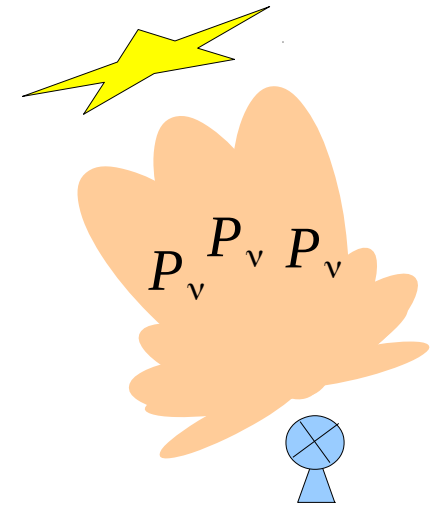
Sky Brightness



$I(\nu)$

Primary Beams

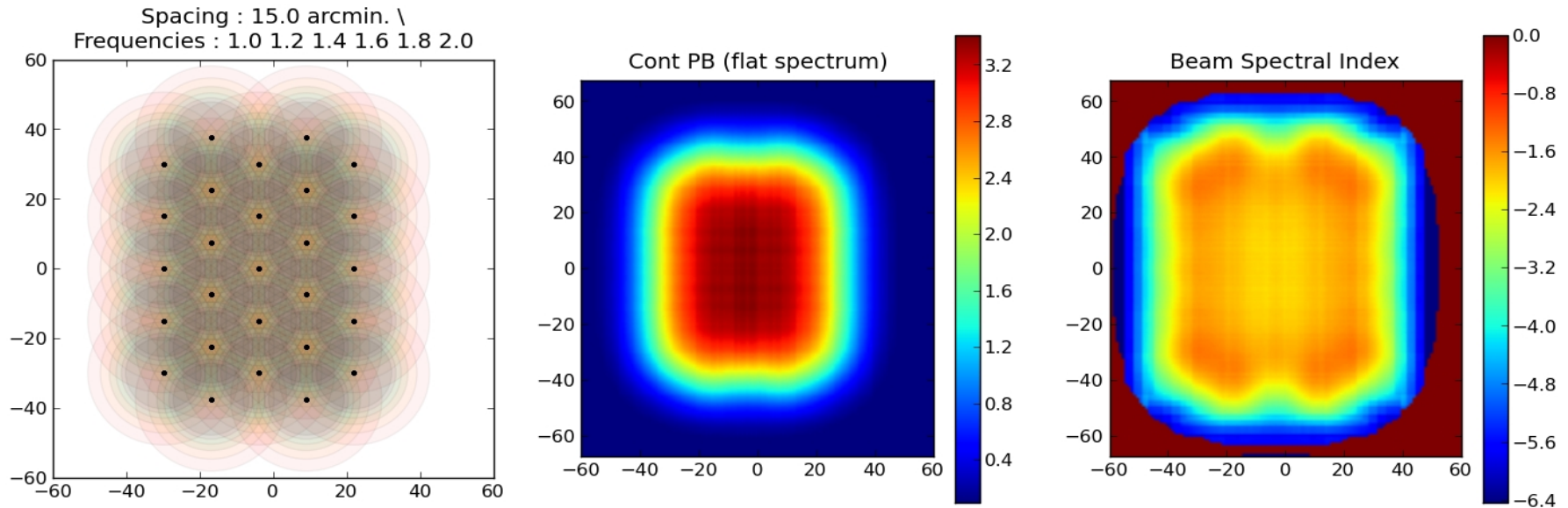
(Mosaic)



$$HPBW_\nu = \frac{\lambda}{D} = \frac{c}{\nu D}$$

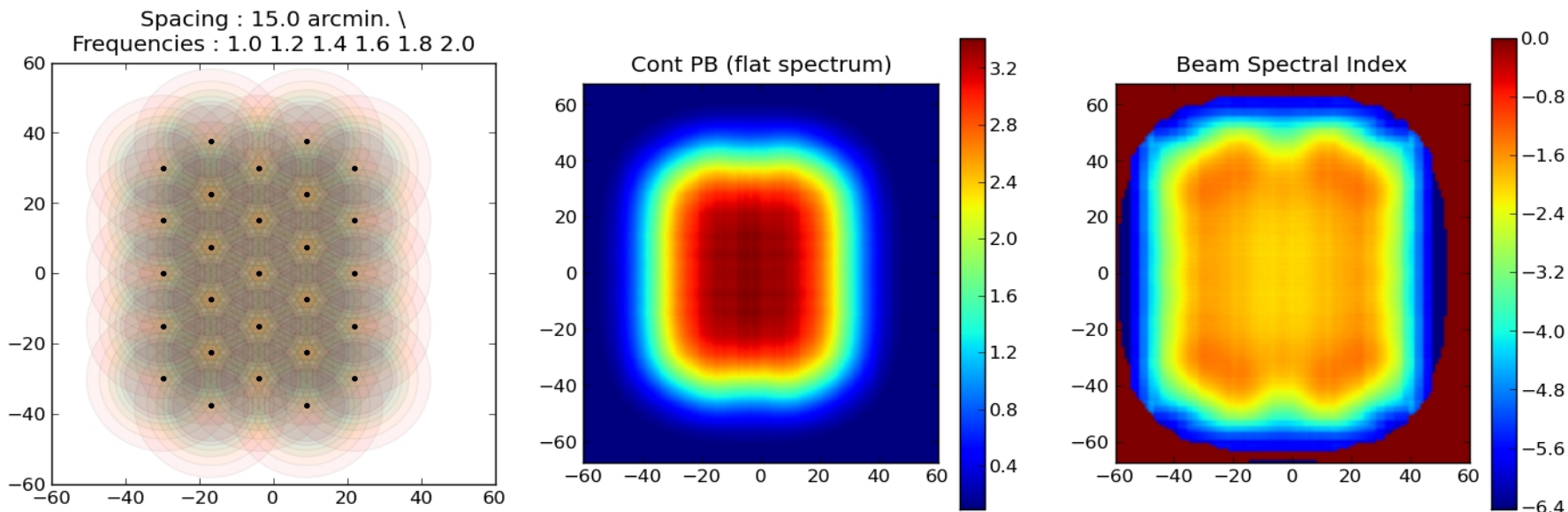
Wide-Band Wide-Field Imaging : Mosaics

The mosaic primary beam has an artificial spectral index all over the FOV



Wide-Band Wide-Field Imaging : Mosaics

The mosaic primary beam has an artificial spectral index all over the FOV



Algorithms :

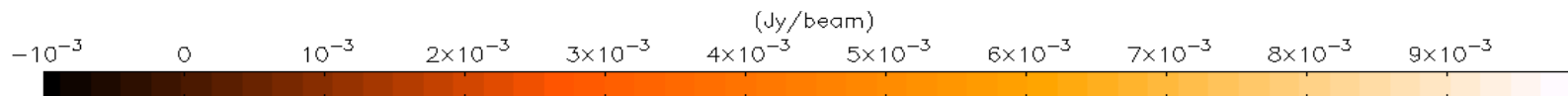
- Deconvolve Pointings separately or together ([Stitched vs Joint Mosaic](#))
 - Impacts image fidelity, especially of common sources.

(Ref: Wide-Field Imaging – Mosaicing lecture)

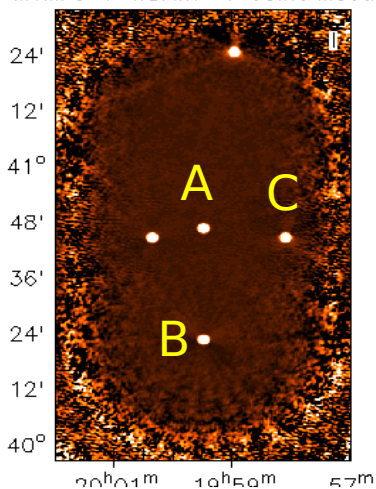
- Deconvolve Channels separately or together ([Cube vs MFS](#))
 - Impacts imaging fidelity and sensitivity, dynamic range
- Use A-Projection or not ([Accurate vs Approximate PB correction](#))
 - Impacts dynamic range and spectral index accuracy

Comparison of several wideband mosaic methods

Dataset : L-Band D-config, 3 pointings, 5 sources (intensity = 1 Jy, alpha= -0.5)

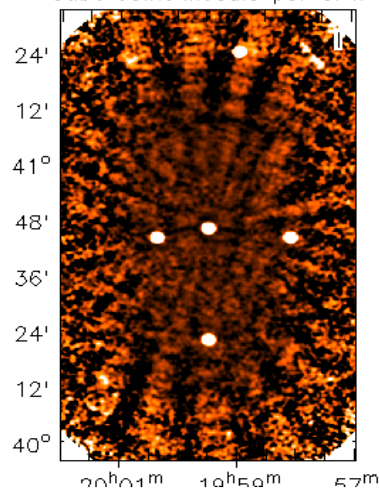


MTMFS + WBAWP + Joint Mosaic



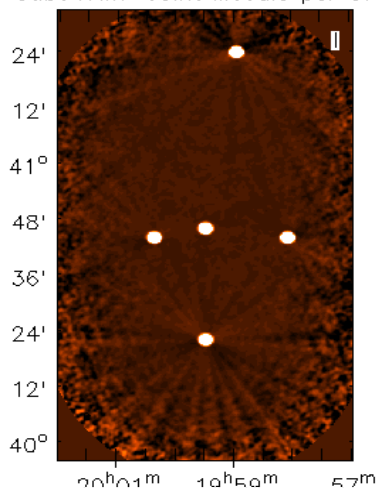
Joint Mosaic
Wideband-AP

Cube Joint Mosaic per SPW



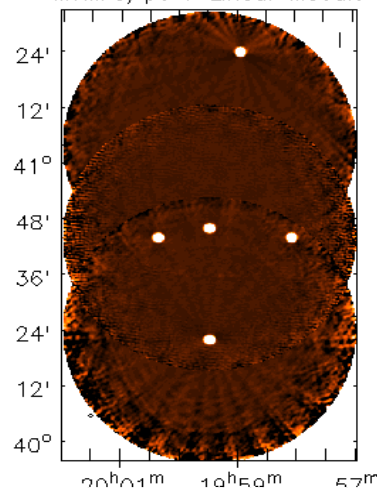
Joint Mosaic
Cube

Cube+AWP Joint Mosaic per SPW



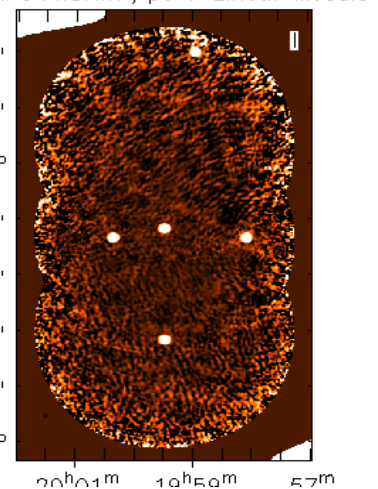
Joint Mosaic
Cube-AP

MTMFS/pt + Linear Mosaic



Stitched Mosaic
Wideband

MTMFS+WBAWP/pt + Linear Mosaic

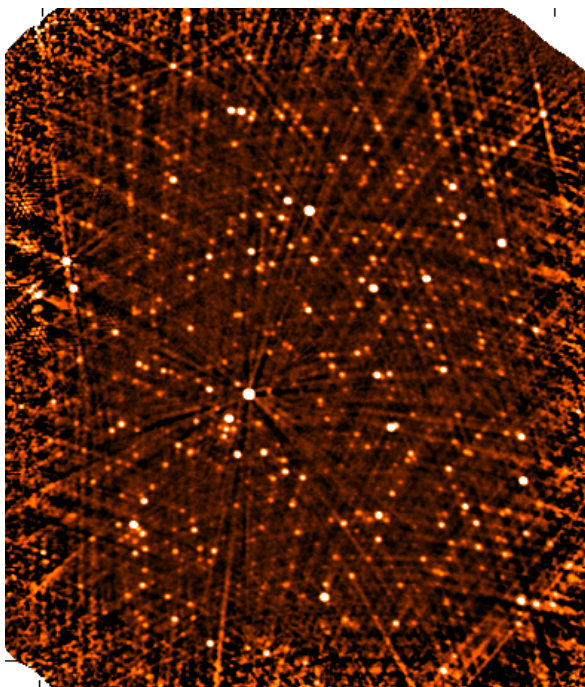


Stitched Mosaic
Wideband-AP

A	1.0002 -0.508	0.98 -0.52	1.011 -0.51	0.88 -0.87	1.01 -0.48
B	1.0004 -0.502	0.99 -0.47	1.012 -0.48	0.90 -0.80	0.99 -0.50
C	1.0005 -0.507	0.887 -0.62	1.04 -0.53	0.73 -1.6	1.007 -0.7

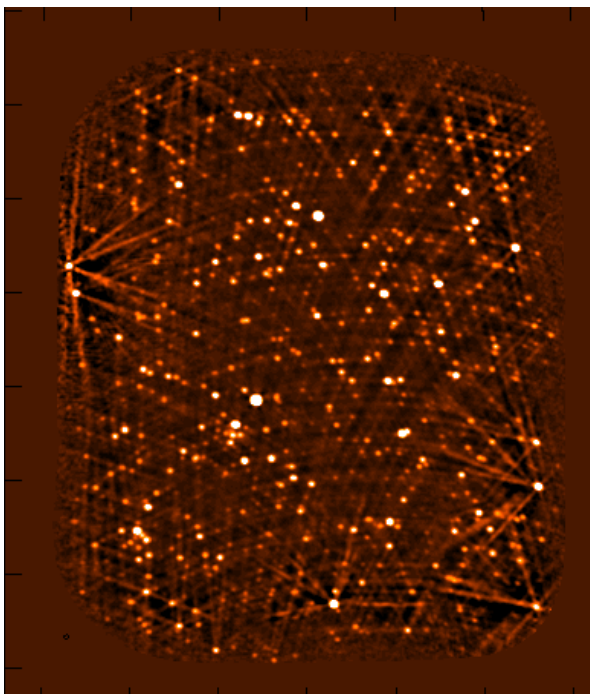
Cube + Joint Mosaic (with static Primary Beams)

Dyn.Range = 5000:1



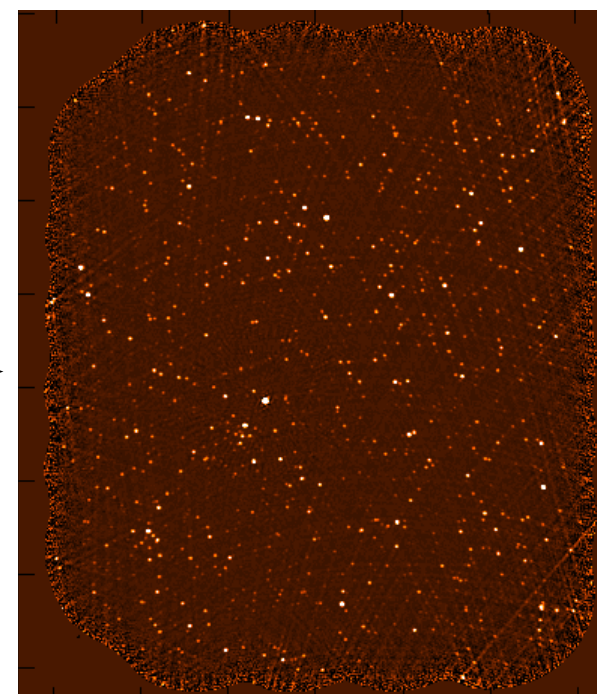
Cube + A-Projection + Joint Mosaic

Dyn.Range = 10000:1



Wideband A-Proj + Joint Mosaic + Multi-term MFS

Dyn.Range = 40000:1



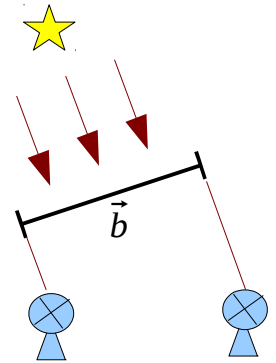
Method	I/I_{true}	I/I_{true}	I/I_{true}	$\alpha - \alpha_{true}$	$\alpha - \alpha_{true}$
Intensity Range	$> 20\mu Jy$	$5 - 20\mu Jy$	$< 5\mu Jy$	$> 50\mu Jy$	$10 - 50\mu Jy$
Cube	0.9 ± 0.1	0.9 ± 0.3	0.9 ± 0.5	-0.5 ± 0.2	-0.6 ± 0.5
Cube + AWP	1.0 ± 0.05	1.0 ± 0.2	1.0 ± 0.3	-0.15 ± 0.1	-0.1 ± 0.25
MTMFS + WB-AWP	1.0 ± 0.02	1.0 ± 0.04	1.0 ± 0.15	-0.05 ± 0.05	-0.1 ± 0.2

So far, none of our methods produced accurate spectral indices below 10 micro Jy.

Wide-Band (wide-field) Imaging - Summary

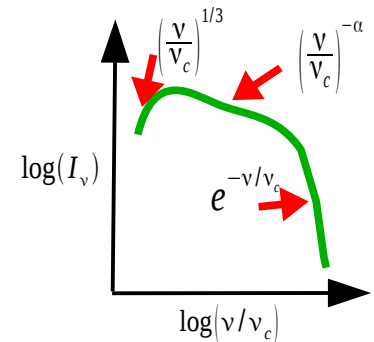
- UV coverage changes with frequency

- Avoid bandwidth-smearing
- Use multi-frequency-synthesis
 - to increase the uv-coverage and image-fidelity
 - to make images at high angular-resolution



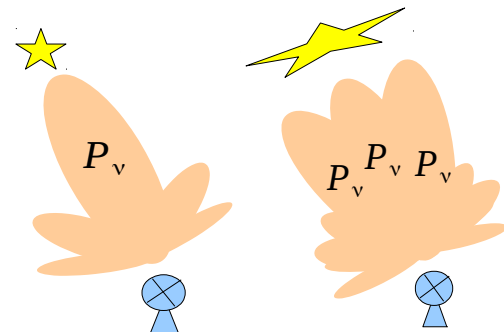
- Sky brightness changes with frequency

- reconstruct intensity and spectrum together (MT-MFS)
- (or) make a Cube of images



- Instrumental primary beam changes with frequency

- divide PB-spectrum from observed sky-spectrum.
- apply wide-field imaging techniques to eliminate the PB frequency dependence during imaging.
- Stitched vs Joint mosaics



Wide Band (wide field) Imaging – some guidelines

- MFS has better imaging fidelity, resolution and sensitivity than Cube
- For 2:1 bandwidth, the dynamic range limit with standard MFS (no spectral model) is few 100 to 1000 for a spectral index of -1.0
- For point sources,
MT-MFS spectral index errors < 0.1 for $\text{SNR} > 50$ (2:1 bwr)
for $\text{SNR} > 10$ (4:1 bwr)
- For extended emission
MT(MS)-MFS spectral index errors < 0.2 for $\text{SNR} > 100$
- For 2:1 bwr, the PB's artificial spectral index at the HPBW is -1.4
- VLA beam squint and rotation effects appear at the few $\times 10^4$ DR.
- Joint mosaics have better imaging fidelity than stitched mosaics.
- The current most practical approach to wideband mosaicing is cube joint mosaicing using A-Projection (accuracy vs cost vs software)

Example : SNR G55.7+3.4

7 hour synthesis, L-Band, 8 spws x 64 chans x 2 MHz, 1sec integrations

Due to RFI, only 4 SPWs were initially imaged (1256, 1384, 1648, 1776 MHz)

J2000 Declination

22°00'

45'

30'

15'

21°00'

45'

Imaging Algorithms applied : MS-MFS with AW-Projection

(nterms=2, multiscale=[0, 6, 10, 18, 26, 40, 60, 80])

Peak Brightness : 6.8 mJy

Extended Emission : ~ 500 micro Jy

Peak residual : 65 micro Jy

Off-source RMS : 10 micro Jy (theoretical = 6 micro Jy)

19^h26^m

24^m

23^m

22^m

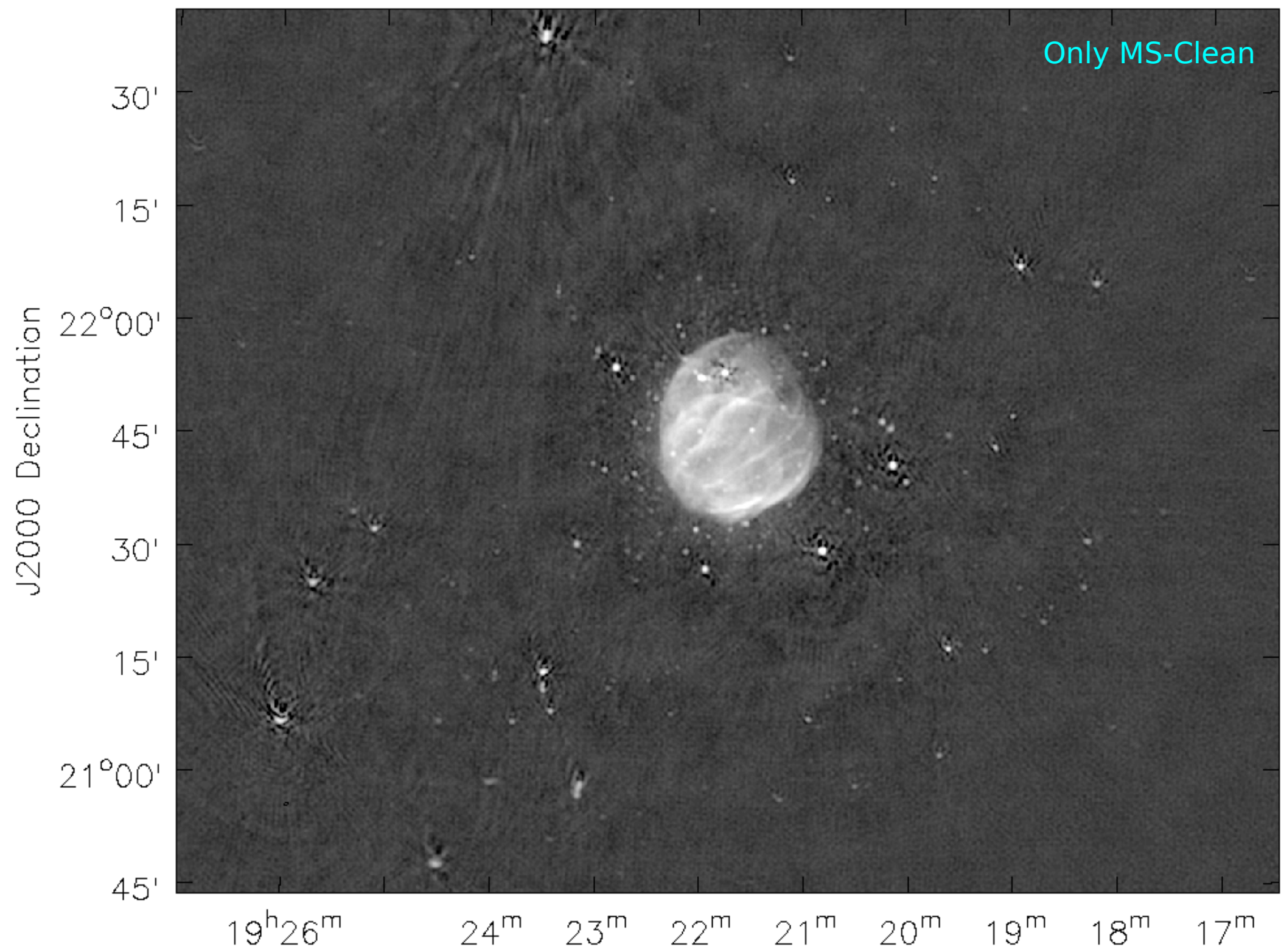
21^m

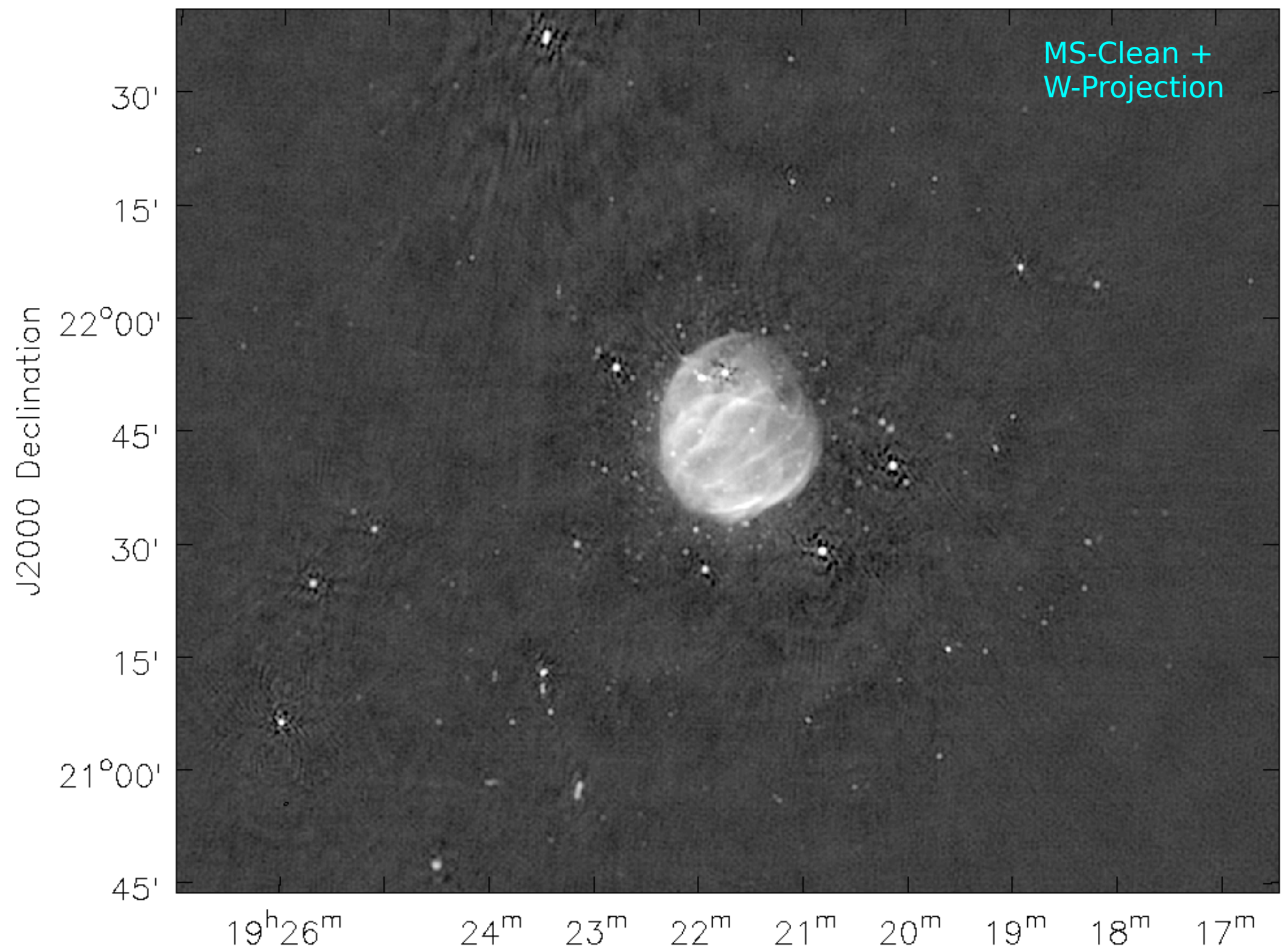
20^m

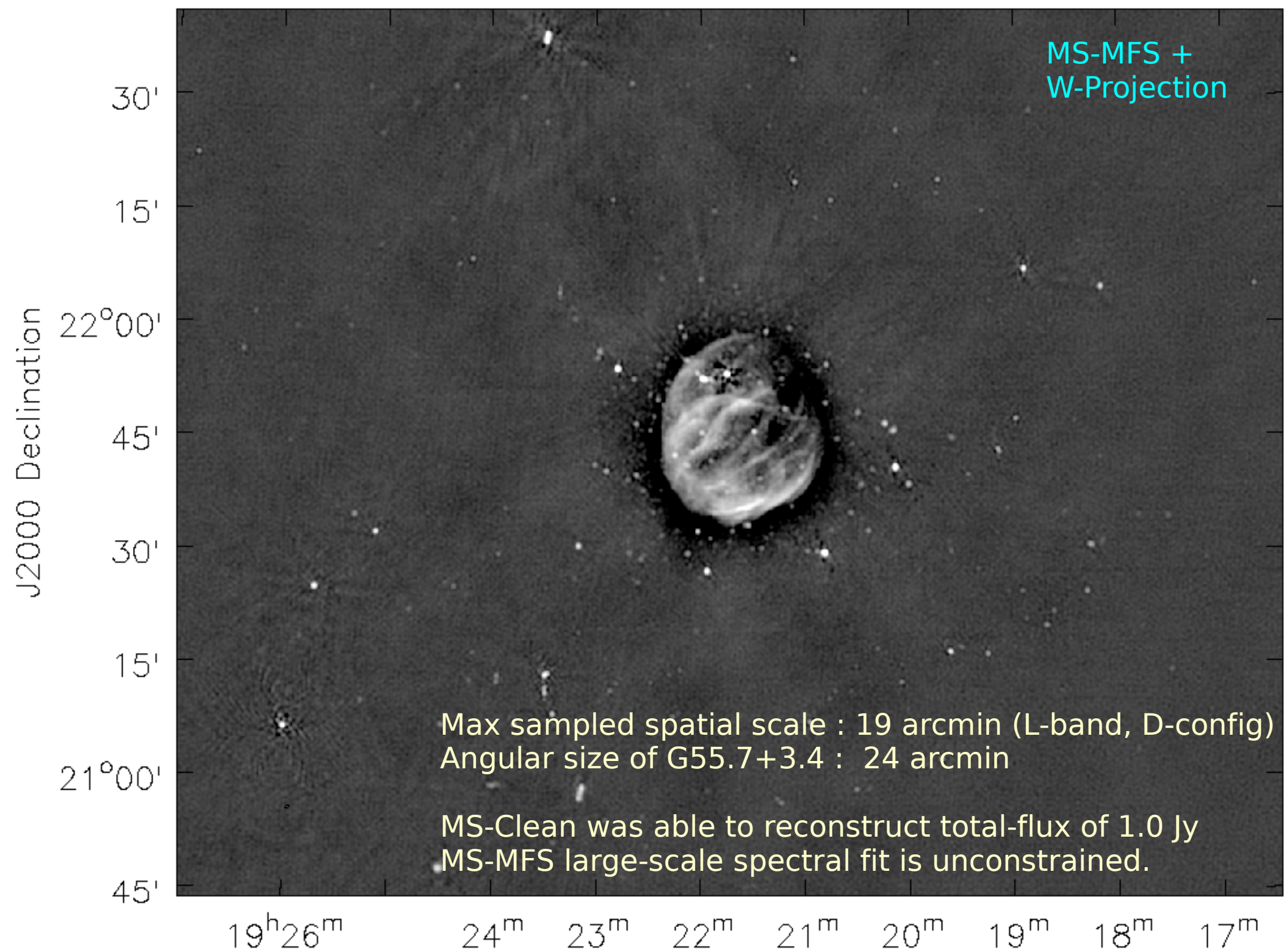
19^m

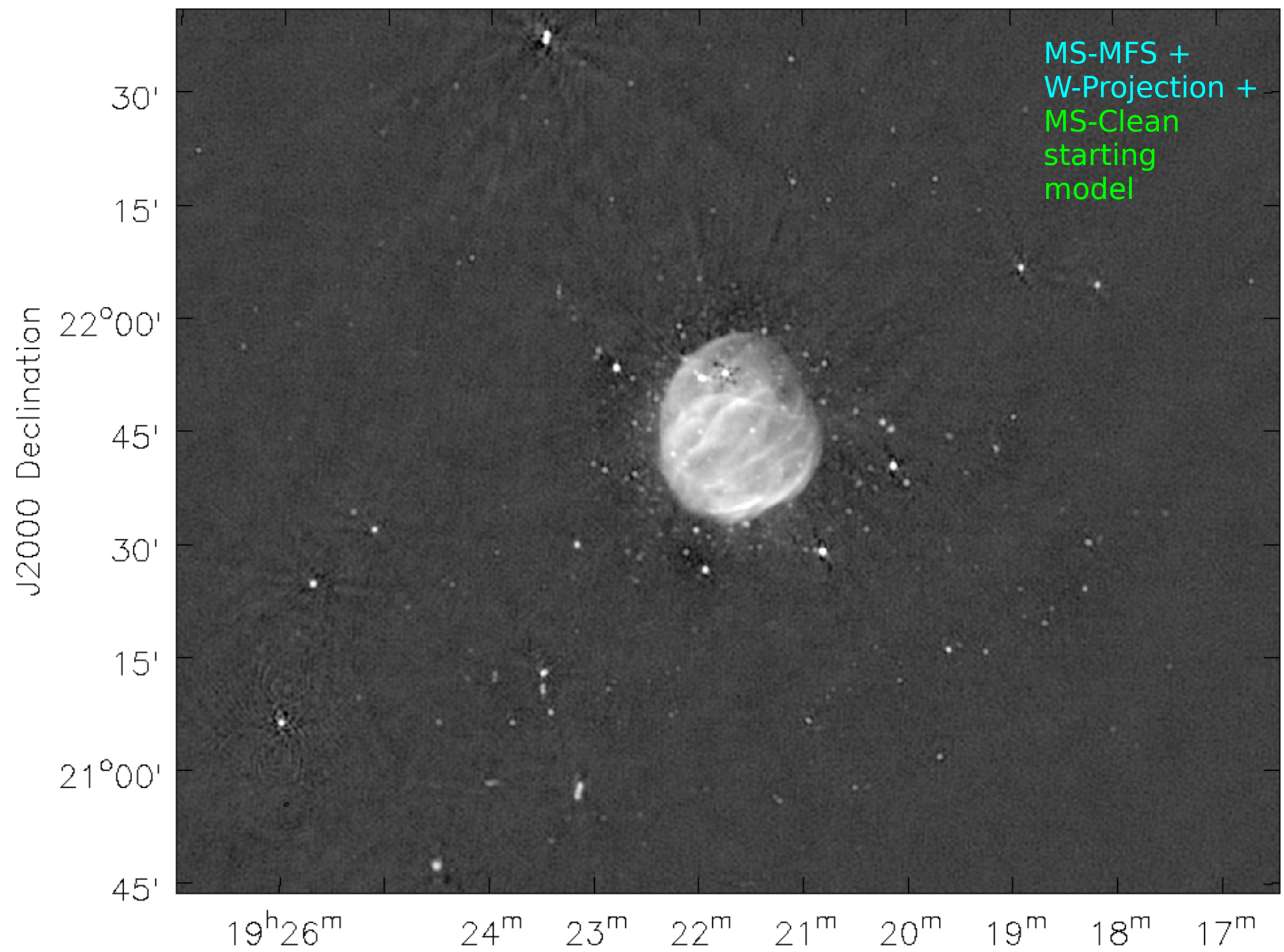
18^m

17^m



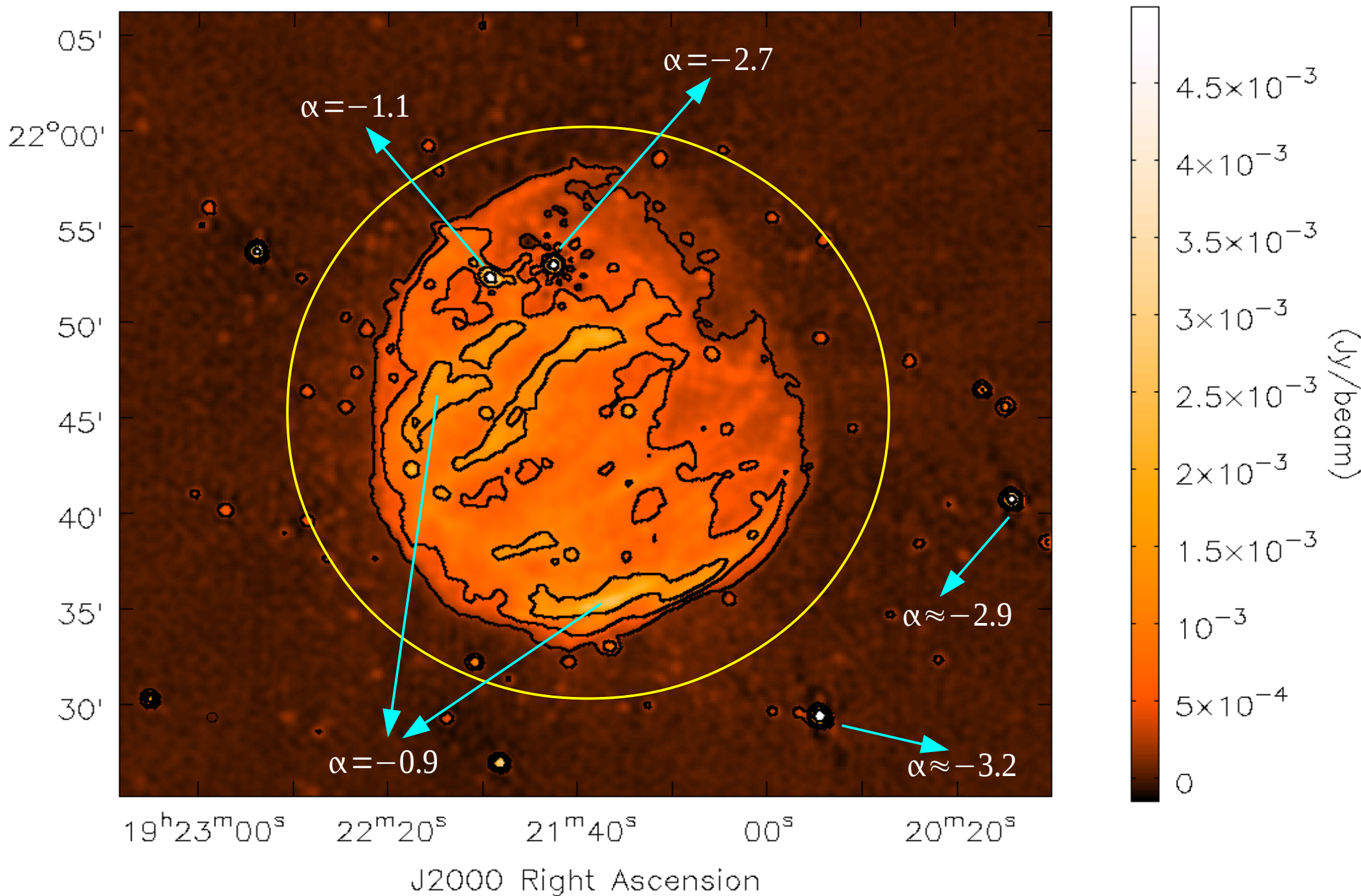






G55.7+3.4 : Supernova-Remnant + Pulsar

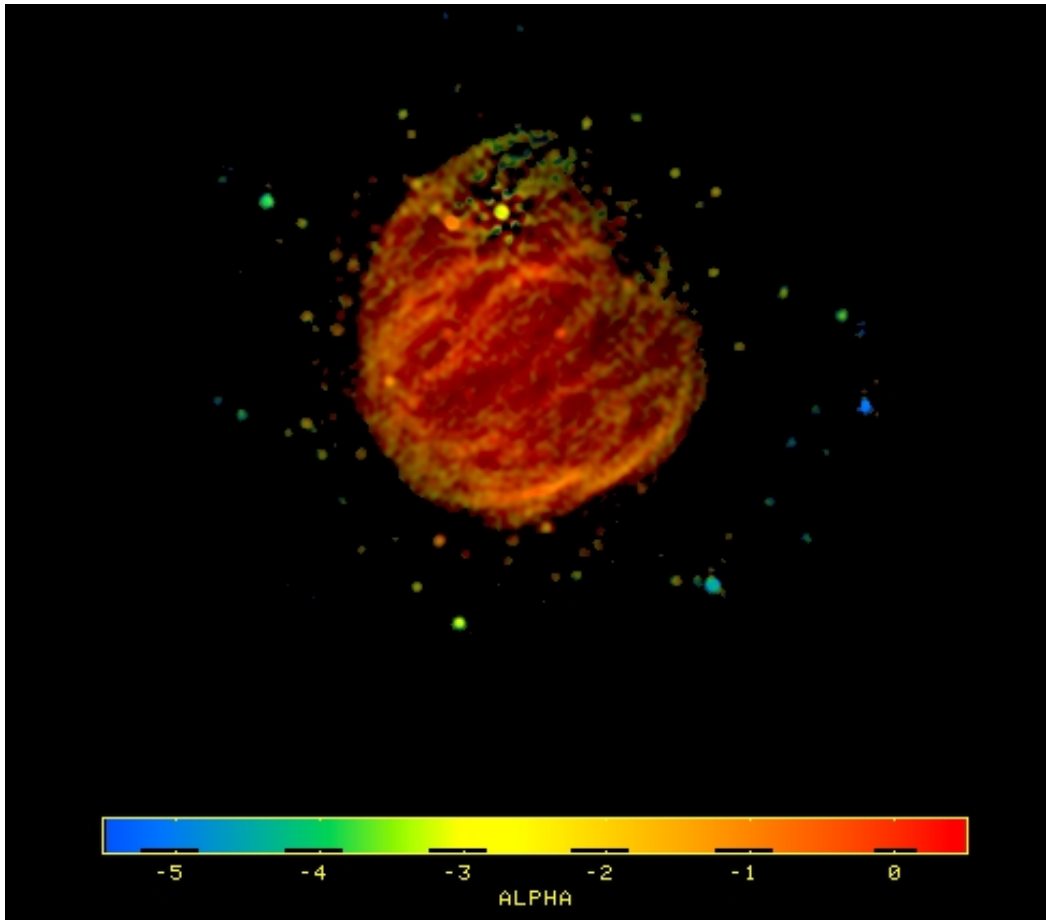
Spectral Indices are artificially-steepened by the Primary Beam



Spectral Indices before and after WB-A-Projection

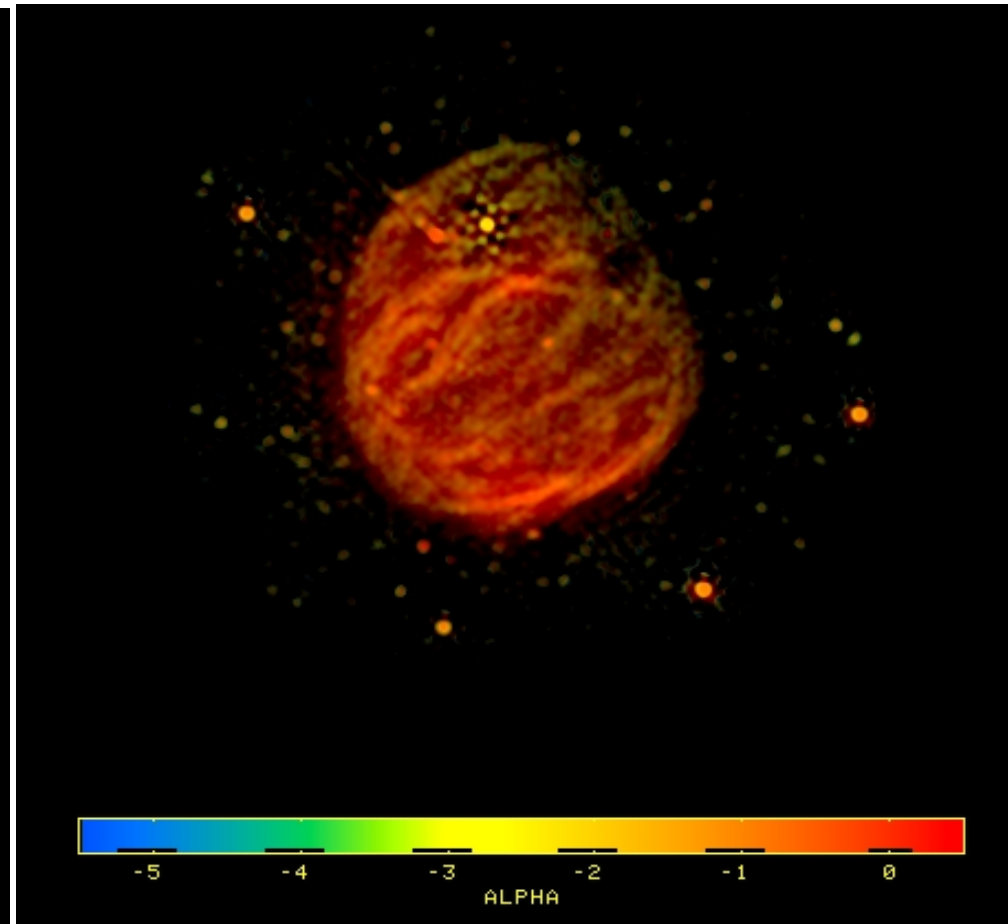
Without PB correction

Outer sources are artificially steep



With PB correction (via WB-AWP)

Outer sources have correct spectra



Intensity-weighted spectral index maps (color = spectral index from -5.0 to +0.2)

Wide-field sensitivity because of wide-bandwidths

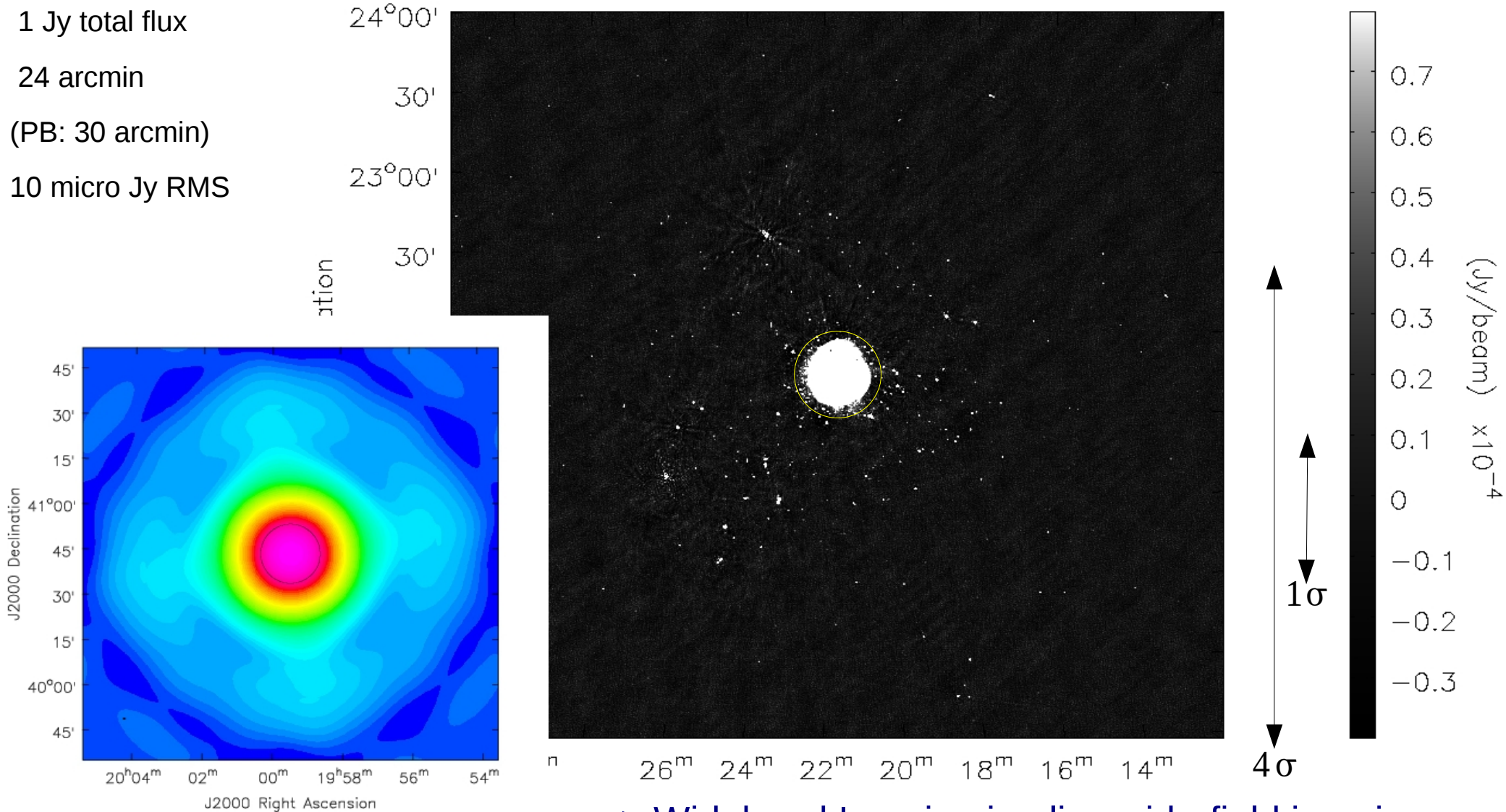
G55.7+3.4 : 4 x 4 degree field-of-view from one EVLA pointing

1 Jy total flux

24 arcmin

(PB: 30 arcmin)

10 micro Jy RMS



=> Wideband Imaging implies wide-field imaging

Summary

Broad-band receivers provide increased instantaneous sensitivity



Cube-imaging will suffice for a quick-look, and bright simple targets



For deep imaging, do wideband MFS (intensity and spectrum)



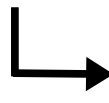
Apply appropriate wideband primary beam correction



Choose your algorithms based on desired accuracy and computing cost



Pay attention to the **many** sources of error in this whole process.



New astrophysics made possible by new instruments !

→ High dynamic range, wideband, full-polarization, mosaic imaging
--> An ACTIVE area of research for VLA and other new telescopes